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# **THESIS**

RESONANT ACOUSTIC DETERMINATION OF COMPLEX ELASTIC MODULI

by

Tan, Beng Hock

March 1991

Thesis Advisor: Co-Advisor:

Section 199

Steven L. Garrett David A. Brown

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# Resonant Acoustic Determination of Complex Elastic Moduli

by

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B.Eng(Mech), National University of Singapore, 1981

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN ENGINEERING SCIENCE

from the

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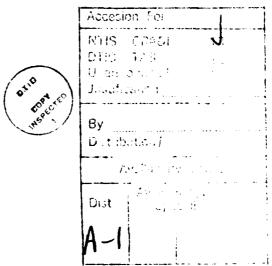
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### **ABSTRACT**

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The reader is cautioned that computer programs developed in this research may not have been exercised for all cases of interest. While every effort has been made, within the time available, to ensure that the programs are free of computational and logic errors, they cannot be considered validated. Any application of these programs without additional verification is at the risk of the user.

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# LIST OF SYMBOLS

 $a_n$  = coefficient of polynomial function

 $a_T$  = temperature-frequency shift factor

b = loss tangent empirical constant

 $c_F$  = phase speed of flexural wave

 $c_L$  = phase speed of longitudinal wave

 $c_T$  = phase speed of torsional wave

d = diameter of rod

f = resonance frequency

 $f_n^F$  = normal mode frequency of flexural vibration

 $f_n^L$  = normal mode frequency of longitudinal vibration

 $f_n^T$  = normal mode frequency of torsional vibration

 $\Delta f = -3 \text{ dB bandwidth}$ 

 $k, k_1, k_2 =$  spring constant of material

 $k^*$  = complex spring constant

k' = real part of complex spring constant

k'' = imaginary part of complex spring constant

m = mass of rod

n = mode number

u = speed of vibration at the ends of rod

z = distance from neutral axis

A = constant of proportionality

B = magnetic field magnitude

E = Young's modulus

 $E_{st}$  = energy stored

 $E_d$  = average rate of energy dissipation

F = force

G = shear modulus

 $G^*$  = complex shear modulus

G' = shear storage modulus

G'' = shear loss modulus

I = electrical current

L = length of rod or effective length of coil

N = number of turns of coil

Q = quality factor

 $R, R_2$  = mechanical resistance

S = cross-sectional area of rod

T = temperature

 $T_s$  = standard reference temperature for WLF equation

 $V_{in}$  = in-phase output voltage of lock-in amplifier

 $\delta$  = phase angle between stress and strain

 $\phi$  = angular displacement

 $\lambda$  = wavelength

 $\kappa$  = radius of gyration

 $\rho$  = mass density

 $\sigma$  = Poisson's ratio, or standard deviation

 $\tau$  = relaxation time constant

 $\omega$  = angular frequency

 $\xi$  = linear displacement

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# I. INTRODUCTION

#### A. MOTIVATION

It is important that the mechanical properties of elastomeric or rubber-like materials be accurately measured and their dependence on temperature, static pressure and other ambient parameters be determined for many fields of science and engineering. These rubber-like materials are being used in various applications such as materials for anti-vibration mounting, hydrophone designs and other acoustics applications. It is known that the static and dynamic moduli of plastics can differ substantially [Ref. 1] and in many situations, it is the dynamic moduli that are the appropriate moduli which determine the quantity of interest such as the dissipative characteristics of vibration isolation material, the resonant frequencies of a linear mechanical system and the sensitivity of many transduction mechanisms.

For most applications, the elastic moduli at the frequencies of intended operations are of interest rather than the static modulus. Nevertheless, manufacturers' specifications for elastic constants of castable polymers are not particularly useful as they are usually determined by static techniques and rarely contain more than one modulus if available. For an isotropic, homogeneous material, all the elastic properties can be completely characterized by just two moduli. Therefore, development of a technique that can accurately determine these dynamic properties is essential for applications engineers and designers and is the topic of this research.

# **B. TECHNIQUE**

In general, the dynamic moduli of a material can be determined by forced vibration test methods. That is, directly measuring the force and resulting displacement or acceleration and using Hooke's law. These can be broadly classified as resonant and non-resonant methods, each method having its advantages and disadvantages [Ref. 2]. Resonant based techniques have the advantage of higher signal-to-noise ratio because at resonance, the response of the sample is quality factor, Q, times higher than the response off resonance. This is an important consideration with a high loss material. Further, as the fundamental measurement is frequency, this suggests that one can obtain extremely high precision with a relatively inexpensive instrument such as a frequency counter. The resonant technique used in this research has been described and discussed in detail in a paper written by Garrett [Ref. 3], using a transducer consisting of coils of magnet wire placed in the magnetic field created by a pair of permanent magnets. Using identical transducers for driver and receiver (pick-up), it is able to selectively excite a single rod-shaped sample of circular or elliptical cross-section into torsional, flexural and longitudinal resonant modes. After obtaining the resonant frequency, knowing the mass density,  $\rho$ , and dimensions of the sample, the storage modulus can be obtained from the fact that the bar resonance is proportional to the appropriate wave speed. The complex moduli of the rubber-like material can be obtained together with the measurement of the quality factor, Q, or the free decay time,  $\tau$ . A commercially available device can be obtained from Reference 4.

#### C. HISTORY

The resonant bar technique, as it will be called from now onward, is a refinement of one developed by Barone and Giacomini [Ref. 5] to study the modes of vibration of bars of different cross sections. It was used as a teaching laboratory experiment at University of California Los Angeles by Professor Isadore Rudnick and currently, it is being used in acoustic laboratory courses at Naval Postgraduate School to demonstrate modes of bar, and recently, by Wetterskog, Beaton and Serocki [Ref. 6], to determine the dynamic moduli and their temperature dependence for numerous sample of materials for fiber-optic

hydrophone applications. Improvements to the resonant bar technique and continuous resonance tracking to yield both storage and loss moduli as a function of temperature and frequency are described in this thesis.

# II. THEORY

#### A. DYNAMIC MODULI DETERMINATION

A uniform, isotropic, cylindrical rod of a homogeneous solid with a diameter, d, and length L, with  $L > \lambda >> d$ , so that radial motion can be neglected, will propagate three independent waves. These modes will exhibit resonances at appropriate frequencies, depending on the boundary conditions imposed on the ends of the rod. Applying the boundary conditions to a slender rod with unrestricted ends, *i.e.*, free-free boundary conditions, the solutions to the resonant modes can be obtained [Ref. 7: pp. 57-76, Ref. 3].

# 1. Non-dispersive Modes

The displacement,  $\xi$ , and angular displacement,  $\phi$ , associated with the longitudinal and torsional modes satisfy an ordinary second-order wave equation [Ref. 8: pp.94, 112]. For a free-free boundary condition, the resonances are harmonically related and correspond to an integral number of half-wavelength contained within the length of the rod. It should be noted that the assumed boundary condition does not take the added mass of the transducers and their adhesive into account. Nevertheless, the effect is not ordinarily significant since the additional mass is rarely more than a few percent of the mass of the rod.

# a. Longitudinal Vibration - Dynamic Young's Modulus

The phase speed of the longitudinal waves,  $c_L$ , is given by Young's modulus, E, and the mass density,  $\rho$  [Ref. 7: p. 59]

$$c_L = \sqrt{\frac{E}{\rho}} \tag{1}$$

The normal-mode frequencies of the bar are then given by

$$f_n^L = \frac{nc_L}{2L}; \quad n = 1, 2, 3, \dots,$$
 (2)

where n is the mode number of the vibration corresponding to the number of nodes in the standing wave. When the wavelength,  $\lambda$ , begins to become comparable with the lateral dimension of the bar, the assumption of slenderness fails and the normal-mode frequencies deviate increasingly from a harmonic progression. Nevertheless, for a slender rod, these two equations can be used to solve for Young's modulus of the bar

$$E = 4\rho L^2 \left(\frac{f_n^L}{n}\right)^2. \tag{3}$$

## b. Torsional Vibration - Dynamic Shear Modulus

For a cylindrical rod, the phase speed for the torsional waves,  $c_T$ , is given by the shear modulus, G, and the mass density,  $\rho$  [Ref. 8: p.11]

$$c_T = \sqrt{\frac{G}{\rho}} \tag{4}$$

If the rod was elliptical, with major and minor radii, a and b, respectively, the speed is modified by the multiplicative factor  $[2ab/(a^2+b^2)]$  [Ref. 9]. Applying the free-free boundary condition leads to a series of harmonic modes with frequencies given by

$$f_n^T = \frac{nc_T}{2L} \; ; \; n = 1, 2, 3, \dots$$
 (5)

These two equations can be used to solve for the shear modulus of the bar

$$G = 4\rho L^2 \left(\frac{f_n^T}{n}\right)^2,\tag{6}$$

where n is again the mode number of the vibration. By obtaining the resonance frequency of both the torsional and longitudinal modes of a homogeneous, isotropic rod of known mass and dimensions, the complete set of elastic constants (i.e., bulk modulus, Poisson's ratio, etc.) can be determined as only two independent moduli are required to completely characterize such a system.

# 2. Dispersive Mode - Flexural Mode

The flexural phase speed,  $c_F$ , is given as [Ref. 7: p. 71]

$$c_F = \sqrt{2\pi f \kappa c_L},\tag{7}$$

where  $\kappa$  is the radius of gyration given by [Ref. 7: p.69]

$$\kappa^2 = (\frac{1}{S}) \int z^2 dS$$
(8)

where S is the cross-sectional area of the rod, and z is the distance of an element above the neutral axis in the direction of flexure. Therefore the flexural wave phase speed varies with the square root of the frequency. A slender rod thus exhibits dispersion for flexural mode. The application of free-free boundary condition gives a series of modes that are not harmonic. The frequency of the *n*th overtone,  $f_n^F$ , is given by [Ref. 7: p. 75]

$$f_n^F = \frac{\pi n^2 c_L \kappa}{8L^2}$$
;  $n = 3.0112, 4.9994, 7, 9, 11...$  (9)

for a rod of circular cross-section,  $\kappa = d/4$ , where d is the diameter of the rod. Solving the above equations to obtain Young's modulus

$$E = \frac{1024}{\pi^2} \frac{\rho L^4}{d^2} \left(\frac{f_n^F}{n^2}\right)^2; \quad n = 3.0112, 4.9994, 7...$$
 (10)

#### **B. VISCOELASTIC MODEL OF SOLID**

# 1. Viscoelasticity

Many solids exhibit primarily elastic effects when subjected to low levels of strain and obey Hooke's law. Under a low amplitude dynamic force, there is a corresponding deformation such that in the linear limit, the resulting strain is proportional to the magnitude and in-phase with the applied stress. The imparted energy is recoverable and not dissipated as heat. The ratio of the applied stress to the resulting normalized deformation or strain is equal to the elastic modulus. The modulus of these materials may be independent of frequency over a large range of frequencies. On the other hand, many liquids show appreciable viscous effects. The stress and strain are always 90° out-of-phase under infinitesimal rates of strain, and all of the shear energy transferred to the liquid is dissipated as heat. If the properties of a material fall between an ideal Hookean solid and an ideal Newtonian fluid, which is the case for most polymers, when a dynamic stress is applied, some of the energy input will be stored and some of the energy input will be dissipated. The material may recover part of its deformation when the stress is removed. Under sinusoidal oscillating stress, the strain is neither exactly in-phase with the applied stress nor 90° out-of-phase but it is somewhere in between. Materials whose behavior show such characteristics are called viscoelastic.

# 2. Simple Mechanical Model

The simplest mechanical model of a viscoelastic system is one spring (elastic) and one dashpot (viscous), either in series or in parallel [Ref. 10: pp. 16-18]. A series element is called a Maxwell element and a parallel element is called a Voigt element. Nevertheless, a combination of these elements are needed to accurately represent the viscoelastic properties of a material.

For a Voigt element, the force, F, can be written in terms of the viscous element, R, the elastic element, k, and the displacement,  $\xi$ , as

$$F = (k + j\omega R) \xi, \tag{11}$$

where,  $j = \sqrt{-1}$ , hence, the equivalent complex modulus can be represented as

$$k^* = k + j\omega R, \tag{12}$$

which has a real part and imaginary part and a relaxation time constant,  $\tau$ , and a phase angle,  $\delta$ , given by

$$\tau = \frac{R}{k}, \tag{13}$$

$$\delta = \tan^{-1}\left(\frac{\omega R}{k}\right). \tag{14}$$

$$\delta = tan^{-1} \left( \frac{\omega R}{k} \right). \tag{14}$$

In this simple model, the real component is independent of frequency, but it may be a function of temperature. The imaginary part is definitely a function of frequency and it increases without bound with increasing frequency. Obviously, this model is inadequate to accurately describe the behavior of a viscoelastic material under dynamic stress.

By adding an elastic element in parallel with a Maxwell model, as in Figure 1(a), which has a equivalent circuit as shown in Figure 1(b), the equivalent impedance can be expressed as

$$Z = \frac{F}{u} = \frac{k_1}{j\omega} + \frac{R_2 k_2}{k_2 + j\omega R_2},$$
 (15)

where u is the velocity equal to  $d\xi/dt$ . Then the dynamic force can be written as

$$F = Zu$$

$$= \left(\frac{k_1}{j\omega} + \frac{R_2k_2}{k_2 + j\omega R_2}\right)j\omega\xi$$

$$= \left(k_1 + \frac{\omega^2 R_2^2 k_2}{k_2^2 + (\omega R_2)^2} + j \frac{\omega R_2 k_2^2}{k_2^2 + (\omega R_2)^2}\right) \xi$$
(16)

Hence the equivalent complex modulus is

$$k^* = k_1 + \frac{\omega^2 R_2^2 k_2}{k_2^2 + (\omega R_2)^2} + j \frac{\omega R_2 k_2^2}{k_2^2 + (\omega R_2)^2}$$
(17)

From this expression, it can be seen that the real part and the imaginary part depend on

frequency, and if  $R_2 / k_2$  is a function of temperature,  $k^*$  depends on temperature also. The frequency dependence of k' (real part of  $k^*$ ) and k'' (imaginary part of  $k^*$ ) is shown in Figure 2. Other similar models can be found in Bland [Ref. 11: pp.114-115].

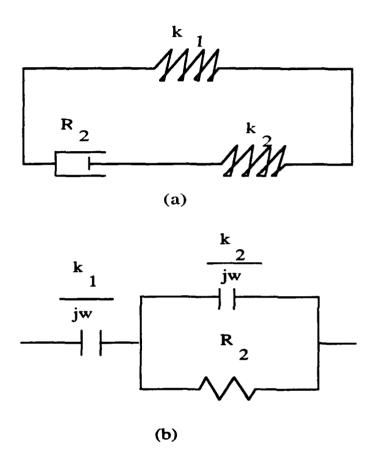


Figure 1. The simple viscoelastic model:

- (a). The mechanical equivalent circuit.
- (b). The electrical equivalent circuit.

This model, with a single relaxation time constant, is similar in approach to that applied by Rudnick in describing the low temperature liquid <sup>3</sup>He [Ref. 12]. Using this model, some preliminary calculations were done. Nevertheless, as it has been stated above, the results for polymeric elastomers deviate substantially. This can be expected as

the behavior of the viscoelastic polymeric material is far more complex than this simple single relaxation time model can fully describe.

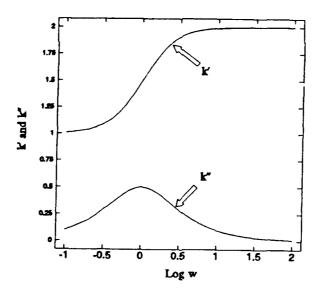


Figure 2. Frequency dependence of k' and k''

# 3. Complex Modulus, Loss Tangent and Quality Factor

In a dynamic measurement, the characteristic elastic modulus of a viscoelastic material can be represented as a complex quantity,  $G^*$ , [Ref. 10: p.32]

$$G^{+} = G' + jG'', \qquad (18)$$

$$\tan \delta \equiv \frac{G^{"}}{G'}.$$
 (19)

The storage modulus, G', is defined as the stress in-phase with the strain in a sinusoidal shear deformation divided by the strain. It is a measure of the energy stored and recovered per cycle.

The loss modulus, G'', is defined as the stress 90° out-of-phase with the strain divided by the strain. It is a measure of the energy dissipated or lost as heat per cycle of sinusoidal deformation.

The loss tangent,  $tan \delta$ , is thus a measure of the ratio of energy lost to energy stored in a cyclic deformation process. It is also equal to the reciprocal of quality factor, Q.

The quality factor of a system can be defined by [Ref. 7: p.16]

$$Q = \frac{f}{\Delta f},\tag{20}$$

where f is the resonant frequency and  $\Delta f$  is the full bandwidth over which the average power has dropped to one-half its resonance value. In terms of relaxation time of the system,  $\tau$ , the quality factor can be expressed as [Ref. 7: p.16]

$$Q = \pi f \tau, \tag{21}$$

or in a simple harmonic oscillator, as a function of mass, m, and mechanical resistance, R, as

$$Q = \frac{2\pi fm}{R} \tag{22}$$

The quality factor can also be expressed as [Ref. 13]

$$Q = \frac{2\pi f E_{st}}{E_d} \tag{23}$$

where  $E_{st}$  is the energy stored in the resonance and  $E_d$  is the average rate of energy dissipation.

If u is the speed of the vibration, F is the amplitude of the constant applied force and m is the mass, at resonance,

$$u = \frac{F}{R}, \tag{24}$$

and thus,

$$R = \frac{F}{u}, \tag{25}$$

combining equations (22) and (25), we arrive at

$$Q = Afu, (26)$$

where A is a constant of proportionality

$$A = \frac{2\pi m}{F}, \tag{27}$$

and hence.

$$\frac{Q}{fu} = A \tag{28}$$

### 4. Dynamic Behavior of Viscoelastic Material

From equation (17), the storage modulus, k', can be expressed as

$$k' = k_1 + \frac{\omega^2 R_2^2 k_2}{k_2^2 + (\omega R_2)^2}$$
 (29)

As  $\omega \to 0$ ,  $k' \to k_I$ , and as  $\omega \to \infty$ ,  $k' \to k_I + k_2$ . As stress is applied at low frequency, the delayed response of the material occurs within the period of the stress reversal. Near equilibrium is achieved at all time. However, as the frequency of the applied stress increases, a point will be reached when the response of the material cannot "keep up" with the stress and its deformation reduces. Consequently, as the frequency of applied stress increases, the storage modulus increases substantially. Moreover, energy loss, which can be measured by the phase angle between the stress and strain ( or the loss tangent ), behaves differently. At low frequencies, where the phase angles are small, the energy losses are small. When frequencies are high, the strain cannot response fast enough to the applied stress, so energy loss remain small too. Thus, the energy loss is highest between

the two frequency limits, when the phase angle and the strain amplitude assume relatively large values. When temperature increases, the mobility of molecules increases, and the strain can track the dynamic stress more closely. With lower temperatures, stiffening of the material occurs. Therefore, the same effect can be achieved by either of the following:

- 1. Increase of temperature or decrease of frequency.
- 2. Decrease of temperature or increase of frequency.

This correspondence allows one to experimentally determine the behavior of materials at frequencies higher than typical apparatus may accommodate by decreasing the sample temperature. Likewise, an experiment can obtain very low frequency performance predictions by measuring the response of sample at elevated temperatures.

Factors like molecular weight, composition of the elastomer, pressure, etc, have their effects on the dynamic properties of the viscoelastic materials but they are not included in this study. [Ref. 14]

As the dynamic response of a viscoelastic material depends on the temperature and frequency [Ref. 10: Chap.11], it appears to be most convenient if one of the two variables is being held constant while the other varies. Nevertheless, only a small range of viscoelastic behavior can be observed over the experimentally accessible frequency range, therefore a complete characterization of the material and its viscoelastic transition is only possible through measurements over a limited range of frequencies at various temperatures. This is the most popular approach to characterize viscoelastic materials in the field today, and it is based on the method of reduced variables developed by Williams, Landel and Ferry [Ref. 10: pp. 294 - 320]. The treatment yields a master curve relating a chosen dynamic property such as storage modulus to a reduced frequency through a temperature-frequency shift factor,  $a_T$ . Each material has its own expression for this temperature-frequency factor. The development of this temperature-frequency factor is discussed in depth in the original paper of Williams, Landel and Ferry [Ref. 15].

In the resonant bar technique, it is required that measurement be made at discrete frequencies which correspond to the normal-modes of the bar. When the temperature of the bar varies, the resonant frequency changes also, and it is tracked by a phase-lockedloop (PLL) which will be discussed in Chapter III. The two variables of interest, i.e., temperature and frequency, are coupled and this presents a challenging problem in presenting and analyzing the experimental data. This problem is rather unique. In the more established technique using an accelerometer as a receiver and a shaker table as a driver [Ref. 16], the excitation frequency can be chosen independently of the temperature. Therefore, it can be seen that the resonant bar technique presents a simple solution to the problem of characterization of material under dynamic stress but with variables that are coupled together. In contrast, the direct measurement method using accelerometer is able to isolate the variables but it is mathematically more complex due to the large mass loading induced by the accelerometer and the attachment to the shaker table. To verify the application of this technique in the investigation, an effort was made to select a material that has been investigated by authorities in this research area, in particular, by Capps of the Naval Research Laboratory - Underwater Sound Reference Detachment (NRL-USRD). The experimental data obtained in this investigation are converted to reduced frequency using the empirical formulae given in Capps' report [Ref. 16].

# III. EXPERIMENTAL APPARATUS

# A. INTRODUCTION

The resonant bar theory is based on simple wave equations. Experimentally, it is also easy to set up, very repeatable due to the free-free boundary condition, and easy to operate. Moreover, with the electrodynamics transduction scheme, one can selectively excite torsional, flexural, or longitudinal modes using the same sample, transducer pair, and experimental set up and thus it is extremely versatile. There is no other known apparatus that can excite all three modes with the same set up, same transducers and with virtually no mass loading effects. Basically, the set up consists of the following components:

- 1. Test sample.
- 2. Two transducers mounted on the sample.
- 3. Test jig for supporting the sample and providing the magnetic field for the transducer coils.
- 4. Electronic instrumentation and computer/controller.

# **B. SAMPLE**

### 1. Preparation of Materials

With the exception of PMMA, the samples used in the study each consisted of two potting components, the resin (part A) and the hardener (part B). They are mixed together in proportions recommended by the manufacturers. The epoxies E-CAST® F82/215, PR1592 and EN9, were heated and degassed at 50°C before mixing. Epoxies PR1570 and EN5, were mixed and degassed at room temperature. The epoxies are heated and degassed in an oven equipped with a vacuum pump. The data sheets for the epoxies are included in Appendix B.

# 2. The Casting of Sample

The cylindrical rod shaped samples are typically 30 cm in length and 1.27 cm (0.5") in diameter, so that a large L/d ratio is achieved. The apparatus can accommodate samples of dimensions with diameters of  $1.2 \pm 0.5$  cm and lengths of  $30 \pm 10$  cm. The samples are made by pouring the prepared elastomers into a mold. The molding tubes for these samples are thick walled (1/8") Teflon® tubing with inner diameter of  $0.5 \pm 0.05$ ". Teflon® is used as the mold material due to its release properties. It does not require any mold release agent in the preparation of a sample.

#### 3. Curing

After the polymer is poured into the mold, the epoxy is cured according to manufacturer's recommendation. When the epoxy is properly cured, the sample is pushed out from the Teflon® tubing. A post cure (at 50°C for 24 hours) is carried out so that the properties of the sample reach their final stable state. Figure 3 shows the sample cast from epoxy EN9 with attached transducer coils and thermistor.

## C. TRANSDUCER COILS

The transducers that act as the driver and receiver of the resonant bar are identical in construction. Each consists of No. 32 gauge copper wire with a nominal diameter of 0.2 mm which are approximately one meter in length, and wound into a 10-turn coil. Each coil weighs about 0.56 gram. They are glued to the ends of the sample by a general purpose plastic cement (GC Electronics 10-324). The ends of the coil are stripped of their insulating layer, and are then coated with solder to assure good conductivity. After each coil is prepared, a continuity check is done to ensure that it is capable of driving and receiving of signals. The coil typically has a resistance of about 1.1  $\Omega$ . If a large signal is desired, the turn ratio can be increased by a factor of N, thus increasing the the signal by  $N^2$  at the expense of added mass of coil. If this added mass becomes significant, a simple

effective length correction factor can be included in the analysis of the result [Ref. 3]. The elastic properties of the plastic cement are not expected to affect the observed resonance and in-phase magnitude of the bar.

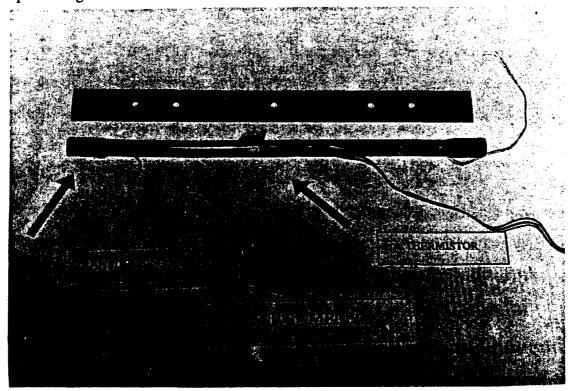


Figure 3. Photograph of a prepared EN9 material sample.

#### D. APPARATUS

The apparatus used in this research, shown in Figure 4, was constructed "in-house" based on a commercial apparatus [Ref 4]. The apparatus is made up of an excitation system, an adjustment system and a suspension system. The electrodynamic excitation system has two pairs of permanent magnets. They provide the necessary magnetic field, so that a varying sinusoidal electrical signal can be converted into a mechanical driving force or torque and the reciprocal effect. The gap between the magnetic poles is approximately two centimeters and it is adjustable to accommodate samples of different

diameters. The magnetic field strength in the gap is approximately  $2.4 \pm 0.1$  KOe (0.24 Tesla) over a temperature range of -17°C to 85°C. The temperature dependence of the magnets was determined to be -2.3 Oe/°C. One pair of the magnets is attached to a sliding platform to accommodate samples of different lengths.

The suspension system for the material sample consists of a pair of "X" supports with rubber bands in a crisscross manner. The rod-shape sample is then placed on the two supports so that a free-free boundary condition can be realized. The "X" supports can be raised or lowered vertically and they can slide horizontally. This is useful as they can support the material sample at any desired points and heights. The smallest effect from the suspension supports is achieved when the rod is placed so that the vibrational nodes rest on the "X" supports. This is not necessary for high loss materials due to the fact that the suspension losses are relatively low as has been quantified in this research (see Chapter IV Section C).

#### E. ENVIRONMENTAL CHAMBER

An environmental chamber is used to control the temperature of the material sample under test. The model used is BHD-408 Bench-Top Temperature and Humidity Test Chamber manufactured by Associated Environmental System. It has a internal dimensions of 24" (Height) x 24" (Width) x 24" (Depth). The temperature range of the system is -17°C to 85°C and the temperature control stability is ±0.5°F (approx. ±0.3°C). It has a dual loop controller capable of independent operation, or it can be controlled by a host computer through a IEEE 488 Interface. For the controller, a computer like the HP9000 series computer can be used. For our application, the local control mode is used. The detailed specification of the chamber is provided in Appendix C.

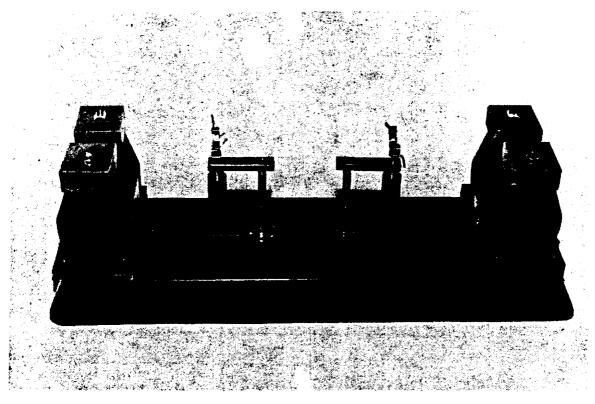
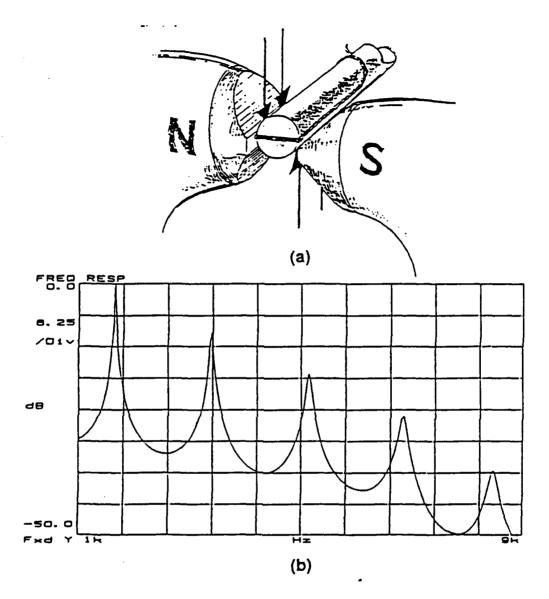


Figure 4. Resonance based moduli measurement apparatus.

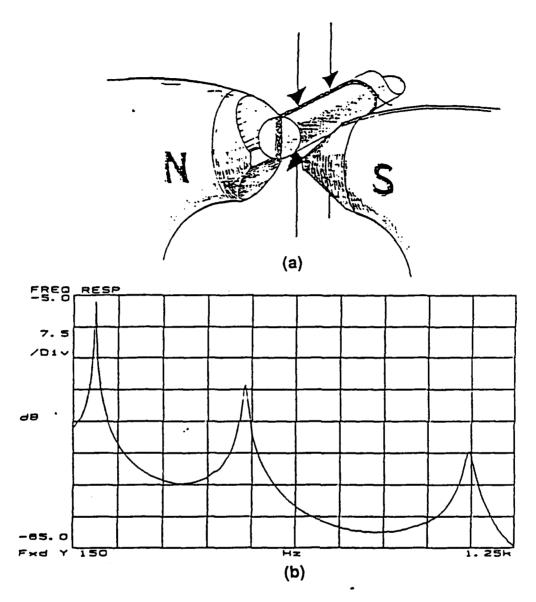
# F. SELECTION AND EXCITATION OF A DESIRED MODE

The material sample is positioned on the apparatus so that the ends of the sample and the transducer coils are in the vicinity of the maximum magnetic field strength during the dynamic moduli measurements. The mode of excitation can be selected by the orientation of the coils within the magnetic field. Figures 5, 6, and 7 shows the relative arrangement of the coil and magnetic field to produce the torsional, flexural and longitudinal vibration respectively. A detailed discussion can be found in Garrett's paper [Ref. 3].



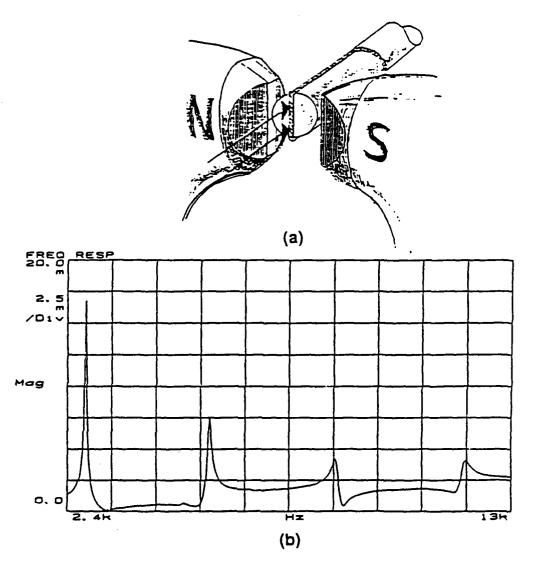
- Figure 5. Torsional vibration excitation and detection scheme

  (a). Arrangement for torsional vibration, the arrows indicate the direction of the electromagnetic forces on the coil for a given phase of current.
  - The torsional frequency response of F-28 (b).



- Figure 6. Flexural vibration excitation and detection scheme

  (a). Arrangement for flexural vibration, the arrows indicate the direction of the electromagnetic forces on the coils for a given phase of current.
  - The flexural frequency response of F-28. (b).



- Figure 7. Longitudinal vibration excitation and detection scheme

  (a) Arrangement for longitudinal vibration, the arrows indicate the direction of the electromagnetic forces on the coils for a given phase of current.
  - The longitudinal frequency response of F-28. (b)

# G. ELECTRONIC INSTRUMENTATION

# 1. Room Temperature Dynamic Moduli Determination

The instrumentation required for determination of dynamic moduli at room temperature is shown in Figure 8. The HP3562A Dynamic Signal Analyzer is used as a signal source as well as a receiver, so that the frequency response of the material sample can be obtained. The excitation signal used is a swept-sine wave with a driving output from the amplifier (HP467A) of typically two to three volts peak-to-peak. Typical frequency response are shown in Figure 5(b), 6(b), and 7(b).

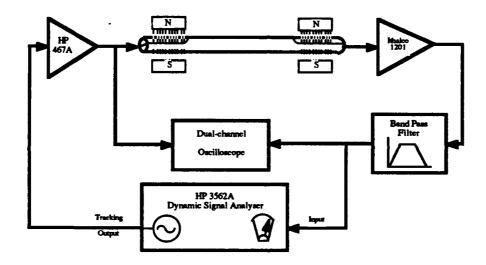


Figure 8. Block diagram of the instrumentation used at room temperature.

The HP3562A has a built-in curve fit function which is used in the study extensively. Using this pole-zero plot curve fit function, the quality factor, resonant frequency, and loss factor can be calculated. The theoretical basis for obtaining the resonance frequency and quality factor from the pole-zero plot is discussed in Brown, Tan and Garrett's paper in Appendix A.

# 2. Temperature and Frequency Dependence of the Dynamic Moduli

The instrumentation for this measurement is shown in Figure 9. The temperature of the material sample is varied by an environmental chamber. Using a lock-in amplifier and a voltage controlled oscillator (VCO) in a phase-locked-loop configuration, the resonant frequency of a selected mode of the material sample is tracked. When the temperature of the specimen changes, its resonance frequency changes due to the changes in the modulus. There is also a contribution to the change in frequency due to the change in the length of the sample via the coefficient of thermal expansion, but this effect is small by comparison and is neglected in this study. Using a HP9836C computer as a system-controller through the HPIB, readings of the temperatures, resonant frequencies of the sample and the in-phase component of the lock-in amplifier can be recorded. A listing of the control program is included in Appendix D.

The sample rod is placed on the apparatus in the same manner as in the dynamic moduli determination at room temperature. The temperature of the rod is monitored by a thermistor (HP0837-0164) which is compatible to the HP3456A Digital Voltmeter. The voltmeter is set up to read the thermistor temperature in degrees Celsius (°C) with a resolution of 0.001°C.

The procedure of this measurement is to identify the modes of the bar at room temperature first, as discussed previously, and then select a given mode for automatic tracking with temperature. This is done by tuning the voltage controlled oscillator (VCO) manually to resonance with the integrator shorted and the error signal feedback path open so that there is no error signal presented to the voltage control (feedback) point. The phase shifter is then adjusted so that there is zero output from the quadrature signal channel of the lock-in amplifier. The integrator can then be opened and the control loop completed. If the resonance "runs away", the signal (either transmitter or receiver) needs to be inverted. This

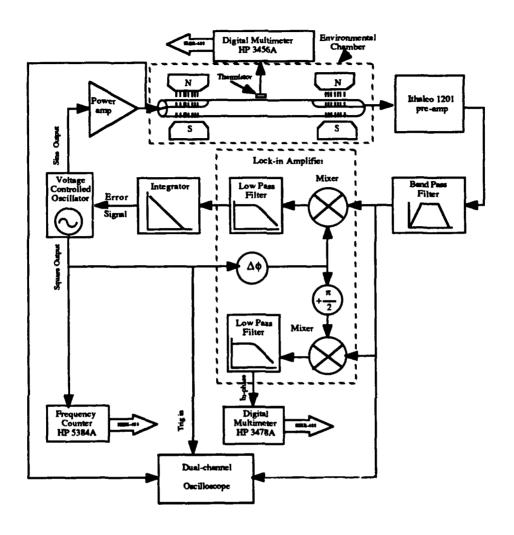


Figure 9. Block diagram of the instrumentation used to track the dynamic moduli dependence on temperature and frequency.

is most easily accomplished by shifting the phase an additional  $\pm$  180° if a lock-in analyser is being used as the mixer/phase shifter/low pass filter. It may also be necessary to adjust the filter time constant and amplifier gain if the signal oscillates. Once the control loop is locked and stable, the temperature may varied. [Ref.3]

After setting up the PLL, the environmental chamber is programmed to run a temperature profile as shown in Figure 10. The long time interval is used to achieve a quasi-equilibrium state, so the material sample is in equilibrium with the uniform temperature environment.

The nature of the experimental set up calls for automation. Thus, in their material selection study [Ref. 6], Beaton has written a BASIC program using the HP9000 series 200 computer Model 236C to acquire inputs of temperature and frequency data. The program is modified to include the input from the in-phase component of the lock-in amplifier and to extend the duration of the measurement from 40 minutes to 20 hours.

To facilitate the graphical presentation of data, the data are converted from the HP data format to Macintosh Cricket Graph<sup>™</sup> format. Using a software package called MacTerm for Macintosh II and software written by Professor Steven R. Baker of NPS (Appendix E) for HP9000 series computer, the data recorded in HP BDAT file are transported from the HP9000 computer via a RS 232C port to the Macintosh II computer.

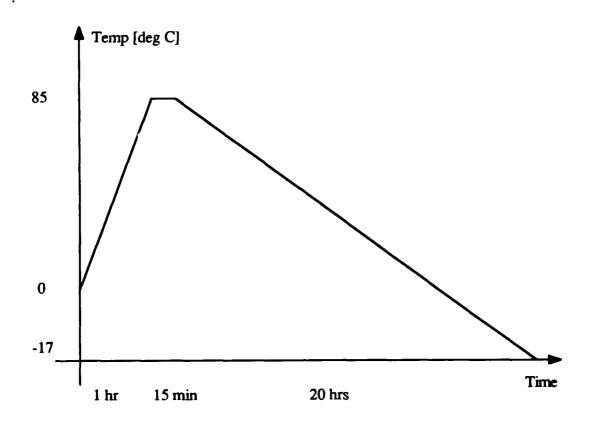


Figure 10. Typical temperature profile for the dynamic moduli measurement

# IV. SYSTEM VERIFICATION

# A. INTRODUCTION

To investigate the complex moduli of a material using the resonant bar technique, it is essential to quantify the losses due to the suspension system. As mentioned earlier, the computations of the moduli are based on a free-free boundary condition. This assumption is valid when the suspension has a negligible effect on the response of the rod.

#### **B. INITIAL INVESTIGATION**

An existing sample rod of E-CAST® F82/215 that was used in a previous experiment involving fiber-optics (see Appendix A) was initially chosen to investigate the losses due to the suspension system. The quality factor, Q, which is a measure of the energy stored to the energy lost per acoustic cycle (Chapter II, equation (23)) was measured, for various support positions (Figure 11) and two types of suspensions: rubber bands and fishing line. As the suspension positions one and three illustrated in Figure 11 correspond to the nodal position of mode two and three respectively, it is expected that the losses are lower than the non-nodal placement positions.

The experimental set up is shown in Figure 8, Chapter III. The HP3562A Dynamic Signal Analyzer is used to generate a swept sine signal which is used as the reference input (channel 1) for the HP3562A. This signal is amplified by HP467A power amplifier and then applied to the driver coil. The electrical signal is converted to a mechanical driving force through the magnetic field and the transducer coil electrodynamic interaction. The response of the material sample is then converted to an electrical signal through the reciprocal electrodynamic transduction mechanism. The received signal is amplified and filtered by an Ithaco 1201 pre-amplifier and input to the second channel of HP3562A.

Plotting the ratio of these two inputs as a function of frequency, the frequency response of the sample material can be obtained directly using the HP3562A. Typical frequency response curve is shown in Figure 5(b). Using the built-in curve fit function of the HP3562A, the quality factor and resonant frequency of each resonant mode can be determined from the pole-zero table generated by HP3562A (see Appendix A).

From Table 1(a), it can be seen that quality factor of mode one and mode two is almost identical, but mode three and mode four differ from these two modes by approximately 5% and 10% respectively. Using the grand average as the reference, only mode four deviates by about 10%. It is noted that, suspension position three produces the highest quality factor in the third mode as expected, but suspension position one produces the lowest quality factor in the second mode instead of the highest which is not the expected result.

From Table 1(b), response of mode three and four is equal within 5%. The quality factor of mode one is the lowest and for mode two it is the highest. Except for mode one, the other modes are less than 18% different from the grand average. Suspension position three has the highest quality factor within the third mode as expected and it is significantly higher than the average quality factor within the mode. Suspension position one does not produce the highest quality factor in second mode as it is expected, although it is the second highest among the quality factors obtained in the same mode.

The experiment was repeated and the similar observations were made. Thus, within the experimental uncertainty, we may conclude that the suspension loss contribution is small and it will be substantial only if a very high quality factor material is under investigation.

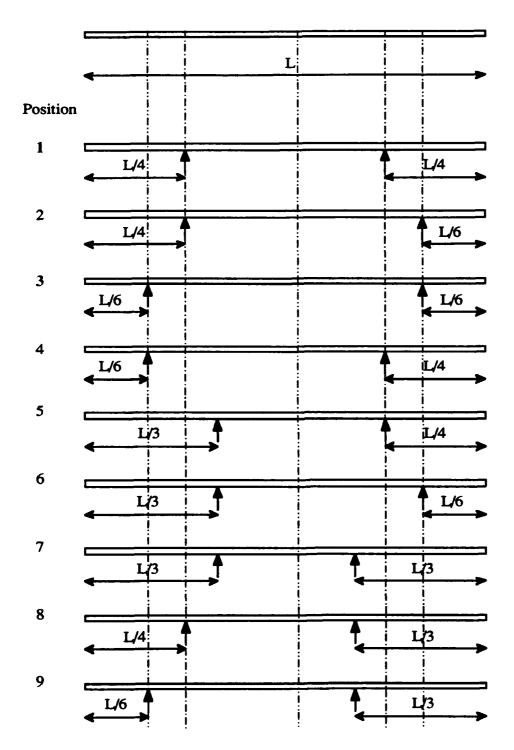


Figure 11. Support positions used in suspension loss measurements and indicate the nodal positions of second and third mode respectively

TABLE 1. QUALITY FACTOR OF E-CAST® F82/215 OBTAINED FROM DIFFERENT SUSPENSION POSITIONS IN TORSIONAL VIBRATION

# (a) RUBBER BAND SUSPENSION

Position	1st Mode	2nd Mode	3rd Mode	4in de
1	22.20	21.79	21.01	19.83
2	22.83	22.29	21.48	19.92
3	23.09	22.51	21.76	19.71
4	22.12	23.02	21.41	19.42
5	22.89	22.47	21.20	20.37
6	22.01	22.19	21.24	20.67
7	21.94	22.32	21.18	20.45
8	22.49	22.40	21.17	20.44
9	22.68	22.28	21.27	20.48
Average	$22.4 \pm 0.4$	$22.4 \pm 0.3$	21.3 ± 0.2	20.1 ± 0.4

Grand average: 22 ± 1

TABLE 1. QUALITY FACTOR OF E-CAST® F82/215 OBTAINED FROM DIFFERENT SUSPENSION POSITIONS IN TORSIONAL VIBRATION

# (b) FISHING LINE SUSPENSION

Position	1st Mode	2nd Mode	3rd Mode	4th Mode
1	15.47	22.97	20.89	19.20
2	12.57	22.84	20.77	19.21
3	10.55	22.73	21.59	19.45
4	10.31	23.12	21.46	18.88
5	14.71	22.38	20.43	19.31
6	12.95	22.30	20.12	20.10
7	17.78	21.51	19.77	20.10
8	14.72	21.92	19.09	19.79
9	12.05	22.04	20.60	19.61
Average	13 ± 2	22.4 ± 0.5	$20.5 \pm 0.8$	$19.5 \pm 0.4$

Grand average: 19 ± 4

# C. SUSPENSION LOSS DETERMINATION USING AN ALUMINIUM SAMPLE

The total losses of a forced vibration system in the resonant bar technique is the sum of the intrinsic losses due to the sample's material properties, suspension losses due to the suspension system of the apparatus and radiation losses. Radiation loss is considered to be negligible and therefore, to be able to measure the intrinsic loss of a sample material, an upper bound must be placed on the suspension losses.

For a high Q material, the resonant peak is very sharp and its -3 dB bandwidth is very small. If the Q of the material is of the order of 1000, then the required sweep time, oscillator stability, and sample temperature stability become a problem both with instrumentation and the patience of the experimentalist. Therefore, we can not simply replace the E-CAST® F82/215 by the 6061T6 aluminium rod and repeat the swept sine frequency response measurements using the HP3562A and expect to obtain accurate curve fit parameters (poles and zeroes) for the quality factor.

The half-power point measurement of Q also depends on the frequency resolution and is not suitable due to the temperature stability of the resonance frequency. Another approach that "exploits" the high Q characteristics of the system was used. As the reciprocal of frequency is time, one can use a time measurement technique that has a long time record, and thus an equivalent high frequency resolution to measure the Q of a low loss material. Free decay measurements is one of such techniques that involves the measurement of successive attenuated amplitudes, from which the damping and hence the quality factor can be obtained. Since a long time record means large amount of data can be generated, regressional analysis can be performed to minimize any random errors due to decaying amplitude variation in the determination of the exponential decay time,  $\tau$ .

A block diagram of instrumentation for the free decay measurement is shown in Figure 12. The sample is driven at one of the resonant frequencies and the tone burst excitation is abruptly removed. This is achieved by means of the trigger pulse switch which disconnects the driving signal to the transducer coil and at the same time provides a trigger pulse to the external trigger input of the Nicolet digital storage scope which records the response of the material sample. Using a digital storage scope and linear regression analysis, the quality factor of the sample can be determined. A typical graph of the measurement is shown in Figure 13. The results are summarized in Table 2 where the uncertainties in Q result from the uncertainty of the slope as determined by the least square method. Based on the average of multiple measurements, the systematic error is larger than the random error when the quality factors are this large and the losses are correspondingly small. From these results, it can be seen that the difference of the quality factors between the "brst" and "worst" support positions varies from 24% to 43% for the first three modes.

It can therefore be concluded that for a low loss (high Q) system, the suspension loss makes a significant contribution to the total losses of the suspension system/sample combination as currently configured. Using the worst case analysis, the suspension loss is about 43% for a system with a Q of about 1300. For a high loss (low Q) system, such as the F82/215 sample, that has a Q of about 20 (and most viscoelastic materials with Q's typically less than ten, see Chapter V, Table 5), the suspension loss contributes less than 1% to the total losses of the entire system.

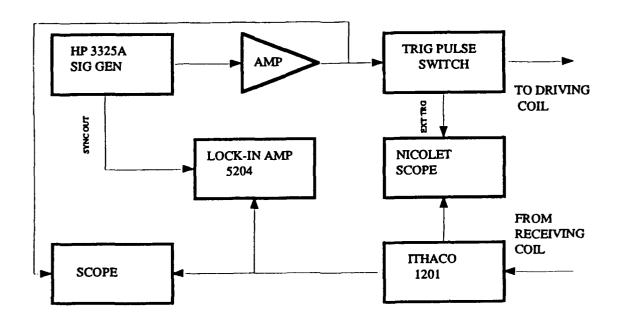


Figure 12. Block diagram of the free decay measurement of aluminium rod

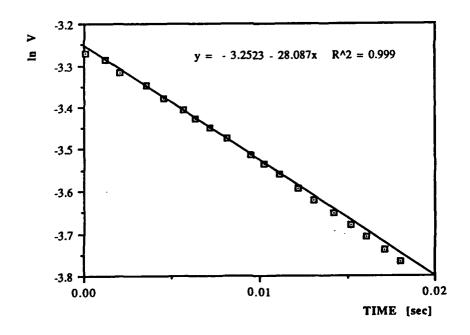


Figure 13. Free decay measurement of Q

TABLE 2. QUALITY FACTOR OF 6061T6 ALUMINIUM ROD OBTAINED FROM TWO DIFFERENT SUSPENSION POSITIONS USING FREE DECAY METHOD.

	1st Mode	2nd Mode	3rd Mode
Best	1306 ± 0.8%	868.7 ± 0.6%	1222 ± 1.4%
support	1338 ± 0.4%	$830.5 \pm 0.9\%$	$1437 \pm 0.8\%$
			1792 ± 1.3%
Average ± σ	1320 ± 16	850 ± 20	1500 ± 300
Worst	751 ± 0.4%	644.9 ± 0.4%	968 ± 5%
Support		$653.5 \pm 0.5\%$	940 ± 3%
			934 ± 4%
Average ± σ	751	650 ± 5	950 ± 18
Relative difference	43 %	24 %	36 %

#### V. DATA

#### A. INTRODUCTION

This study consists of three main areas. The first is the verification of the resonant bar technique to determine the elastic properties of a sample material called E-CAST® F82/215. The second portion involved quantifying the suspension losses using E-CAST® F82/215 and 6061T6 aluminium bar sample. The results of the suspension losses were reported in Chapter IV. The third section is the investigation into the temperature and frequency dependence of the elastomeric materials: Uralite 3130, PR1592 and plexiglass or polymethyl methacrylate (PMMA). Uralite was chosen because of its use in fiber-optic hydrophones [Ref.17], PR1592 because of an accessible NRL-USRD report [Ref.16], and PMMA because of its wide use as a "standard" material in viscoelastic investigation.

#### **B. PRELIMINARY INVESTIGATIONS**

To gain experience with the resonant bar technique, some preliminary measurements were made on E-CAST® F82/215 to determine its dynamic moduli at room temperature. The result, which is summarized in Table 3, where  $\rho$  is the mass density, G is the shear modulus, and E is the Young's modulus, agreed with those obtained in Reference 6 which used a similarly constructed resonant bar apparatus.

TABLE 3. DYNAMIC MODULI OF E-CAST® F82/215

	ρ	G	E	σ
	[kg/m <sup>3</sup> ]	[GPa]	[GPa]	
Ref. 5	1120	0.91±0.06	2.5±0.2	0.37
Present study	1120±20	0.96±0.06	2.70±0.05	0.40

A fiber optic interferometer was constructed by embeding a fiber which comprised of one of the legs of a Michelson interferometer, into a E-CAST® F82/215 rod. In this study, the interferometric output is used as second means to determine the resonant frequency of the rod. It is being investigated for smart skin applications to monitor the state of strain of struts. The results were reported in the proceedings of the SPIE Conference "Fiber Optic Smart Structures and Skins III" in San Jose, September 1990. That paper is included as Appendix A.

# C. TEMPERATURE AND FREQUENCY DEPENDENCE OF VISCOELASTIC MATERIALS

#### 1. Test Matrix

In this study, Uralite 3130, PR1592 rods cast in Teflon® tubing and PMMA rods were used. The torsional mode is the easiest mode to excite and detect, and thus most of the data collected were on the shear modulus. For the PR1592, data was also collected for the flexural resonant mode which depends on the Young's modulus. The test matrix is as follows

TABLE 4. TEST MATRIX FOR VISCOELASTICITY MEASUREMENTS

	PR1592	PMMA	U3130
Torsional	<b>✓</b>	<b>✓</b>	<b>/</b>
Flexural	<b>/</b>	_	_
Quality Factor	<b>✓</b>	<b>✓</b>	

# 2. Data Presentation for PR1592, PMMA and U3130

The resonant bar technique produced data with the two variables, frequency and temperature, coupled together. That is, neither was held constant through a measurement

run. This was dis ussed in Chapter II. The temperature-frequency dependence measurement of the first four torsional modes of PR1592 have been investigated in this study. Graphs produced from the data are shown in Figure 14 and Figure 15. Note that the points were taken at arbitrary time intervals, in this case, every five minutes. The resonance is tracked continuously, thus the discrete data points which are presented could have been obtained with different data density. It can be seen from Figure 14 that as frequency increases, the shear modulus increases in a quadratic manner. As the higher order mode is examined, the slope of the response curve reduces at each frequency. In Figure 15, the higher modes have a higher value of shear modulus at a constant temperature. Further, it can be observed that at the highest temperature, the shear modulus of all the four modes approaches a constant value asymptotically as expected in a single relaxation time constant system discussed in Chapter II. The temperatures were not large enough to obtain the high temperature asymptotic behavior.

The experimental data was then plotted in three dimensional space to visualize the relationships between shear modulus, temperature, and frequency. To compute the loss tangent, the quality factor, Q, of specimen was measured as a function of temperature. In order to present the data in the conventional format, Capps' [Ref. 16: p. 210] and Ferry's [Ref. 10: p.316] results were used to determine the temperature-frequency shift factor  $a_T$  necessary to obtain the master curve.

#### a. Three Dimensional Plots

The effects of temperature and frequency on the behavior of a viscoelastic material can be most easily visualized in a three dimensional plot. The following sections will discuss the various data obtained to construct the three dimensional plots.

(1) Shear Modulus. The three dimensional plots are shown in Figure 16, Figure 17 and Figure 18 for PR1592, PMMA and Uralite 3130 respectively. In Figure 16, all the data from the lowest four torsional modes of PR1592 are presented.

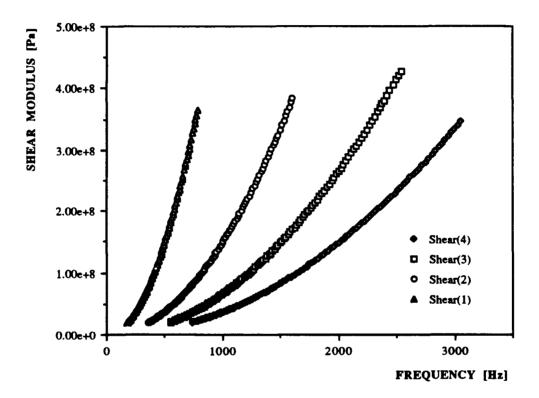


Figure 14. Shear modulus of PR1592 plotted against resonance frequency (temperature is not constant). The numeric indicates the mode number.

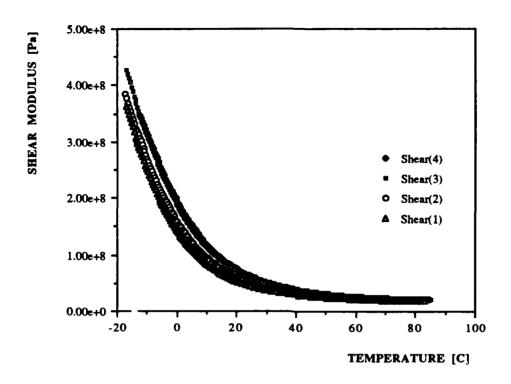


Figure 15. Shear modulus of PR1592 plotted against temperature.

It can be seen that all these are smooth, continuous curves. As temperature increases, the resonant frequency decreases and the shear modulus decreases correspondingly. Both Uralite 3130 and PR1592 are "rubbery" materials at room temperature. The curvature of the projection of their three dimensional modulus graphs in the frequency-temperature plane is opposite to that of the PMMA which is in the "glassy" state at the temperature of this study. When the higher resonant mode is used, the resonant frequency increases and the span of frequency also increases, however, the amplitude of the in-phase output of the lock-in amplifier decreases. Lastly, it can be seen that, the shear modulus is not a simple function of temperature and frequency.

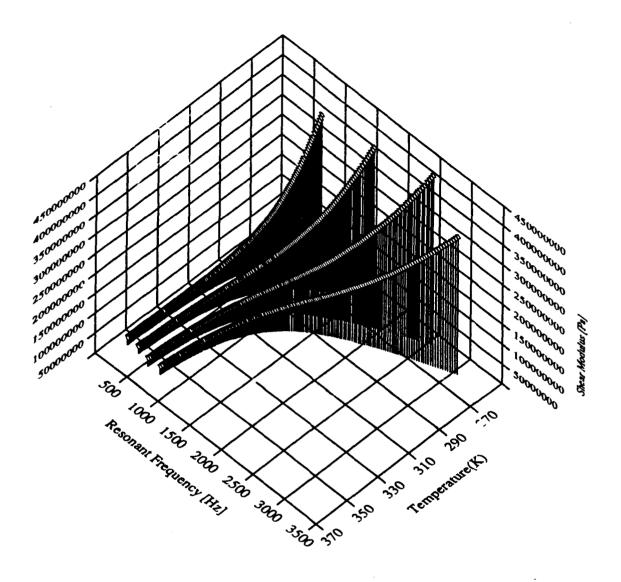


Figure 16. Shear modulus of PR1592 as a function of frequency and temperature.

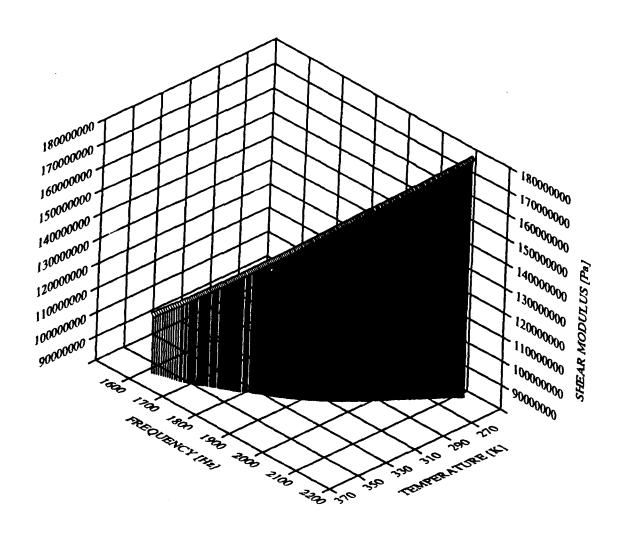


Figure 17. Shear modulus of PMMA as a function of frequency and temperature.

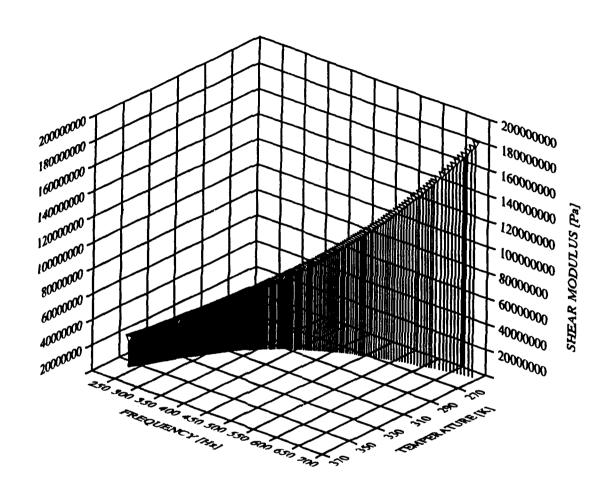


Figure 18. Shear modulus of U3130 as a function of frequency and temperature.

(2) Loss Tangent. The three dimensional plots of the loss tangent of PR1592 and PMMA are shown in Figure 19 and Figure 20 respectively. For PR1592, the presence of glass-rubber transition is evident. The graph of loss tangent has a maximum. There is no local maximum in the loss tangent plot of PMMA for the range of frequencies and temperatures tested.

From Chapter II equation (28), it is shown that the ratio of quality factor, Q, to product of vibrational speed of the end of the bar and resonance frequency, fu, is a constant. Since the in-phase output,  $V_{in}$ , of the lock-in amplifier is proportional to this speed, equation (28) can be rewritten as

$$\frac{Q}{V_{in}f} = b \tag{30}$$

where b is a constant of proportionality. Noting that,

$$\tan \delta = \frac{1}{Q},\tag{31}$$

and combining equations (30) and (31), the loss tangent can be expressed as

$$\tan \delta = \frac{1}{bV_{in}f}.$$
 (32)

By measuring the quality factor, Q, and in-phase voltage at a set of temperatures and frequencies, the loss tangent empirical constant b can be obtained at the start of a test and then the loss tangent of the sample material can be determined continuously. One set of results used to obtain a value for the constant b is shown in Table 5. For this example, the constant has a value of 64 milliseconds per volt (msec/volt). The standard deviation of the 13 measurements is 8 msec/volt so the uncertainty is 2.3 msec/volt or about  $\pm 4\%$ . The reader should be cautioned that this constant is a function of

the position of the coils and the gain of the pre-amplifier and lock-in amplifier. Thus, it must be determined for each sample and instrument setting used.

(3) Young's Modulus. The plot of Young's modulus of PR1592 is shown in Figure 21. It was obtained using the flexural mode of the sample material.

#### b. Master Curves

The conventional way to present viscoelastic behavior is to use the master curve. The master curves are produced from reduced frequency for the shear modulus or loss tangent. The reduced frequency is calculated from data of Capps [Ref. 16: p. 210] and Ferry [Ref. 10: p.316].

The general form of the temperature-frequency shift factor,  $a_{T_i}$  based on the WLF equation [Ref. 10: chap.11], for a great variety of polymers can be expressed as

$$\log a_T = \frac{-8.86 (T - T_s)}{101.6 + T - T_s},$$
(33)

where T is the absolute temperature in degrees Kelvin K, and  $T_s$ , is the reference temperature in K. The equation is applicable at temperature about 50° C above the glass transition temperature. However, as discussed in Ferry [Ref. 10: chap.11], it is better to determine specific values of the two constants in this equation for each sample. Therefore, to explore this particular area, constants from the measurements of Capps for PR1592 and Ferry for PMMA were used. Their expressions are as follows

$$\log a_T = \frac{-12.9 (T - 283.15)}{107 + T - 283.15},$$
(34)

for PR1592 and

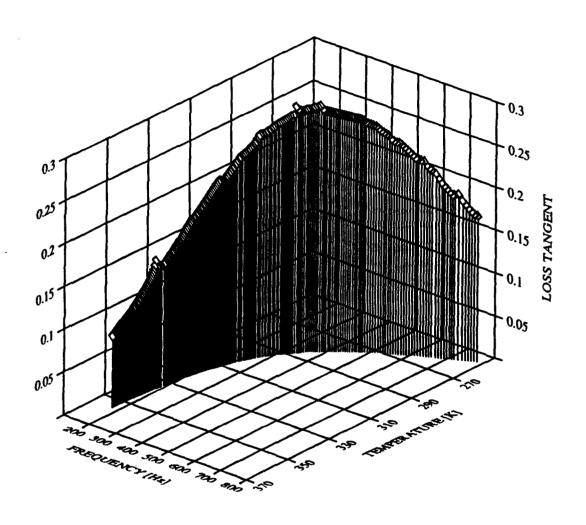


Figure 19. Loss tangent of PR1592 as a function of frequency and temperature.

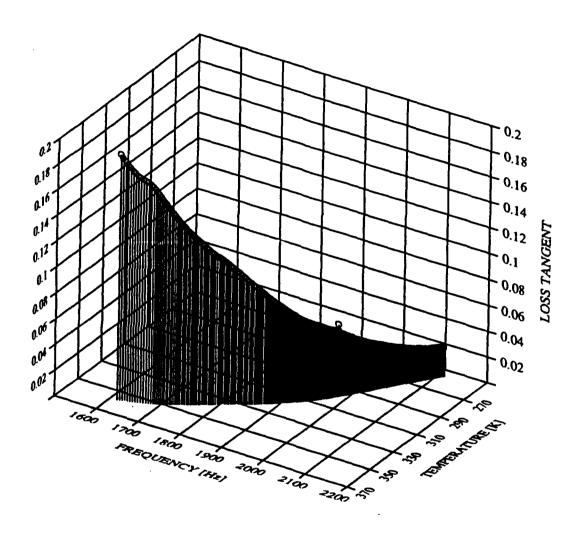


Figure 20. Loss tangent of PMMA as a function of frequency and temperature.

TABLE 5. DETERMINATION OF THE LOSS TANGENT EMPIRICAL CONSTANT " b ".

Т	f	V in	Q	Q/fV in
Temperature	Frequency	In-phase voltage	Quality factor	
[C]	[Hz]	[DCV]		[msec/V]
-17.138	801.9	-0.1125	5.523	-61.22
-10.124	678.4	-0.1048	3.825	-53.80
-0.224	515.2	-0.1140	4.378	-74.53
0.085	511.5	-0.1147	2.913	-49.65
9.321	398.7	-0.1372	2.927	-53.51
19.430	306.5	-0.1842	3.415	-60.49
29.480	259.4	-0.2452	3.847	-60.48
39.342	231.6	-0.3142	5.082	-69.84
49.096	217.1	-0.4092	6.304	-70.97
58.929	201.7	-0.5401	7.805	-71.66
69.546	195.0	-0.7048	9.701	-70.58
79.561	190.0	-0.9350	12.41	-69.86
84.277	188.1	-1.0700	13.60	-67.58

Average:  $-64 \pm 8$  msec/V

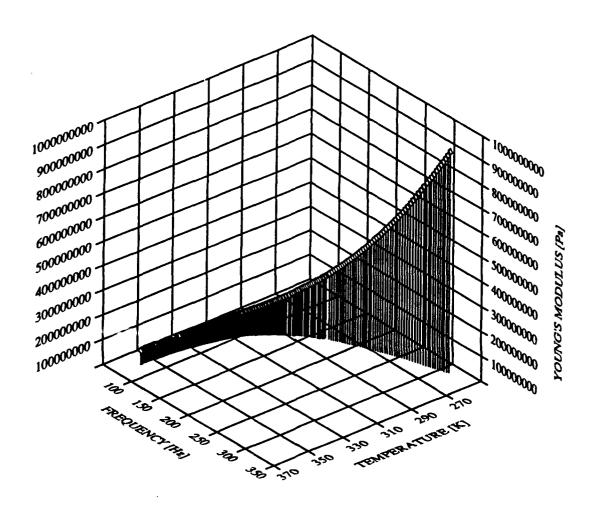


Figure 21. Young's modulus of PR1592 as a function of frequency and temperature.

$$\log a_T = \frac{-21.5 (T - 211)}{43.1 + T - 211},\tag{35}$$

for PMMA. The parameter,  $a_{T}$ , was not independently determined in our study since we did not have sufficient time to use samples of different length. Samples with different lengths would allow moduli at the same temperature but with different frequencies, which were sufficiently well separated to determine the temperature-frequency shift factor with adequate precision.

(1) Shear Modulus and Loss Tangent. The plots of the master curve for the shear modulus of PR1592 and PMMA are shown in Figure 22 and Figure 23 respectively. It should be noted that, for a one order-of-magnitude change of frequency and a temperature range of 100° C (approximately 30% change in absolute temperature), there is a ten-order-of magnitude change of the corresponding reduced frequency. This is rather extraordinary, and it demonstrates the strong dependence of the dynamic modulus of viscoelastic materials on temperature.

From Figure 22, it can be clearly seen that there is a transition from rubbery plateau to glassy zone for PR1592. This is evident from the maximum in the loss tangent curve which is a characteristic of a glass-rubber transition region. By inspection, for PR1592, the transition has occured at a reduced frequency of about 100 Hz, assuming a reference temperature of 10°C.

However, looking at the data obtained from the PMMA (plexiglass) sample, only the glassy zone and part of the glass-rubber transition region are observed. This is also evident in the loss tangent curve in which the loss tangent increases monotonically as the reduced frequency decreases.

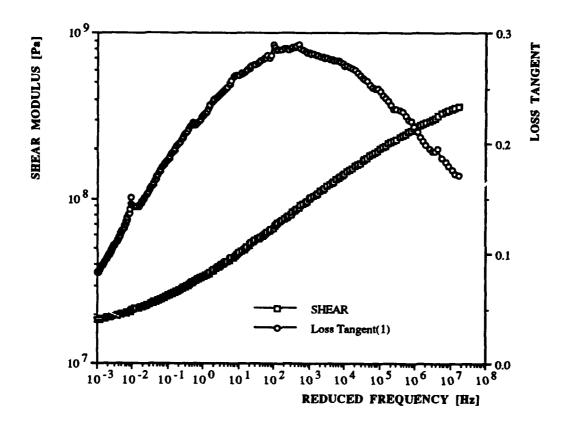


Figure 22. Master curve of PR1592 based on the measurement of the first torsional mode.

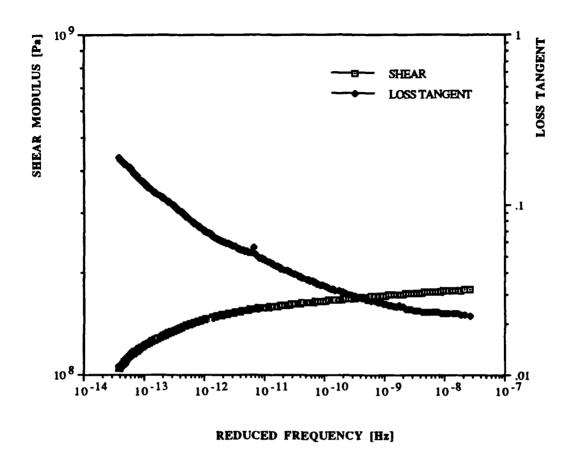


Figure 23. Master curve of PMMA based on the measurement of the first torsional mode.

TABLE 6. COEFFICIENTS OF CURVE FIT FOR PR1592 TORSIONAL MODE

Coefficient	1st mode	2nd mode	3rd mode	4th mode
<b>a</b> 0	7.5324	7.5210	7.5607	7.5529
al	0.13067	0.13592	0.13998	0.13972
a2	1.0742e-2	1.1154e-2	1.1289e-2	1.1633e-2
<b>a</b> 3	-1.162e-3	-1.159e-3	-1.949e-3	-1.757e-3
a4	-1.679e-5	2.309e-5	5.790e-5	1.876e-5
Correlation Coefficient	1.000	1.000	1.000	1.000

TABLE 7. COEFFICIENTS OF CURVE FIT FOR LOSS TANGENT (TORSIONAL MODE)

	PR1592		PMNIA
Coefficient	1st Mode	2nd Mode	1st Mode
<b>a</b> 0	-0.63667	-0.60388	9.0104
al	7.2174e-2	7.8122e-2	4.2034
a2	-1.8544e-2	-2.1478e-2	0.61220
a3	1.6625e-3	1.3403e-3	3.9509e-2
<b>a4</b>	-1.1907e-4	-4.5023e-5	9.8409e-4
Correlation	0.998	0.998	0.999
Coefficient			

The master curves for PR1592 are fitted to a fourth order polynomial function given in equations (36) and (37) and the coefficients for the shear modulus is tabulated in Table 6. The coefficients of the loss tangent of PR1592 and PMMA are given in Table 7.

$$Log G = \sum_{n} a_{n} (Log f)^{n}, n = 1,2,3,4.$$
 (36)

$$Log (tan \delta) = \sum_{n} a_{n} (Log f)^{n}, n = 1,2,3,4.$$
 (37)

By inspection of Figure 22, we see that the location of the inflection point in shear modulus occurs at approximately the maximum of the loss tangent as would be expected for a simple relaxation model discussed in Chapter II. Differentiation of the fourth order polynomial fits to the shear modulus and loss tangent yields an inflection point at  $log \ a_T f = 2.85$  for shear modulus and a maximum at  $log \ a_T f = 2.65$  for loss tangent. This is considered to be in excellent agreement for the span of  $log \ a_T f$  which is from -3 to 7, over ten order-of-magnitude.

(2) Young's Modulus. As for the shear modulus, the master curve for Young's modulus uses the same fourth order polynomial curve fit. The result is shown in Table 8.

TABLE 8. COEFFICIENTS OF CURVE FIT FOR PR1592 FLEXURAL MODE - YOUNG'S MODULUS

Coefficient	1st mode	Capps' result
<b>a</b> 0	8.0219	7.71248
al	0.12331	0.12531
a2	9.985e-3	2.1141e-2
<b>a</b> 3	-8.876e-4	-1.8216e-3
a4	-4.271e-5	-2.1893e-5
Correlation Coefficient	1.000	-

These results are plotted in Figure 24 in which Capps' curve was overlaid on the regression curve obtained from the flexural experiment. We may conclude that the deviation between the two curves is greater than the experimental uncertainty of the data. Therefore, no definite conclusion can be made from this comparison as there are too many possible reasons for the deviation. The samples are not be identical in every aspect, namely, in preparation and curing and hence the assumption that  $a_T$  is the same in our sample may not be true. It might be advised to obtain a sample previously tested by a more conventional method such as Capps' [Ref. 16] and collect data using the technique outlined in this study.

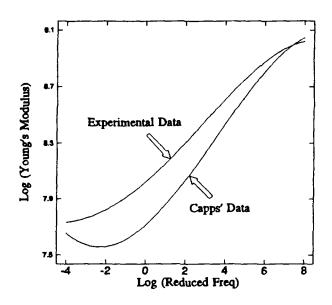


Figure 24. Comparison of experimental data with data from Capps.

### VI. CONCLUSIONS AND RECOMMENDATIONS

The purpose of the research reported in this thesis was the extension of the free-free resonant bar technique described by Garrett [Ref. 3], which measured the shear and Young's moduli of elastic materials, to include the measurement of complex moduli of viscoelastic materials, particularly those materials which are important in the fabrication of hydrophones.

#### A. LOSS MODULUS MEASUREMENT TECHNIQUE

Since much of the utility of the free-free resonant method is due to its simplicity, both in the acquisition and analysis of the data based on measurement of the frequencies of the resonance modes of the sample, a simple extension of the method was devised for determining the loss tangent. This was accomplished by using the in-phase output of the phase sensitive detector to determine loss while the quadrature (out-of-phase) component was integrated and feed back to a voltage controlled oscillator to maintain the system at resonance. The validity of the relation used to convert in-phase output voltage to loss tangent (or its inverse, the resonance quality factor, Q) was verified by obtaining pole-zero curve fits to the entire resonance response curves as a means of independently determining the loss tangent. The experiment dependent (but temperature independent) conversion factor was found to be constant to within a few percent for the samples which were investigated.

Due to the interest in the measurement of loss modulus of polymeric samples, the contribution to the loss due to the sample suspension system, e.g., rubber bands, were quantified by measuring the change in quality factor as a function of position of the sample suspension points. This was done with a low quality factor ( $\approx$ 20) elastomeric sample

using a pole-zero curve fit and with a high quality factor (≈1000) metallic sample using a free oscillation decay time measurement. Both techniques unambiguously established that the suspension losses were minimized when the sample was suspended at vibration nodes and that the maximum effect on the measured loss modulus due to the suspension system losses for elastomeric samples with quality factors less than 20 was less than 1%. For samples with intrinsic quality factors of order 1000, the suspension losses could in the worst case be as large as 40% as the support system is currently configured.

# **B. MODULI OF VISCOELASTIC SAMPLES**

The technique was used successfully to measure the elastic moduli (both shear and Young's) and loss tangent for three elastomeric samples (Uralite 3130, PR1592, and PMMA) over a temperature range of -17°C to +85°C. The measured data for PR1592 and PMMA were converted to master curves using the frequency-temperature shift factors for those materials from the published literature. Over that temperature range, the PR1592 sample exhibited a complete viscoelastic transition with a peak in the loss tangent and an inflection point in the shear modulus which were observed at the same value of reduced frequency to within experimental error as would be expected from a simple viscoelastic model.

The absolute value of the Young's modulus for PR1592 differed from the master curve for that substance measured by NRL-USRD by an amount which exceed experimental error. The cause of this discrepancy has not yet been determined. One possible reason is that the samples were not of identical composition (molecular weight, cure time, etc.). We hope that this discrepancy can be resolved in the future by an exchange of samples between NPS and NRL-USRD.

# C. ADVANTAGES OF THE FREE-FREE RESONANT TECHNIQUE

One conventional technique for making the measurement of storage and loss moduli involves the longitudinal excitation of a rod-shaped sample at one end by an electrodynamic shaker table and the detection of the rod response at the other end by a piezoelectric accelerometer. The complex transfer function thus obtained is used to derive the Young's modulus of the sample. This is accomplished by solving a complex transcendental equation which results from the fact that the mass of the accelerometer is a non-negligible fraction of the sample mass and the fact that the data obtained is, in general, at frequencies below resonance. The conventional technique also only obtains the Young's modulus. A different set-up, sample, and transducers are required to measure the shear modulus.

The free-free resonant bar technique is far simpler and all of the advantages discussed by Garrett [Ref.3] for this technique when used in the measurement of the shear modulus also apply to the measurement of the loss modulus. These include (1) the simplicity of the conversion of resonance frequency to modulus since the mass loading due to the transducers is small; (2) the fact that the transducers, consisting only of magnet wire, are so inexpensive that they can be left on the sample; and most importantly, (3) the ability to selectively and strongly excite all three modes of the bar (longitudinal, torsional, and flexural) and detect them with a high value of signal-to-noise using the same transducer. This ability to measure all three modes means that (4) both the Young's and shear moduli are available from the same apparatus and (5) there are two modes which yield values for Young's modulus so there is an intrinsic self-consistency check. The use of a phase sensitive detection scheme allows (6) the resonance to be tracked automatically and continuously by using the quadrature signal in a feed back circuit to maintain the bar at resonance as the temperature of the sample is varied. This thesis established that the inphase signal can also be used to (7) automatically and continuously track the loss tangent as a function of temperature.

# D. DISADVANTAGE OF THE FREE-FREE RESONANT TECHNIQUE

At the present time there seems to be only one significant disadvantage to this modulus measurement method in comparison with the conventional transfer function method described by Capps [Ref. 16]. This problem arises when one attempts to determine the temperature-frequency shift factor that is required to present the modulus data in the master curve format. In its present implementation, the free-free resonant technique described in this thesis provides modulus data at resonance frequencies which necessarily change with changing temperature. The determination of the shift factor is simplified if the modulus is obtained at fixed frequencies and a variety of temperatures.

In principle, the free-free resonant technique can provide the modulus at several frequencies for each temperature since more than one resonant mode can be observed (four modes were tracked for torsional vibrations of PR1592) but at this time we have not been successful in developing an algorithm which can extract the shift parameter from these multiple modes. One could, of course, obtain a variety of frequencies at all temperatures by using samples of different length but this would increase the measurement complexity by requiring more than one sample.

#### E. RECOMMENDATION FOR FURTHER STUDY

Based on the conclusions reported in this chapter, the two most interesting and important follow-on research problems would have to be (1) the derivation of an algorithm for the extraction of the frequency-temperature shift factor for the modulus measured by the temperature dependance of the fundamental resonance and its next few overtones and (2) a "round robin" calibration of "standard" samples using both the free-free resonant technique and the conventional transfer function technique.

APPENDIX A. CONFERENCE PAPER PRESENTED IN SPIE CONFERENCE "FIBER OPTIC SMART STRUCTURES AND SKIN III" IN SAN JOSE, SEPTEMBER 1990.

# Nondestructive Dynamic Complex Moduli Measurements Using a Michelson Fiber Interferometer and a Resonant Bar Technique

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#### **ABSTRACT**

An optical fiber, used as a leg of a Michelson interferometer, is cast into a long cylindrical bar of E-CAST F-82 epoxy<sup>1</sup>. The bar can be selectively excited in any of its lowest flexural, torsional, and longitudinal modes. The interferometer is used to detect the resonant modes of the "free-free" bar and from these modes both the Young's and shear elastic moduli are determined. The complex modulus is determined by measuring the quality factor (Q) for each resonant mode. The measurement technique is entirely nondestructive and yields results of the two independent moduli with the same transducers.

# 1. INTRODUCTION

This article involves the use of fiber-optic sensors in the non destructive resonant determination of elastic moduli of epoxies. A "free-free" bar is selectively excited in its flexural, torsional, and longitudinal vibrational modes using a transducer consisting of coils of magnet wire placed in the magnetic field created by a pair of permanent magnets, the details of which are covered in an article entitled "Resonant Acoustic Determination of Elastic Moduli"<sup>2</sup>. A commercially available apparatus<sup>3</sup> was used to excite the modes of a bar which had embedded in it an optical fiber acting as the sensing leg of an interferometer. The bar is placed on a pair of soft rubber bands so that the ends are free to move. The phase modulations induced in the optical fiber are converted interferometrically into intensity modulations at the coupler location. The output of the interferometer at the photodetector is monitored to accurately determine the resonant frequency (and its overtones) of the particular mode of excitation of the bar. The square of the frequencies of the flexural and longitudinal resonant modes are proportional to the Young's modulus and the square of the frequency of the torsional modes is proportional to the shear modulus. The quality factor, or Q, of the resonant modes is equal to the ratio of the real to imaginary parts of the complex moduli and the inverse of the characteristic loss tangent, tan  $\delta$ . Since the measurement technique is resonant, the signal to noise ratios are typically very high and the modulus that is obtained is a dynamic complex modulus at the frequencies corresponding to the fundamental bar resonance and its overtones. The modes are also determined by a second coil electrodynamically as described in reference 2.

# 2. EXCITATION AND DETECTION

The differential Lorentz,  $d\vec{F}$ , force produced on a segment of wire,  $d\vec{l}$ , carrying a current, I, in a static magnetic field,  $\vec{B}$ , is given by

$$d\vec{F} = I d\vec{l} \times \vec{B}. \tag{1}$$

Longitudinal, torsional, or flexural forces can be generated in order to selectively excite each of the three vibrational modes with the apparatus pictured in Figure 1. The particular mode excited depends on the relative positioning of the wire coils carrying the current, I, and the direction of the magnetic field. Typically the magnetic field direction and strength created by the pair of permanent magnets as well as the current driven through the coil of wire are constant and independent of frequency. When the frequency of the oscillator driving the wire coil is varied the bar is excited in its characteristic resonant modes of vibration. The detection of these modes is typically an easy task and can be accomplished by placing a second wire coil at the opposite end of the bar within a magnetic field created by a second pair of permanent magnets. The output of this coil of wire transducer is an EMF (voltage) which is proportional to the change in magnetic flux linking the coil and is given by

$$V = -\frac{d}{dt} \int_{s} \vec{B} \cdot \vec{n} \, dA \tag{2}$$

For a small segment of wire moving with velocity,  $\vec{u}$  in a magnetic field  $\vec{B}$ , the induced EMF is given by

$$V = \vec{B} \cdot \vec{l} \times \vec{u} \tag{3}$$

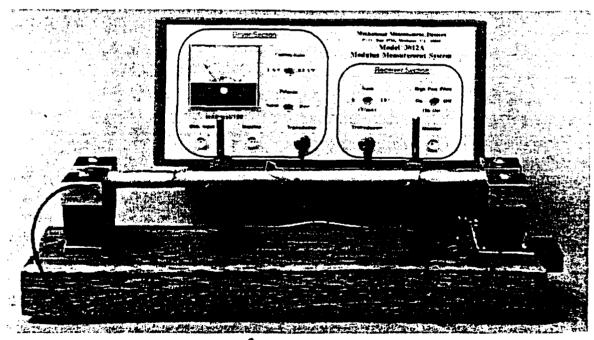


Figure 1. The MMD measurement apparatus<sup>3</sup> used to electrodynamically excite and detect the flexural, longitudinal, and torsional modes of a bar in order to determine the shear and Young's elastic moduli.

The resonant vibrational modes can also be detected interferometrically due to the sinusoidally excited strain induced phase shifts in the leg of the interferometer. The output of a pigtailed single mode laser (Sharp LT010, 818 nm) is delivered to a 2 x 2 fiber optic splitter/coupler where it is divided into two separate legs of a Michelson interferometer. One leg is cast axially a constant radial distance from the center of the rod and the other acting as a reference placed on the lab bench. The interferometer is cleaved at the end of the rod so that the coherent light reflects and combines interferometrically at the coupler which is characteristic of a Michelson interferometer. The resulting characteristic fringe pattern is observed with an oscilloscope from the output of a photodetector as illustrated in the measurement setup in Figure 2.

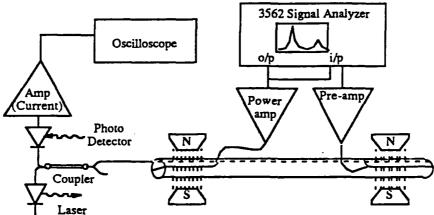


Figure 2. Illustration of the measurement setup for the electrodynamic excitation and both electrodynamic and interferometric detection of the modes of a bar.

# 3. THEORETICAL RESONANCE FREQUENCY

Once the resonances have been determined the appropriate moduli, Young's, E, or shear, G, can be determined from the equations in this section provided that the dimensions and density of the bar can be measured. The resonance frequencies will also depend on the boundary conditions which for this apparatus is "free-free" corresponding to zero stress and zero moment at both ends.

A uniform, cylindrical rod-shaped sample of a homogeneous, isotropic solid having circular cross-sectional diameter, d, and length, L, which is significantly greater than its diameter, will propagate three independent waves if their wavelengths,  $\lambda$ , are much greater than d. The displacements associated with the longitudinal and torsional modes satisfy a partial second-order wave equation, and for a free-free boundary condition, the resonances are harmonically related. The Young's modulus can be expressed in terms of these parameters as

$$E = 4\rho L^2 \left(\frac{rL_n}{n}\right)^2 \tag{4}$$

where n is a positive integer. Similarly, the free-free boundary condition leads to a series of harmonic torsional modes whose frequencies,  $f_n^T$ , are related to the shear modulus by

$$G = 4\rho L^2 \left(\frac{f^T_n}{n}\right)^2. \tag{5}$$

The measurement of the flexural mode is not necessary but it does provide a second estimate for the Young's modulus and its fundamental frequency is typically an order-of-magnitude lower than the longitudinal modes. The flexural mode is also strongly excited by this electrodynamic transduction scheme so it is easy to observe.

Unlike the torsional and longitudinal modes, the flexural waves of the bar obey a fourth-order differential equation and the flexural wave phase speed is dispersive. The application of "free-free" boundary conditions in this case leads to a series of modes which are overtones but not harmonics. The Young's modulus of the rod can be expressed in terms of the flexural modes as

$$E = \frac{1024}{\pi^2} \frac{\rho L^4}{d^2} \left( \frac{f_n^F}{n^2} \right)^2. \tag{6}$$

where n takes on the values 3.0112, 4.9994, 7, 9, 11...

# 4. CONCEPT OF A COMPLEX MODULUS

# 4.1 The Loss Tangent and Quality Factor

Many solids and most metals behave as nearly perfect elastic media and obey Hooke's Law. For the application of a dynamic force to these materials, there is a corresponding deformation that, in the linear limit, is proportional to the magnitude of, and in phase with, the applied stress. The ratio of the applied stress to the resulting normalized deformation or strain is therefore a characteristic property of the material which is termed the elastic modulus. The modulus of these metals may be independent of frequency over a large frequency range. If a material possesses sufficient damping characteristics, (or equivalently low Q's) energy can be dissipated as heat in each cyclic deformation resulting in a strain that is out of phase an angle  $\delta$  with the applied stress. The characteristic elastic modulus can thus be represented as a complex quantity in phasor notation with magnitude G and phasor angle  $\delta$ , or as an in phase, G', and quadrature term, G" as<sup>4,5</sup>

$$G^* = Ge^{j\delta_0} = G' + jG''$$
(7)

where G"/G' =  $\tan \delta_G$  and  $j = \sqrt{-1}$ . The loss tangent is related to the mechanical Q by the relation:

$$\tan \delta_{G} = G''/G' = \frac{1}{Q} \tag{8}$$

To illustrate the concept of the complex modulus further, let us start with the familiar equation of motion for a damped driven oscillator

$$M \frac{\partial^{2} \xi(t)}{\partial^{2} t} + R \frac{\partial \xi(t)}{\partial t} + K \xi(t) = F(t)$$
(9)

where  $\xi$  is the displacement from equilibrium, M is the mass of the oscillator, R is the resistive mechanical damping coefficient, K is the spring constant or characteristic stiffness, and F is the applied force. If the applied force is sinusoidal of frequency  $\omega$ , the above equation is expressed as complex variables in the form

$$-\omega^{2} M \xi^{*} + K \left(1 + j \frac{\omega R}{K}\right) \xi^{*} = F^{*}$$
(10)

where the coefficient of  $\xi$  (the effective stiffness term) can also be expressed as a complex variable<sup>6</sup>

$$K^* = K \left( 1 + j \frac{\omega R}{K} \right) = K \left( 1 + j \tan \delta \right). \tag{11}$$

At a driving frequency coinciding with resonance,  $\omega = \omega_0 = \sqrt{K/M}$ , the tangent of the phase difference  $\delta$  is inversely related to the quality factor, Q by

$$\frac{1}{\tan \delta} = \frac{K}{\omega_0 R} = \frac{\sqrt{K M}}{R} = \frac{\omega_0 M}{R} = Q. \tag{12}$$

The quality factor also has the following common definitions

$$Q = \frac{\omega_0}{\omega_{\rm u} - \omega_{\rm L}} = \frac{1}{2} \omega_0 \tau \tag{13}$$

where  $\omega_{tt}$   $\omega_{tt}$  are the frequencies above and below resonance for which the average power is 3 dB down relative to its value at resonance and  $\tau$  is the decay modulus or characteristic time required for the free decay amplitude to decrease to 1/e of its initial value. The Q is also equal to the ratio of  $2\pi$  times the mechanical energy stored in the oscillator to the energy dissipated per acoustic period.<sup>7</sup>

# 4.2 Quality Factor determination from pole-zero plots

The Q, and thus complex modulus, can also be found from a pole zero plot of the mechanical admittance of the oscillator as will be illustrated in this section by measuring the frequency response of the output, eqn. (3), (induced EMF) of the detection transducer (which is proportional to velocity) to the input force, eqn. (1), (which is typically constant).

Again considering the damped driven harmonic oscillator of frequency  $\omega$ , and noting that the complex velocity and displacement are related by  $u^* = j\omega \xi^*$ , the complex admittance  $u^*/F^*$  (which is equal to the inverse of the complex impedance) is given by

$$Y^{*}(j\omega) = \frac{j\omega}{M\left(j\omega\right)^{2} + \frac{R}{M}(j\omega) + \frac{K}{M}}$$
(14)

The complex mechanical admittance is directly analogous to the the complex electrical admittance of an RLC circuit<sup>8</sup> with the familiar electrical quantities voltage, current, electrical resistance, inductance, and capacitance (V, I, R, L, C) corresponding to the mechanical quantities force, velocity, mechanical resistance, mass, and compliance or inverse stiffness (F, u, R, M, 1/K) respectively. Letting  $j\omega = s$ , we can factor the admittance in pole-zero format as follows

$$Y^{*}(s) = \frac{s}{M \left[s^{2} + \frac{R}{M}s + \frac{K}{M}\right]} = \frac{1}{M} \left[\frac{s}{(s-\gamma)(s-\gamma^{*})}\right]$$
(15)

where  $\gamma, \gamma^*$  are complex conjugates. Noting  $\omega_0 = \sqrt{K/M}$ , the characteristic roots are

$$\gamma = \frac{-R}{2M} + j \sqrt{\omega_0^2 - \left(\frac{R}{2M}\right)^2} \quad \text{and} \quad \gamma = \frac{-R}{2M} - j \sqrt{\omega_0^2 - \left(\frac{R}{2M}\right)^2}. \tag{16}$$

Thus the transfer admittance function has poles at  $\gamma$  and  $\gamma^*$  and a single zero at  $\omega = 0$ . Note that in this derivation we are only considering oscillatory solutions which correspond to R/(2M)  $< \omega_{\sigma}$  The pole zero plot is illustrated in Figure 3 and the poles are located on a circle of radius  $\omega_0$ .

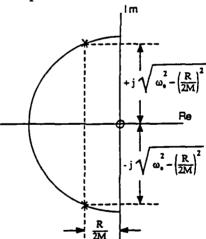


Figure 3. Pole zero plot of complex admittance function.

If we express the location of the poles as  $\gamma = a + jb$  and  $\gamma^* = a - jb$ , then Q can be expressed as follows

$$Q = \frac{\sqrt{b^2 + a^2}}{-2a} \tag{17}$$

and the resonance frequency is equal to

$$\omega_0 = \sqrt{b^2 + a^2} \cong b \left( 1 + \frac{1}{2} \frac{a^2}{b^2} \right) = b$$
 (18)

where the first approximation is from the binomial expansion theorem and the second approximation is valid for low to moderate damping.

# 6. MEASUREMENTS AND RESULTS

A single optical fiber is used as the leg of a Michelson interferometer, and was cast into a long bar of E-CAST F-28 (1.24 cm diameter, 30.36 cm length, and density of 1120 Kg/m³) at an off axis distances of approximately 6.0 mm. As the rod is sinusoidally driven with either longitudinal, transverse, or torsional stresses, strains will be produced in the leg of the interferometer which result in phase shifts relative to the unattached unstrained reference leg of the interferometer.

The flexural, torsional, and longitudinal modes were clearly described from the transducer coil output and interferometric phase modulated output. The first three torsional resonances occurred at 1485, 3075, and 4684 Hz. The first two flexural resonances occurred at 182.3 and 514.7 Hz. The first three longitudinal resonances occurred at 2535, 5243, and 7712 Hz. These resonances were measured at an average room temperature of 24 °C. A typical interferometric output and electromagnetic coil output pair for the flexural fundamental resonance mode is illustrated in Figure 4. From eqn. (4-8), the complex shear and Young's modulus corresponding to these resonances are tabulated in Table 1 for the bar.

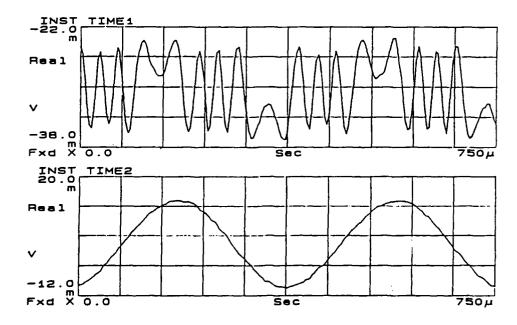


Figure 4. Typical interferometric output (Top) and corresponding transducer coil output (Bottom) at resonance for the fundamental flexural mode of the E-CAST bar.

Mo	ode# [n]	Frequency [f <sub>n</sub> ] (Hz)	Freq/Mode # $[f_n/n]$ (Hz)	Quality factor [Q]	Loss factor [δ] (%)	Modulus (Pa)
	Torsional 1 2 3	1485 3075 4684 Average	1485 1538 <u>1561</u> 1528	20.1 19.8 19.1 19.7	4.97 5.05 <u>5.24</u> 5.09	(shear modulus G*) 0.935 x 10 <sup>9</sup> (1 + j .0509)
	Flexural (3.0112) <sup>2</sup> (4.9994) <sup>2</sup>	182.3 514.7 Average	20.11 20.59 20.35	30.0 30.4 30.2	3.33 3.29 3.31	(Young's modulus Y*) 2.66 x 10 <sup>9</sup> (1 + j .0331)
	Longitudin 1 2 3 Average	al 2535 5243 7712	2535 2622 <u>2571</u> 2576	21.6	4.63 <del>4.63</del>	(Young's modulus Y*) 2.74 x 10 <sup>9</sup> (1 + j .0463)

Table 1. Summary of the frequencies of the modes of vibration of the sample bar described in the text.

After using the HP3562 (dynamic signal spectrum analyzer) to sweep through the appropriate frequency range in order to excite each mode of vibration as illustrated in the measurement setup diagram in Figure 2, the resonances were determined from the displayed frequency response and verified by manually adjusting the oscillator for greater resolution. The quality factor, or Q's, for each mode were obtained by measuring the upper and lower 1/e (or -3dB) points on each side of resonance by adjusting the local oscillator. The Q's listed in Table 1 were obtained from this method.

Since the HP3562 also possesses pole-zero curve fitting features, the resonances and quality factors were determined from the HP3562 generated curve fit parameters according to eqns. (17) and (18) derived earlier. It should be noted that the poles and zeros from the HP3562 generated plot are in Hertz and not in radians as suggested in eqns. (17) and (18). The frequency response of the detection wire coil transducer to the input drive for the torsional mode of vibration, the corresponding HP3562 curve fit response, and the list of poles and zeros are illustrated in Figure 5. The first four torsional resonances, which are harmonically related, are clearly identifiable. The frequency response of the flexural mode of vibration, the corresponding HP3562 curve fit response, and corresponding table of poles and zeros are illustrated in Figure 6. The corresponding resonance frequencies and quality factors determined from these poles and zeros are tabulated in Table 2. Due to temperature changes in the room, the measured resonance frequencies do differ for different measurements and thus more accurate temperature control by means of an environmental chamber is needed for measurement-to-measurement repeatability.

Having obtained the two independent moduli, the set of elastic constants for the isotropic material can be determined, i.e. the Poisson's ratio, v, is found to be 0.444 from<sup>4</sup>, v = [E/(2G)] - 1, and using the average value for the Young's modulus of  $E = 2.7 \times 10^9$  Pa and the shear modulus of  $G = 0.935 \times 10^9$  Pa.

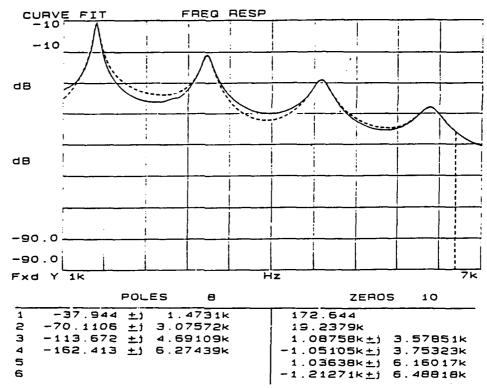


Figure 5. Frequency response of the transducer coil output for the torsional modes of the bar. The dotted line is a generated HP3562 frequency response with corresponding curve fit parameters (poles and zeros) listed below.

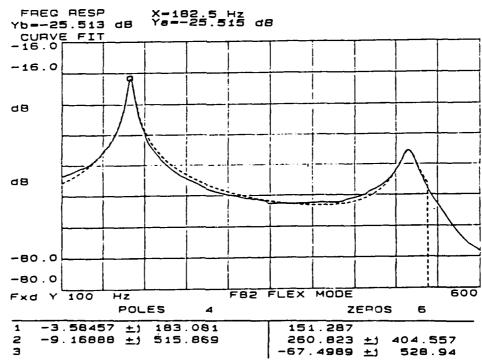


Figure 6. Frequency response of the transducer coil output for first two flexural modes of the epoxy bar. The dotted line is a the HP3562 curve ft frequency response with corresponding curve fit parameters (poles and zeros) listed below.

Mode # [n]	Frequency [f <sub>n</sub> ] (Hz)	Freq/Mode # [f <sub>n</sub> /n] (Hz)	Quality factor [Q]
Torsional			
1	1474	1474	19.42
2 3 4.	3077 4692 6276 Average	1539 1564 <u>1569</u> 1536	21.94 20.64 <u>19.32</u> 20.34
Flexural			
(3.0112) <sup>2</sup> (4.9994) <sup>2</sup>	183.1 516.0 Average	20.11 20.59 20.35	35.54 <u>38.14</u> 36.86

Table 2. Resonance frequencies and Q's determined from the pole zero plots in Figures 5 and 6 and the eqns. (17) and (18).

# 6. CONCLUSIONS

A resonant method for determining the complex Young's and shear modulus of elasticity has been presented that uses coils of wire to excite and detect vibrational modes of a bar. For detection, an optical interferometer, whose leg is cast in the material under investigation, can also be used to accurately detect the three resonant modes via strain induced phase modulations.

# 7. ACKNOWLEDGEMENTS

This work was supported by the Naval Postgraduate School Direct Funded Research Program.

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# APPENDIX B. MATERIAL SPECIFICATION SHEETS

- 1. **URALITE 3130**
- 2. PR1592



# URALITE® 3130

URETHANE CASTING ELASTOMER

80-85 Shore A 25-30 Shore D

# TECHNICAL DATA BULLETIN

- No moisture sensitivity
  - Excellent hydrolytic stability (Reversion Resistance)
    - No TDI, no 4,4' -Methylene-bis-(2-chloroaniline)
      - Fast cure, quick demolding
        - High abrasion resistance
          - Low Viscosity
            - Good Electrical Properties
              - Good Adhesion to many substrates

#### DESCRIPTION

Uralité 3130 is a two component, natural amber or black urethane casting elastomer. This tough room temperature mixing and curing system has excellent handling characteristics. Uralite 3130 is a middle of the hardness range, general purpose, versatile Uralite elastomer. It does not exhibit typical moisture sensitive characteristics of most urethane elastomers.

#### USES:

- Electrical and Electronic Encapsulating
- Molds and Mold Facings
- Metal forming pads
- Flexible snakes
- Gaskets
- Abrasion resistant parts

#### PROPERTIES:

Test Method	<u>Value</u>	(Metrics)
ASTM D 2240-68 ASTM D 2393-71 ASTM D 2393-71 ASTM D 2393-71 ASTM D 412-68 ASTM D 412-68 ASTM D 624 Die C	80-85/25-3 3400 120 2000 2750 250	(193) (45)
ASTM D 149-64 ASTM D 150-54T	240 5.6 7.2	
ASTM D 257-70 ASTM D 257-70	1 x 10 <sup>13</sup> 2 x 10 <sup>13</sup>	
	ASTM D 2240-68 ASTM D 2393-71 ASTM D 2393-71 ASTM D 2393-71 ASTM D 412-68 ASTM D 412-68 ASTM D 624 Die C  ASTM D 149-64 ASTM D 150-54T  ASTM D 257-70	ASTM D 2240-68 ASTM D 2393-71 ASTM D 412-68 ASTM D 412-68 ASTM D 412-68 ASTM D 624 Die C  ASTM D 149-64 ASTM D 150-54T  5.6 7.2  ASTM D 257-70  1 x 10 <sup>13</sup>

(over)

#### **URALITE® 3130 TECHNICAL DATA BULLETIN**

PRO	PERTIES: (Continued)	Test Method	Value	(Metrics)
	Insulation Resistance — @77°F (25°C) oh	ms		
	after 28 days @ 95°F (35°C) 95% RH	WE ATS612	1 x 10 <sup>11</sup>	
	Pot Life - min. @ 77°F (25°C)	ASTM D 2471-71	.14	
	Shrinkage - in/in (mm/mm)	ASTM D 2566-69	0.0016	
	Density	ASTM D 792-66		
	Cured Compound Ibs/in3 (g/cm3)		0.039	(1.07)
	Part A lbs./gal. (g/cm³)		8.58	(1.03)
	Part B lbs./gal. (g/cm <sup>3</sup> )		9.15	(1.10)
	Demolding Time - hrs @ 77°F (25°C)		4	
	Demolding Time — hrs @ 175°F (79°C)		1	
	Complete Cure – days @ 77° F (25°C)		2 - 4	
	Complete Cure - hrs. @ 175°F (79°C)		2 - 3	
	Color		Amber or Black	
	Ratio (By Weight):			
	Part A		100	
	Part B		30	
	Ratio (By Volume):			
	Part A		100	
	Part B		28	

These physical properties are representative of typical values obtained by tests conducted in the Chemical Products Division laboratory.

#### STORAGE:

Uralite 3130 should be stored in a cool dry area. Avoid temperatures above 90°F and below 65°F. Always blanket Uralite 3130 with dry nitorgen or 8440 Inert Blanketing Gas and reseal container after use.

#### SURFACE PREPARATION SUGGESTIONS:

Porous materials, such as plaster and wood, must have all surfaces that come in contact with Uralite 3130 well-sealed with a sealer which is compatible with urethane (acrylic sealers are suggested). After sufficient drying time, approximately thirty (30) minutes after last coat, the final surface preparation consists of the application of a release agent such as Partingkote® 8302 (wiping off excess) to accomplish a complete and uniform release coating.

#### MIXING:

Ratio: Parts by Weight	Part A - 100	Ratio: Parts by Volume Part A - 100
	Part B - 30	Part B - 28

Weigh both components into same container and stir slowly for 2-4 minutes, scraping the sides and bottom of container periodically to include unmixed material which may adhere to these surfaces. Care must be taken to avoid whipping air into mixture. Pour the thoroughly mixed Uralite 3130 onto the prepared surface and allow to cure. Working pot life of Uralite 3130 is approximately 14 minutes.

#### URALITE® 3130 TECHNICAL DATA BULLETIN - SHEET #2

#### CURING:

Near ultimate physical properties are normally attained after 2 days at room temperature (77°F). Curing of Uralite 3130 may be accelerated by heating for 1-2 hours at 175°F. Demolding can be accomplished after 4 hours at room temperature.

#### **PACKAGING:**

UNIT DESIGNATION	PART A	PART B	UNIT NET WEIGHT
12 Qt. Pack (pre-weighed)	12-One Qt. Cans	12-1/2 Pint Cans	22 lbs. 13.12 ozs.
Pail Pack	5 Gal. Pail	2½ Gal. Can	52 lbs.
Drum Pack	55 Gal. Drum	30 Gal. Drum	585 lbs.

#### CAUTION:

#### FOR INDUSTRIAL USE ONLY.

This product contains an isocyanate based prepolymer, amines and heavy metal catalysts which are harmful if swallowed. It does not contain toluene diisocyanate or 4,4' methylene bis-(2-chloroaniline). It may cause burns or skin irritation. Use only in a well ventilated area. Protect skin and eyes from contact and avoid inhalation of vapors.

Should skin contact occur, wash with soap and water. For eye contact, flush with water immediately and obtain medical attention. If swallowed, drink water, induce vomiting and contact a physician immediately.

WARRANTY. The following is made in fleu of all warranties, express or implied: Seller's only obligation shall be to replace such quantity of this product which has proven to not substantially comply with the data presented in the Manufacturer's latest bulletin describing the product. In the event of the discovery of a non-conforming product, Seller shall not be liable for any property loss or damage, direct or consequential, arising out of the use of or the inability to use the product. Before using user shall determine the suitability of the product for his intended use, and user assumes all risks and liability whatsoever in connection therewith. Statements relating to possible use of our product are not guarantees that such use is free of patent infringement or its approved by any government agency. The foregoing may not be changed except by an agreement signed by an officer of seller.

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Printed in U.S.A.



# AEROSPACE/ELECTRONIC PRODUCTS

# PR-1592

# POTTING AND MOLDING COMPOUND

#### Use

Especially formulated as a high hardness molding compound for electrical cables and/or as a potting compound for electrical connectors where resistance to cold flow, fexibility, high tensile strength, and exposure from -70°F to 275°F for extended periods are required.

# Description

PR-1592 is a noncracking, chemically curing, polyurethane compound which is supplied in Amber or Black and in two-part quantities or premixed and frozen in plastic cartridges. PR-1592 cures at 180°F to a tough, flexible, cold flow-resistant, high tensile strength rubber with a Shore A hardness of 85. PR-1592 will cure at 75°F, but the resultant physical properties will be lower than when heat cured. Properly cured PR-1592 is designed to withstand temperatures as high as 275°F for extended periods without blowing, deterioration or loss in electrical properties, and has excellent flexibility at -70°F.

The viscosity of PR-1592 allows the material to be degassed easily when supplied in two part units and provides for excellent flow of characteristics in encapsulating, molding and potting applications.

PR-1592 must be used with a primer on metal, neoprene and polyvinyl chloride surfaces.

# **Specifications**

material, molds, etc. to reach the temperature.

Part B

PR-1592 meets the requirements of MIL-M-24041C Category B

Straw

Application Properties (Typical)		(Cured 16 hours at 180°F)		
Color		Color	Dark Amber or Black	
Part A	Dark Amber or Black	Specific Gravity	1.08	

Mixing Ratio
Part A:Part B
53:100 by weight
Volume Shrinkage
Volume Shrinkage
4%
Nonvolatile Content
99%
Tensile Strength
6000 psi
Viscosity (Brookfield Spindle #3 @ 10 rpm)
Ultimate Elongation
425%

Viscosity (Brookfield Spindle #3 @ 10 rpm)

Two-part unit

Premixed, frozen

Viscosity (Brookfield Spindle #3 @ 10 rpm)

Ultimate Elongation

425%

Tear Strength (Die C)

320 lbs./in. ±

100% Modulus

600 psi

Application Life
Two-part unit
Time to 2500 poises 2 hrs. @ 75°F

Compression Set (ASTM D 395, Method B)
22 hrs. @ 158°F

40%

Premixed, frozen

Ozone Resistance

Conforms

Time to 2500 poises 1 hr. @ 75°F

(Tested in accordance with MSFC-SPEC 202B)

Mold Release Time 2 hrs. @ 180°F Moisture Absorption 2.4%

Cure Time (Tested in accordance with MIL-M-24041)
To 75 Shore A hardness 7 days @ 75°F or Flame Resistance

6 hrs. @ 180°F 12'C Current overload; 55 amps DC
To 85 Shore A hardness 21 days @ 75°F or
(Ultimate cure) 16 hrs. @ 180°F 21'C through #16 wire No ignition

NOTE: The above times are at the temperature indicated.
Therefore, it is necessary to allow time for the mass of

(Continued on Page 2)

Self-extinguishing

SUPERSEDES

MARCH 1987

DATE ISSUED

SEPTEMBER 1987

PRODUCTS RESEARCH & CHEMICAL CORPORATION

01-T-0:0

PR-1592

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PR-1592

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PR-1592

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01-T-0:0

PR-1592

PRODUCTS RESEARCH & CHEMICAL CORPORATION

PR-1592

GLOUCESTER CITY, NEW JERSEY 08030

AREA CODE (818) 240-2060

AREA CODE (609) 456-5700

#### Performance Properties (Continued from Page 1)

Hydrolytic Stability, Hardness Change		
After 120 days @ .		
158°F, 95% RH	~ 15%	
Adhesion, Peel Stength		
Aluminum		
(Primed with PR-420)	40 piw	
Neoprene	•	
(Primed with PR-1523-M)	25 piw	
PVC (MEK tackified)	28 piw	
Fungus Resistance	Non-nutrient	

# Electrical Properties (Typical) (Cured 16 hrs. @ 180°F)

•		
Arc Resistance	150 seco	nds
Dielectric Strength	300 volts	/mil
Dielectric Constant		•
At 1 KHz @ 75°F	6.5	
At 1 MHz @ 75°F	4.6	
Power Factor		
At 1 KHz @ 75°F	0.08	
At 1 MHz @ 75°F	0.06	
Insulation Resistance		
At 75°F	5 x 10 <sup>5</sup> n	negohms
At 250°F	150 meg	ohms
Resistivity	At 75°F	At 250°F
Volume, ohm-cm	1 x 1012	4 x 109
Surface, ohms	1 x 1013	8 x 1010

NOTE: The above application, performance and electrical property values are typical for the material, but are not intended for use in specifications or for acceptance inspection criteria because of variations in testing methods, conditions and configurations.

# **Purchasing Data**

#### PRODUCT DESIGNATION

(Tested in accordance with MIL-E-5272A)

When ordering this product, designate PR-1592 and color as follows: PR-1592 Amber or PR-1592 Black. NOTE: Refer to "Surface Preparation" for primer requirement.

#### STANDARD PACKAGING

#### Two-Part Units

Designation	Part A Container	Part B Container	Units per Case
40 fl. oz. unit	1-pt. can	1-qt. can	9
160 fl. oz. unit	1/2-gal, can	1-gal, can	4

NOTE: The unit designates the total fluid ounce content of Part A and Part B (128 fluid ounces per gallon). Standard units are furnished with a premeasured quantity of Part A and Part B, individually packaged.

## Frozen Cartridges

Designation	Approximate Contents	No. Cartridges per Case
21/2 oz. cartridge	2¼ fl. oz.	72
6 oz. cartridge	5¾ fl. oz.	36
12 oz. cartridge	111/2 fl. oz.	36

#### PRIMER DESIGNATION

When ordering primer, designate PR-420, PR-1523-M or PR-1543 as required under "Surface Preparation."

#### STANDARD PACKAGING

PR-420 is packaged as follows:

	Part B	Total	No. per
Designation	Container	Contents	Case
# 7 kit	1/₂-pt. can	7 fl. oz.	16
#14 kit	1-pt. can	14 fl. oz.	16

NOTE: the kit number designates the total fluid ounce content of Part A and Part B. Kits are furnished with a premeasured quantity of Part A and Part B individually packaged. The kits are designed so that adequate space is available in the Part B container for addition of Part A and mixing.

PR-1523-M and PR-1543 are packaged ready to use

in the following containers: No. per Designation Contents Case 2 fl. oz. 2 fl. oz. bottle 2 fl. oz. 6 1/2 pint 1/2-pint bottle 8 fl. oz. , 12 One pint 1-pint bottle 16 fl. oz. 12

# **Surface Preparation**

#### **CLEANING**

Connectors or other metal surfaces must be free of grease, oil and wax in order to insure good adhesion. Use oil-free solvent applied with a small brush or oil-free cloths for cleaning (reclaimed solvents should not be used). Premixed cleaners are commercially available. Do not expose wire insulation and inserts to the cleaning solvent beyond the time necessary for adequate cleaning.

#### APPLICATION OF PRIMER

For maximum adhesive strength between PR-1592 and the material to which it is to be bonded, the following surface preparations are required:

NOTE: Do not dip priming brush into primer supply. To maintain an uncontaminated primer supply, pour a small portion of primer into a clean container from which it should be used. Reseal primer supply immediately after portion has been removed.

#### (a) Metal

Metal must be primed with PR-420. Thoroughly mix 1 part of Part A with 6 parts of Part B by volume. Do not mix more than can be used within a 4 hour period. Brush a thin film of mixed PR-420 on all inside surfaces of connectors and on wire, but not on the insulation. Let primer dry for 1 hour at 75°F. If primer becomes contaminated, reclean primed surface lightly with methyl ethyl ketone and dry. Stripping the primer from the connector and repriming is not necessary.

#### (b) Neoprene

To obtain good adhesion to neoprene insulation, the surface should be abraded with a suitable abrasive to remove grease, oil, wax or mold release. Remove rubber particles with a dry oil-free brush.

Apply a liberal coat of PR-1523-M to the clean neoprene surface by brush and allow to dry for approximately 30 minutes at room temperature. After 30 minutes drying time, wipe off excess PR-1523-M primer with a clean, gauze pad and start the potting or molding procedure. Drying time of PR-1523-M should not exceed 4 hours at room temperature before potting or molding. If primed surface becomes contaminated or potting or molding is not accomplished within 4 hours after application of PR-1523-M, buff neoprene and repeat priming procedure. NOTE: PR-1523-M is hygroscopic and must be kept free of moistures. Mol PR-1523-M hydrolyzes, a dark grainy precipitate is formed decreasing the primer usefulness. Material containing precipitate should be tested to determine that adhesion is satisfactory before using.

#### (c) Polyvinyl Chloride

To obtain good adhesion to polyvinyl chloride insulation, the surface should be made tacky with methyl ethyl ketone. The use of a primer may be necessary only with some formulations of polyvinyl chloride. Therefore, it is suggested that tests be made to determine the adhesive strength of PR-1592 to the polyvinyl chloride in question.

Should a primer be required, then apply a thin coat of PR-1543 to the tackified surface by brush and allow to dry 30 minutes at room temperature. If primed surfaces become contaminated before potting or molding, buff primed surface with a suitable abrasive and reapply a thin coat of PR-1543.

It should be noted that there are many formulations of polyvinyl chloride. Therefore, it is suggested that before production quantities of PR-1543 are ordered, tests be made to determine the adhesive strength of the PR-1543/PR-1592 system to the polyvinyl chloride in question.

NOTE: PR-1543 is hygroscopic and must be kept free of moisture. When PR-1543 hydrolyzes, a precipitate is formed decreasing the primer usefulness.

#### (d) Tellon\* and Other Fluorocarbons

To obtain good adhesion to insulation made of Tellon and other fluorocarbon resins, it is essential that the insulation be etched or treated to provide a bondable surface. After neutralization of the etchant, in accordance with the manufacturer's instructions, apply PR-1592 directly to the etched surface without primer.

#### REPAIR

To obtain good adhesion to previously cured PR-1592, the surface should be buffed with a suitable abrasive to remove grease, oil, wax or mold release. Remove rubber particles with a dry, oil-free brush.

CAUTION: Do not use solvents for cleaning cured PR-1592. Apply new PR-1592 directly to buffed surface and cure as recommended. No primer is required.

#### Mixing Instructions

#### FOR TWO-PART UNITS

Do not open containers until ready to use.

Part A will solidify at room temperature. Prior to use, loosen lid and warm to 250° ± 10°F with thorough stirring. Do not heat over 260°F. When warming the material, use a thermometer to determine the actual material temperature. Liquefaction is complete when the material becomes smooth and uniform in appearance and loses all signs of graininess. Stirring is essential during liquefaction to provide a uniform material and to hasten melting. Care should be taken to dissolve all solidified Part A around the top of the container. Trace quantities of unliquefied Part A will cause premature solidification. Do not store Part A at temperatures exceeding 100°.

Premeasured quantities may be divided into smaller quantities by using the following proportions: By weight 53 Parts A to 100 Parts B.

NOTE: After removing a portion of Part B from a full container, moisture in the air in the empty portion of the Part B container tends to cause the remaining material to skin over during extended periods of standing. This material may be used by removing the skin.

Where a dense compound free of voids is required, it is recommended that the mixed material be degassed before applications are made. Standard vacuum equipment may be used or, for small usages, the material may be degassed in a standard laboratory desiccator connected to a vacuum pump.

The following degassing procedure is recommended:

- 1. Stabilize Part A and Part B at 75° to 85°F before mixing.
- Place Parts A and B in a clean, dry, metal container having at least twice the volume of the material to be degassed. Mix Part A and Part B thoroughly with a metal mixing paddle. NOTE: DO NOT USE WOOD.
- 3. When Parts A and B are mixed thoroughly, degas the mixture until loaming subsides which is approximately 10 minutes at a pressure of less than 5mm of mercury for a pint of material. Larger quantities will require slightly longer periods of degassing.
- 4. When the material is to be applied by extrusion gun, it is suggested that after tranferring the degassed material into the extrusion gun cartridge the material be degassed at a pressure of less than 5mm of mercury.

<sup>\*</sup>Registered trademark for DuPont tetralluoroethylene resin.

for 2 minutes to remove any air which may have been entrapped during cartridge filling. If extra care is taken when filling cartridges with degassed material, such as flowing the material down the side of the cartridge, the material may not need to be degassed in the cartridge.

NOTE: After mixing Parts A and 8; subsequent operations should be accomplished as quickly as possible to minimize the reduction of application life.

After units of PR-1592 have been mixed and degassed, they may be irozen for storage under refrigeration. Use of a quick-freeze technique is recommended so as to minimize the amount of application life that would be lost in a slower cooling procedure. One successful method is to immerse the filled cartridge in a slurry of dry ice and alcohol for 10 minutes. The temperature of the sealant will drop to approximately – 70°F and the cartridges may be transferred to a refrigeration storage unit maintained at – 20°F or below.

NOTE: Approximately 1 hour application life will be lost in the freezing and thawing process.

It is suggested that tests be conducted to determine whether degassing is necessary for the material to meet particular requirements. When it has been found that degassing is not necessary to meet requirements, mix entire contents of Part A with Part B, or use in the proportions as shown above, and thoroughly mix. Slow mixing by hand or with a mechanical mixer is recommended. A high-speed mechanical mixer will generate internal heat which reduces application life and will whip air into the mixture resulting in a porous material upon curing.

#### THAWING OF FROZEN CARTRIDGES

Frozen cartridges of PR-1592 must be thawed as follows:

NOTE: It is essential that the thawing time and temperature be controlled closely to obtain the maximum application life in the shortest thawing period. An increase in either thawing time or temperature will result in an incomplete thaw.

Remove cartridge from storage and thaw for 30 minutes in a 100° ± 5°F heating block or water bath. If an oven is used to thaw the material instead of the recommended water bath or heating block, the time and temperature will have to be determined because of the variations in oven controls and circulation.

NOTE: If a water bath is used, be sure water does not enter cartridge. The recommended method of preventing water from entering the cartridge is to use a metal sleeve, closed at one end, with a diameter just large enough to allow the cartridge to be inserted to the lip and then place the sleeve upright in the water bath.

CAUTION: When thawing frozen cartridges of PR-1592, keep cartridges in an upright position, nozzle end down with CaPlug in place, to prevent air that may have been drawn into the cartridge during freezing from entering and being trapped in the compound. After thawing is complete, just before placing the cartridge in the gun, insert a thin piece of metal or spatula blade between plunger and cartridge wall to the shoulder of plunger. Then force plunger down to exhaust any air between compound and plunger face and continue until material just starts to extrude between plunger and cartridge wall. Remove metal or spatula while holding plunger down.

# Application Instructions

#### FOR POTTING

Application is accomplished by injecting the sealant into the end bell of the connector which has been coated previously with primer. Separate the wires evenly so that the potting compound will flow around all wires and soldered connections.

For most potting applications, a Semco #440 nozzle with 1/8" diameter has been found most practical. However, nozzles of smaller diameter are available.

When applying PR-1592 with an extrusion gun, the nozzle first should be inserted between the center wires so that the sealant will flow around the contacts. It may be necessary to reposition the nozzle for even coverage. Care should be taken to eliminate voids and air bubbles. It is good practice when filling the connector to keep the tip of the nozzle just above the swell of the material level, moving the nozzle up as the connector fills. The tip of the nozzle should not be held so as to allow it to become submerged nor should it be held so as to allow the material to fold.

In applying PR-1592, every effort should be made to eliminate voids and air bubbles. A small piece of metal, such as a welding rod, should be used to tamp or pack the compound around the wires and the base of the pins. In conjunction with the tamping, the connector should be tapped on a resilient surface or even mechanically vibrated to facilitate the flow of the sealant into the small recesses.

To reduce viscosity and enhance flow of compound, connectors or molds may be heated up to 140°F prior to filling. Do not heat the molding compound, as it will thicken and shorten application life.

Molds may be prepared to the exact shape and form required in a particular connector application by utilizing various plastic materials commercially available. A form or mold may be made for the back of a connector by using masking or polyethylene tape. Reference is made to the handbook, *Installation Practices for Aircraft Electric and Electronic Wiring*, (Navy) NAVAER 01-1A-505 or (USAF) T.O. 1-1A-14 dated 30 June 1975.

#### FOR MOLDING

When PR-1592 is used as a molding compound, molds should be provided for forming the particular form and shape required. To facilitate the removal of PR-1592 from the mold after curing, spread a thin film of mold re-lease compound on mold surface to prevent adhesion. Metal molds may be coated with Tellon tetrafluoroethylene

resin to provide a permanent release film and eliminate the necessity of using a mold release compound.

Inject PR-1592 into the mold, which has been coated previously with mold release and/or on previously \_. prepared surfaces, and allow to firmly set before removing mold. It is recommended that injection holes be located in the bottom of the mold and air bleed holes located in the top of the mold to prevent air pockets in the mold. Flash may be trimmed with a sharp knife or razor blade.

#### Mold Release and Cure

The mold release time for PR-1592 is dependent upon the temperature, quantity of material, mold mass, ect. In molds containing less than 24 fluid ounces of PR-1592, the mold release time is approximately 2 hours at 180°F. In molds containing 24 to 48 fluid ounces of PR-1592, the mold release time is approximately 3 hours at 180°F. Longer times will be required for the mold release of PR-1592 in larger molds.

PR-1592 cures to a tough, resilient material having a 75 Shore A hardness in 6 hours at 180°F. PR-1592 will cure at 75°F, but the physical properties will be lower than when cured at 180°F.

# Cleaning of Equipment

Wash equipment, tools and brushes with methyl ethyl ketone immediately after use or before material cures. Use commercial stripping compounds to remove cured material.

## Safety Precautions

PR-420 contains flammable and volatile solvents. Keep away from heat, sparks and flame. Proper precautions for working with flammable liquids should be followed as well as applicable safety precautions.

# Storage Life

Storage life of PR-1592 in two-part quantities is 12 months when stored at temperatures below 80°F in original unopened containers.

Storage life of premixed, frozen PR-1592 is at least 7 days when stored at -20°F or at least 30 days when stored at -40°F.

Storage life of PR-420 is approximately 1 year when stored in original unopened containers below 80°F.

Storage life of PR-1523-M and PR-1543 is approximately 6 months when stored in original unopened containers below 80°F.

NOTE: PR-1523-M and PR-1543 are hygroscopic and must be kept free of moisture. When these primers hydrolyze, a precipitate is formed decreasing the primers usefulness. Material containing precipitate should be tested to determine that primer is satisfactory before using.

# **Health Precautions**

Part B of PR-1592 and related primers, PR-420, PR-1523-M, and PR-1543, contain isocyanates and can produce irritation or allergic reaction following contact with the skin, eyes or mucous membranes. Avoid all contact with the uncurred components of these materials. In case of contact, promptly wash off with copious quantities of water and follow with a soap and water wash. Avoid breathing vapors. Use with adequate ventilation. Individuals with chronic respiratory problems or prior respiratory reactions to isocyanates should not be exposed to vapors.

PR-420 contains mixed solvents and a lead compound. Use adequate ventilation or air-supplied respirator during application.

In cases of extreme exposure or adverse reactions to any of the products mentioned above, remove affected personnel to fresh air and obtain immediate medical attention. If a rash develops, consult a physician. Ordinary hygienic principles such as washing hands before eating or smoking must be observed. For complete health and safety information, consult a Material Safety Data Sheet.

"PRC" is a trademark of Products Research & Chemical Corporation, registered with the U.S. Patent Office

All recommendations, statements, and technical data contained herein are based on tests we believe to be reliable and correct, but accuracy and completeness of said tests are not guaranteed and are not to be construded as a warranty, either expressed or implied. User shall rely on his own information and tests to determine suitability of the product for the intended use and user assumes all risk and liability resulting from his use of the product. Sellers and manufacturers sole responsibility shall be to replace that portion of the product of this manufacturer which proves to be defective. Neither seller nor manufacturer shall be liable to the buyer or any third person for any injury, loss, or damage directly or indirectly resulting from use of, or inability to use, the product Recommendations or statements other than those contained in a written agreement signed by an officer of the manufacturer shall not be binding upon the manufacturer or seller.

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# APPENDIX C. ENVIRONMENTAL CHAMBER SPECIFICATION SHEETS

# TEMPERATURE/HUMIDITY

#### CH MBERS



#### ASSOCIATED ENVIRONMENTAL SYSTEMS

These are all standard units — readily available — many from stock. Now you can pick the unit to suit your needs and your budget... Bench Top and Floor Models — four temperature ranges to choose from — choice of 6 working volumes — 15 different units in all.

#### **BENCH TOP MODELS—BHD Series**

The BHD-403, 405 or 408 (last two digits indicate cubic foot working volume) are bench top units that will allow testing to meet known Mil. Std. Humidity Specifications. These units are basically Humidity chambers since they have a limited temperature range when compared to the Floor Models. In order to properly control humidity a refrigeration system is required.

Simple and easy to operate. The basic chambers have a digital dry bulb and a direct setting digital % RH controller (see optional extras for automatic programming and recording). Simply connect the power, 1/4" water supply line and 3/8" drain line and you are ready to operate.

Temperature Range: - 18°C (0°F) to + 93°C (+ 200°F)

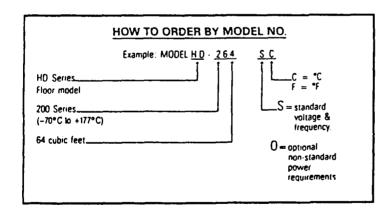
Humidity Range: 20% to 95%  $\pm$ 5% RH within the range of  $\pm$ 20°C (68°f) to  $\pm$ 85°C (185°f) and is limited by a  $\pm$ 4°C (39°f) dew point temperature, using standard controls Optional microprocessor and recorders are available. Lower humidities available with optional chemical difference of the control of th

#### FLOOR MODELS-HD SERIES

This series of Humidity Chambers allows you to custom design a chamber to satisfy your needs and your budget. Four working volumes to choose from 08, 16, 33 and 64 Ft.3—Three Temperature Ranges.

Humidity Range: 20% to 95% RH within the range of +20°C (68°F) to +85°C (185°F) and is limited by a +4°C (39°F) dew point temperature.

With 86651 Programmable controller. Control stability of ±3% RH.



Select the temperature range.

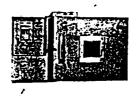
The 400 series has a temperature range of  $-18^{\circ}\text{C to} + 177^{\circ}\text{C (0°F to} + 350°F)$ The 500 series has a temperature range of  $-40^{\circ}\text{C to} + 177^{\circ}\text{C (}-40°\text{F to} + 350°F)$ The 200 series has a temperature range of -70°C to + 177°C (-100°F to +350°F)

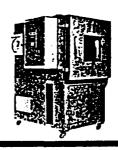
Select the working volume:

Indicate it as the last two digits of the model number - Sizes: 08, 16, 33 or 64 Ft.3.

#### FEATURES (illustrated on page 4)

- FAILSAFE- An adjustable high temperature failsafe
  is standard on all Associated Environmental System
  Chambers it is factory set at the ultimate high temperature capability of the chamber Upon receipt of
  the chamber, the customer should set the dry bulb
  controller to 10° above the highest test temperature
  and adjust the failsafe. This will prevent the test
  chamber from a temperature overrun.
- FUSIBLE LINKS (in the heater circuit) for over temperature protection
- MULTIPANE VIEWING WINDOWS In the door of all chambers (optional on BHD Series)
- INTERNAL LIGHT with external switch standard on all floor models optional on bench top units.
- PILOT LIGHTS to monitor proper function of various systems
- INTERIORS All stainless steel type 304 heliarc
  welded
- EXTERIORS Heavy gauge, cold colled steel with two coats of textured enamel finish
- INSULATION High density, low K factor, non-setting fiberolass.
- VAPOR GENERATORS When humidity is required the controller signals the vapor generator to induce water vapor into the chamber. This method of creating high humidities is superior to the older methods of spraying water or passing warm air over water.
- VAPOR GENERATOR FAILSAFE All A.E.S humidity chambers are equipped with a factory set failsafe control to shut down the vapor generator in the event of a no water situation.
- FREEZE PROTECTION Since all A.E.S. Chambers have the capability of going below the freezing point of water, each humidity chamber has a freeze protector which is factory set at 1.67°C (+.35°F). This control actuates a solenoid valve to drain water from the chamber and prevent damage due to freezing of water.
- FORCED AIR CIRCULATION High volume air circulation is standard on all units to achieve uniformity in the work space. The interior fan is connected to an external motor with a stainless steel shaft.
- WIRING Coded readily accessible. In accordance with NEC
- CONTROLS All located in a hinged access panel with all relays and fuses readily accessible
- ACCESS PORT A 2" diameter access port and plug in left side wall on floor models and right side wall on bench tops is pre-punched in the metal – additional ports and plugs available.
- DIGITAL TEMPERATURE & HUMIDITY CONTROL-LERS





#### BENCH TOP MODELS BHD-403, 405, 408

# FLOOR MODELS HD-400, 500, 200

LINUT CRECICIC ATIONIC

UNII S	FECI	FICATIO			,											
		Temp. Aa	ICH TOP MO Inge: – 18°C Rango: 20%	to - 93°C		Temp. Range: - 18°C to + 177°C Hum. Range: 20% to 95%				FLOOR MODELS Temp Range: - 40°C to + 177°C Hum. Range: 20% to 95%			Temp. Rangs: - 73°C to + 177°C Hum. Rangs: 20% to 95%			
MODEL NO.		BHD-403	8HO-405	BH0-408	HD-400 SERIES			HD-500 SERIES			HD-200 SERIES					
Working	FL2	03	05	08	08	16	33	- 54	08	16	33	64	06	16	33	64
Volume:	Liters	. 85	142	227	227	453	765	1812	106 227	453	765	1812	227	453	765	1812
Power Required:	AVC.	115 , 100	115 , 100	230 200	230 , 200	230 230	230 230	230 230	230 230	230 200	230 200 220	230 200		230,200	230 , 200	
	HZ Amps	60 50 16 16	60 50 16 16	60 50 10 10	60 50 20 24	60 ¦ 50 28   28	50 50 30 30	60 50 32 32	60 50 26 26	50 50 30 30	60 50 30 30	60   50 35   35	60 50 35 30	60 , 50 40 <sub>1</sub> 35	60 50 50 50	60 ; 50 64 ; 34
Shipping	Lbs.	48	528	600	650 750	900	1300	1800	750 850	1000	1400	1900	1050	1200	1725	2375
Weight:	Kg.	182	240	273	295 340	408	590	816	340 386	454	635	862	476	545	184	1080
Window in		Optional	Optional	Optional	6x8	12 x 12	12 x 12	12 = 12	8 . 8	12 x 12	12 x 12	12 x 12	1 : 8	12 x 12	12 x 12	12 x 12
Access Port		2" dia (51 mm) port & plug center right side wall			Z dia. (51 mm) port & plug left side wall											
Nominal Heater	Kw	0.7	0.7	10	25	40	5.0	6.0	2.5	40	50	60	25	40	_50_	60
Refrigeration System:	HP	1/3	1/3	1/2	3/4	,	1	159	199	2	,	5	2 = 2	212	5 x 5	7% 1 7%
Temp. Rise Ambient to Limit in Min	Upper	30	30	40	40	40	60	30	40	40	60	30	40	40	60	30
Temp. Pull ( Time: Ambi Lower Limit	ent 10	45	45	45	60	60	60	60	60	60	60	60	90	60	120	120
Programmable Controller		Optional	Optional	Optional	#86551 PROGRAMMABLE CONTROLLER STANDARD											

<sup>\*</sup>Rise & Pull Down Times may very depending on ambient conditions and power supply

<sup>\* 208</sup> VAC requires additional transformer

	BHD-403	BHD-405	BHD-408	HD-400, 500, 200 SERIES					
Working Volume: Ft,3	<b>0</b> 3	05	08	08	, 16	33	64		
Size: HxWxDIn. HxWxDcm.	16 x 20 x 16 41 x 51 x 41	20 x 22 x 20 51 x 56 x 51	24 x 24 x 24 61 x 61 x 61	24 x 24 x 24 61 x 61 x 61	30 x 30 x 31 76 x 76 x 79	36 x 36 x 45 92 x 92 x 114	48 x 48 x 48 122 x 122 x 122		

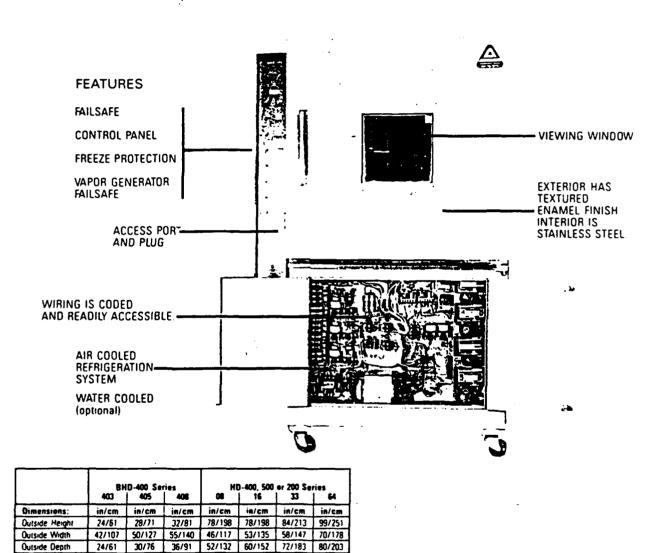
ATSIDE !

32" H x 55" Wile x 36" dopth (cutside dimensions)

#### **OPTIONAL EXTRAS**

- 1. Programmable Controller 86651 (standard on all floor models)
- 2. 86649 IEEE-488 interface ( required #1 option)
- 3. Product Protector limit controls
- 4. Honeywell 2 Pen 12" Circular Chart Recorder
- .5. 8" x 8" Window in Door for BHD-400 models
- 6. Manual Window Wiper
- 7. Internal Light with External Switch (standard on all floor models)
- 8. Water Storage Tank-External
- 9. Water Re-cycling System (includes external storage tank)
- 10. Water Demineralizer System
- 11.1 Extra Demineralizer Cartnoge
- 12. Fully Adjustable Shelves
- 13. Additional Shelves

- 14. Casters
- 15. Additional Ports—Specify Location 44", 2", 3", 4", 5", and 6" diameter
- 16. Chamber Cart (for BHD-403)
- 17. Floor Stand (BHD-405 & 408)
- 18. Liquid CO2 Cooling Capability-specify psi
- 19. Liquid N2 Cooling Capability
- 20. Noise Reduction Package for floor models
- 21. Water Cooled Condenser
- 22. Other Power Source Requirements
- 23. Desiccant Dehumidifier for low % RH requirements (consult factory with specs)



In line with our corporate policy of continuing product improvement and quality control. Associated reserves the right to change product without

# APPENDIX D. RESONANCE TRACKING SYSTEM PROGRAM LISTING

```
RT20C
                          : Resonance Tracking System
10!
20!
      Written by
                          : Brian Beaton
                         : 18 Mar 90
30!
      Date
                          : 21 FEB 91
40!
      Last modified
50!
      Features added
                          : 1.Read one more DVM for Inphmag
                          BDAT change to 40 records
60!
70!
                          Measurement time 20 hours
80!
                          Layout of printer output change
90!
                          Format of data storage change(for Mac)
100!
                          28 Jan 91 by Tan B.H.
110!
                          2.Display In phase mag vs Time on CRT
                          Add plots of Inphmag vs Freq and
120!
                          Inphmag vs Temp
130!
140!
                          13 Feb 91 by Tan B.H.
150!
                          3. Compute reduced frequency
                          Convert old data of RT20B to RT20C format
160!
170!
                          BDAT change to 50 records
180!
                          21 FEB 91
190!
                   ****************
200!****
210! Program initialization
220!***************************
230!
240
        MASS STORAGE IS ":INTERNAL,4,0"
250
        RE-STORE "RT20B:INTERNAL,4,1"
260!
270
        OPTION BASE 0
280
        DIM Thermistor(0:240), Resfreq(0:240), Time(0:240), Inphmag(0:240)
290
        DIM Mod(0:240),X(0:240),Y(0:240),Alphat(0:240),Redfreq(0:240)
        DIM Temp(0:240)
300
        DIM Gtor(0:240), Elong(0:240), Eflex(0:240)
310
320
        DIM Label$(0:25)[50]
330
        DIM Main_title$[50],Sub_title$[50]
        DIM X_axis_name$[50],Y_axis_name$[50]
340
        DIM Block1$[50],Block2$[50],Block3$[50],Block4$[50]
350
        DIM C1$[25],C2$[25],C3$[25],C4a$[25],C4b$[25],C5$[25]
360
370
         DIM C6$[25],C7$[25],C8$[25],C9$[25],C10$[25]
380
        DIM L1$[50],L2$[50],L3$[50],L4$[50]
390!
        Clear$=CHR$(255)&CHR$(75)
                                                  ! CLEAR SCRN key
400
                                                      ! HOME key
410
        Home$=CHR$(255)&CHR$(84)
420!
430
        Flag=0
                             !Flag=1 to indicate editing data
                                     ! first torsional mode
        Tmode=1
440
                                   ! first longitudinal mode
        Lmode=1
450
        Fmode=3.0112
                                       ! first flexural mode
460
470!
480
        Sample_rate=5
                                   ! 1 sample every 5 minutes
                                          ! samples per hour
        Arg1=60/Sample_rate
490
                                        13.14159265
        Pi=PI
500
                                         ! Full, Partial or No
        Default grid$="Partial"
510
```

```
520!
        Label$(1)="Resonance Frequency vs Time"
530
                                                   ! Graph Main Titles,
540
        Label$(2)="Temperature was varied"
                                              ! Sub Titles, Axes names
         Label$(3)="Time, hours"
550
        Label$(4)="Resonance frequency, Hz"
560
570
        Label$(5)="Temperature, C"
580
        Label$(6)="Resonance Frequency vs Temperature"
590
        Label$(7)="Temperature vs Time"
600
        Label$(8)="Frequency variation was observed"
610
         Label$(9)="Young's Modulus vs Temperature"
620
        Label$(10)="Shear Modulus vs Temperature"
630
         Label(11)="Shear modulus, Pa, x10^n"
640
         Label$(12)="Young's modulus, Pa, x10^"
650
         Label$(13)="In Phase Magnitude, DCV"
660
         Label$(14)="In Phase Mag vs Time"
670
        Label$(15)="In Phase Mag vs Temp"
680
         Label$(16)="In Phase Mag vs Freq"
690!
                                 ! White
700
        Pen1=1
                                           Default colors
710
        Pen2=2
                                 ! Red
720
        Pen3=3
                                 ! Yellow
730
         Pen4=4
                                 ! Green
                                ! Cyan
                                           (greenish blue)
740
        Pen5=5
750
        Pen6=5
                                 ! Blue
760!
770!*
780 Options: ! Allow user to process existing data or collect new data
790!***************
800!
810
        OUTPUT KBD; Clear$;
                                                ! Clear the CRT
820
         OUTPUT KBD; Home$;
                                                  ! Home display
830
         STATUS 1.9;Screen
                                            ! Get screen width
840
                                    ! Leading spaces for centering
        Center=(Screen-28)/2
850
        GCLE^*.
        PRIN1. IS CRT
860
                                      ! Use CRT for displaying menu
870
        PRINT TABXY(1,1)
                                      ! Start at top with blank line
880
        PRINT TAB(Center); "Key
                                     Purpose"
890
        PRINT TAB(Center);"-
900
        PRINT TAB(Center);" 0 Process existing data"
        PRINT TAB(Center);" 4 Collect new data"
910
        PRINT TAB(Center);" 5 Editing existing data"
920
930
        FOR Keynumber=0 TO 9
                                                 ! Off all keys
           ON KEY Keynumber LABEL "" GOSUB Comment1
940
950
        NEXT Keynumber
        ON KEY 0 LABEL "Existing Data" GOTO Existing_data ! Turn on Key 0
960
970
        ON KEY 4 LABEL "New Data" GOTO New_data
                                                            ! Turn on Key 4
980
        ON KEY 5 LABEL "Editing Data" GOTO Editing_data ! Turn on Key 5
990 Blink0: WAIT 1
         DISP "Select an option"
1000
1010
         WAIT 1
1020
         DISP
```

```
1030
         GOTO Blink0
1040
         RETURN
1050!***
1060 New_data: ! Main program driver for collecting new data
1070!**
1080
         GOSUB Clear_keys
1090
         GOSUB Init_param
         GOSUB Init_periph
1100
1110
         GOSUB Input run_data
         GOSUB Create_new_file
1120
1130!
         GOSUB Draw freq time
1140
         GOSUB Draw_mag_time
1150
         GOSUB Take_plot_data
1160
         GOSUB Close_file
1170
         GOSUB Free_periph
1180
         GOSUB Post_process
1190
         STOP
1200!***
1210 Existing_data: ! Main program driver for process existing data
1230
         GOSUB Clear_keys
1240
         GOSUB Open_old_file
1250
         GOSUB Post process
1260
         STOP
1270!***
1280 Editing_data: ! Main program driver to compute Redfreq for old data
1290!*
1300
         Flag=1
         GOSUB Clear_keys
1310
1320
         GOSUB Open_old_file
1330
         GOSUB Calc_redfreq
1340
         GOSUB Create_new_file
1350
         GOSUB Close_file
1360
         STOP
1370!***
1380 Clear keys: ! "Turns off" all softkeys and clears the screen
1390!****
1400
         FOR Keynumber=0 TO 9
           ON KEY Keynumber LABEL "" GOSUB Comment1
1410
1420
         NEXT Keynumber
1430
         OUTPUT KBD; Clear$;
1440
         RETURN
                    1450!****
1460 Init param: ! User sets the minimum and maximum values for initial plot
1470!*****
1480
         Center=(Screen-46)/2
                                    ! Leading spaces for centering
         PRINT TABXY(1,1)
1490
                                     ! Start at top with blank line
         PRINT TAB(Center); "Key
1500
                                    Purpose"
         PRINT TAB(Center);"--
1510
1520
         PRINT TAB(Center);" 0
                                 Set minimum resonance frequency"
        PRINT TAB(Center);" 1
1530
                                 Set maximum resonance frequency"
```

```
1540
         PRINT TAB(Center); 2
                                 Set minimum in phase magnitude"
         PRINT TAB(Center): 3
                                 Set maximum in phase magnitude"
1550
         PRINT TAB(Center);" 5
                                 Set minimum temperature in degrees, C"
1560
         PRINT TAB(Center);" 6
                                 Set maximum temperature in degress, C"
1570
                                 Set the default values"
1580
         PRINT TAB(Center);" 7
         PRINT TAB(Center);" 8
                                 Review the assigned values"
1590
1600
         PRINT TAB(Center): 9
                                  To proceed"
1610!
1620
         ON KEY 0 LABEL "Min Freq, Hz" GOSUB Min_frequency
         ON KEY 1 LABEL "Max Freq, Hz" GOSUB Max_frequency
1630
         ON KEY 2 LABEL "Min Mag, DCV" GOSUB Min mag
1640
         ON KEY 3 LABEL "Max Mag, DCV" GOSUB Max_mag
1650
         ON KEY 4 LABEL "" GOSUB Comment1
1660
1670
         ON KEY 5 LABEL "Min Temp, C" GOSUB Min_temperature
         ON KEY 6 LABEL "Max Temp, C" GOSUB Max_temperature ON KEY 7 LABEL "Default Values" GOSUB Default_values
1680
1690
         ON KEY 8 LABEL "Review values" GOSUB Review values
1700
1710
         ON KEY 9 LABEL "Proceed" GOTO Moveon
1720!
1730 Blink1: WAIT 1
                                   ! Wait for user selection and
1740
           DISP "Select an option"
                                       ! then take appropriate action
1750
            WAIT 1
1760
            DISP
1770
           GOTO Blink1
1780 Moveon: GOSUB Clear_keys
1790
             DISP "Proceeding ....."
1800
            WAIT 1
1810
            DISP
1820
             RETURN
1830!**********
1840 Comment1: ! Alerts user when an unassigned soft key is selected
1850!***************
1860
         BEEP 300,.1
1870
         DISP "This soft key is unassigned"
1880
         WAIT 1
1890
         DISP
1900
         RETURN
1910!*******
1920 Default_values: ! Assigns default values for minimum and maximum T, F
1930!***
1940
         User_freq_min=1650
1950
         User_freq_max=1900
1960
         User_temp_min=0
         User_temp_max=25
1970
         DISP "The Default Values are Set"
1980
1990
         WAIT 1
2000
         GOSUB Review values
2010
         RETURN
2020!***
2030 Min frequency: ! Accepts user input for minimum frequency
```

```
INPUT "The minimum frequency for the ple, in Hz?", User_freq_min
2050
         DISP "The minimum frequency is set at: ";U er_freq_min;" Hz"
2060
2070
         WAIT 1
2080
         DISP
2090
         RETURN
2100!******
2110 Max frequency: ! Accepts user input for maximum frequency
2120!****
         INPUT "The maximum frequency for the plot, in Hz?", User_freq_max DISP "The maximum frequency is set at: "; User_freq_max;" Hz"
2130
2140
2150
         WAIT 1
2160
         DISP
2170
         RETURN
2180!*****
2190 Min_mag: ! Accepts user input for minimum magnitude
2200!**
2210
         INPUT "The minimum magnitude for the plot, in DCV?", User_mag_min
2220
         DISP "The minimum magnitude is set at: ":User mag min
2230
         WAIT 1
2240
         DISP
2250
         RETURN
2260!*****
2270 Max_mag: ! Accepts user input for maximum magnitude
2280!**
2290
         INPUT "The maximum magnitude for the plot, in DCV?", User_mag_max
2300
         DISP "The maximum magnitude is set at: ";User_mag_max
2310
         WAIT 1
2320
         DISP
2330
         RETURN
2340!**
2350 Review values: ! Presents currently assigned values for review
2360!**
2370
         DISP "Minimum frequency: "; User freq_min;" Hz"
2380
2390
         DISP " Maximum frequency: ";User_freq_max;" Hz"
2400
         WAIT 1
2410
         DISP "Minimum magnitude: ":User mag min:" DCV"
2420
         WAIT 1
2430
         DISP "Maximum magnitude: ";User_mag_max;" DCV"
2440
         WAIT 1
         DISP "Minimum temperature: ";User_temp_min;" C"
2450
2460
         WAIT 1
2470
         DISP " Maximum temperature: ";User_temp_max;" C"
         WAIT 1
2480
2490
         DISP
2500
         RETURN
2510!**
2520 Min_temperature: ! Accepts user input of minimum temperature
2530!**
2540
         INPUT "Minimum temperature, degrees C?", User_temp_min
2550
         DISP "The minimum temperature is set at: ";User_temp_min;" C"
```

```
2560
         WAIT 1
2570
         DISP
2580
         RETURN
2590!******
2600 Max temperature: ! Accepts user input of maximum temperature
2610!*
2620
         INPUT "Maximum temperature, degrees C?", User_temp_max
         DISP "The maximum temperature is set at: ";User_temp_max;" C"
2630
2640
         WAIT 1
         DISP
2650
         RETURN
2660
2670!***
2680 Init_periph: ! Initializes the voltmeter and the frequency counter
2690!***
2700!
         720 - HP5316A Universal Counter
2710!
         722 - HP3456A Digital Voltmeter
2720!
         724 - HP3478A Digital Multimeter (added on 23 Jan 91)
2730!
2740
         OUTPUT 720:"IN"
                                               ! Default state
         OUTPUT 722;"HF4R1M66STG100STI"
2750
                                                   ! 2 wire ohms, THMS degrees C
2760
                              ! 100 line cycles integration
         OUTPUT 724:"F1RAN5T1Z1D1"
2770
2780
         RETURN
2790!*********
2800 Free_periph: ! Frees the voltmeter and the counter from the HPIB bus
2810!**
2820
         LOCAL 720
2830
         LOCAL 722
2840
         LOCAL 724
2850
         RETURN
2860!*******
2870 Input_run_data: ! Accepts user input of selected run data
2880!**
2890
         Center=(Screen-42)/2
                                      ! Leading spaces for centering
2900
         PRINT TABXY(1,1)
                                        ! Start at top with blank line
2910
         PRINT TAB(Center);"Key
                                      Purpose"
2920
         PRINT TAB(Center);"-
2930
                                   Enter rod identification"
         PRINT TAB(Center);" 0
                                   Enter the run number for this mode"
2940
         PRINT TAB(Center);" 1
         PRINT TAB(Center);" 2
                                   Enter the mode for this run"
2950
         PRINT TAB(Center);" 3
2960
                                   Enter the date for this run"
2970
                                   Enter the mass for this rod"
         PRINT TAB(Center): 5
2980
         PRINT TAB(Center);" 6
                                   Enter the length for this rod"
         PRINT TAB(Center); 7
PRINT TAB(Center); 8
                                   Enter the diameter for this rod"
2990
                                   Review the information entered"
3000
3010
         PRINT TAB(Center);" 9
                                   To proceed"
3020!
         ON KEY 0 LABEL "Rod ID" GOSUB Rod_id
3030
         ON KEY 1 LABEL "Run No." GOSUB Run_number
3040
         ON KEY 2 LABEL "Mode" GOSUB Mode
3050
3060
         ON KEY 3 LABEL "Date" GOSUB Date
```

```
ON KEY 4 LABEL "" GOSUB Comment1
3070
         ON KEY 5 LABEL "Rod Mass" GOSUB Rod_mass
3080
        ON KEY 6 LABEL "Rod Length" GOSUB Rod_length
3090
        ON KEY 7 LABEL "Rod Diameter" GOSUB Rod_diameter
3100
        ON KEY 8 LABEL "Review entries" GOSUB Review entrys
3110
        ON KEY 9 LABEL "Proceed" GOTO Onward
3120
3130 Blink2: WAIT 1
           DISP "Select an option or proceed"
3140
3150
           WAIT 1
3160
           DISP
           GOTO Blink2
3170
3180 Onward: Volume=(Length/100)*Pi*.25*(Diameter/100)^2
            Density=(Mass/1000)/Volume
3190
            GOSUB Clear_keys
3200
             DISP "Proceeding ..... "
3210
3220
            WAIT 1
3230
            DISP
3240
            RETURN
3250!******
3260 Rod_id: ! Accepts user input of rod identification
3270!******
3280
         INPUT "Rod identification block label (i.e. ECP4)?",Block1$
3290
         WHILE LEN(Block1$)>12
3300
          DISP "Limit Rod Identification to 12 characters"
          BEEP 300,.1
3310
3320
          WAIT 1
3330
          DISP
          INPUT "Rod identification block label (i.e. ECP4)?",Block1$
3340
3350
         END WHILE
3360
         DISP "The Rod ID is set at: ";Block1$
3370
         WAIT 1
         DISP
3380
3390
         RETURN
3400!****
3410 Run number: ! Accepts user input of run number
3420!****
         INPUT "Run number for this mode (i.e. 4)?",Block2$
3430
         DISP "The Run number is set at: ";Block2$
3440
         WAIT 1
3450
3460
         DISP
3470
         RETURN
3490 Mode: ! Accepts user input of the mode
3500!****************
3510
         INPUT "Mode (i.e. Torsional, Longitudinal, Flexural)?",Block3$
3520
         SELECT UPC$(Block3$)
          CASE "FLEXURAL", "TORSIONAL", "LONGITUDINAL"
3530
            DISP "The mode is set as: ";Block3$
3540
3550
            WAIT 1
3560
            DISP
          CASE ELSE
3570
```

```
3580
             BEEP 300,.1
             DISP "Choices are: Torsional, Longitudinal or Flexural"
3590
3600
             WAIT 1
             DISP
3610
3620
            GOTO Mode
         END SELECT
3630
3640
         RETURN
3650!********
                      **************************
3660 Date: ! Accepts user input of run date
3670!**
         INPUT "The date for this sample (i.e. 10 SEP 89)?",Block4$
3680
3690
         WHILE LEN(Block4$)>9
           DISP "Limit date entry to 9 characters"
3700
3710
           BEEP 300,.1
           WAIT 1
3720
3730
           DISP
3740
           INPUT "The date for this sample (i.e. 10 SEP 89)?", Block4$
3750
         END WHILE
3760
         DISP "The Date is set at: ";Blo k4$
3770
         WAIT 1
3780
         DISP
         RETURN
3790
3800!*****
3810 Rod_mass: ! Accepts user input of the rod mass
3820!***
3830
         INPUT "The mass for this rod (units: grams)?", Mass
         DISP "The mass is set at: "; Mass;" grams"
3840
         WAIT 1
3850
         DISP
3860
3870
         RETURN
3880!*****
3890 Rod_length: ! Accepts user input of the rod length
3900!**
3910
         INPUT "The length for this rod (units: centimeters)?".Length
3920
         DISP "The length is set at: ";Length;"centimeters"
3930
         WAIT 1
3940
         DISP
3950
         RETURN
3960!*****
3970 Rod_diameter: ! Accepts user input of the rod diameter
         INPUT "The diameter for this rod (units: centimeters)?", Diameter
3990
         DISP "The diameter is set at: ";Diameter;" centimeters"
4000
4010
         WAIT 1
4020
         DISP
4030
         RETURN
4040!**
4050 Review_entrys: ! Presents currently assigned values for review
4060!****
4070
         DISP "Rod ID: ";Block1$
4080
         WAIT 1
```

```
4090
         DISP "Run: ":Block2$
4100
         WAIT 1
         DISP "Mode: ";Block3$
4110
         WAIT 1
4120
        DISP " Date: ";Block4$
4130
4140
         WAIT 1
4150
         DISP "Mass: ";Mass; "grams"
4160
         WAIT 1
4170
         DISP "Length: ";Length;" centimeters"
4180
         WAIT 1
4190
        DISP "Diameter: ";Diameter;" centimeters"
4200
         WAIT 1
4210
         DISP
4220
         RETURN
4230!***
4240 Draw_mag_time: ! Produces Magnitude vs Time graph w/o curve
4250!**
4260
         Main_title$=Label$(14)
4270
         Sub title$=Label$(2)
4280
         X_axis name$=Label$(3)
4290
         Y axis name$=Label$(13)
4300
         Xmin=0
4310
         Xmax=20
4320
        Ymin=Actual_mag_min
4330
        Ymax=Actual mag max
4340
         GOSUB Generic_plot
4350
         RETURN
4360!***
                          ****************
4370 Draw_freq_time: ! Produces Frequency vs Time graph w/o curve
4380!*
4390
        Main_title$=Label$(1)
4400
        Sub_title$=Label$(2)
4410
        X axis name=Label(3)
4420
        Y axis name$=Label$(4)
4430
         Xmin=0
4440
        Xmax=20
4450
        Ymin=Actual_freq min
                                      ! Actual minimum frequency
4460
        Ymax=Actual freq max
                                       ! Actual maximum frequency
4470
        GOSUB Generic_plot
4480
         RETURN
4490!*
4500 Young_mod: ! Compute Young's modulus in flexure modes
4510!*
4520
        D=Diameter/100
4530
        L=Length/100
4540
        Arg6=Density*((32*L^2)/(Pi*D*Fmode^2))^2
        Eflex(I)=Arg6*Resfreq(I)^2
4550
4560
         RETURN
4570!*
4580 Shear_mod: ! Compute Shear Modulus
4590!*********************
```

```
4600
         D=Diameter/100
4610
         L=Length/100
4620
         Arg5=(Density*4*L^2)/(Tmode^2)
4630
         Gtor(J)=(Arg5*Resfreq(J)^2)
4640
         RETURN
4650!****
4660 Lyoung mod: ! Compute Young's modulus in longitudinal mode
4670!**
4680
         D=Diameter/100
4690
         L=Length/100
4700
         Arg7=(Density*4*L^2)/(Lmode^2)
         Elong(K)=Arg7*Resfreq(K)^2
4710
4720
         RETURN
4730!*****
4740 Compute_redfreq: ! Compute redfreq of new data
4750!****
4760
         Temp(I)=Thermistor(I)+273.15
4770!
          X(I)=-12.9*(Temp(I)-283.15)/(107+Temp(I)-283.15)! PR 1592 only
4780
         X(I)=-21.5*(Temp(I)-211)/(43.1+Temp(I)-211)! Plexi-glass only
4790
         Y(I)=X(I)*LOG(10)
4800
         Alphat(I)=EXP(Y(I))
4810
         Redfreq(I)=Resfreq(I)*Alphat(I)
4820
         RETURN
4830!***
4840 Calc redfreg: ! Convert RT20B to RT20C format
4850!*
         FOR I=0 TO 20*Arg1
4860
4870
           Temp(I)=Thermistor(I)+273.15
4880
            X(I)=-12.9*(Temp(I)-283.15)/(107+Temp(I)-283.15) !PR 1592 only
4890
           Y(I)=X(I)*LOG(10)
4900
           Alphat(I)=EXP(Y(I))
           Redfreq(I)=Resfreq(I)*Alphat(I)
4910
4920
          NEXT I
4930
          RETURN
4940!***
4950 Compute modulus: ! Computes appropriate material modulus based on mode
4960!****
4970
          DISP "Computing appropriate modulus ......"
4980
         D=Diameter/100
                                          ! convert to meters
4990
         L=Length/100
                                         ! convert to meters
5000
         SELECT UPC$(Block3$)
5010
           CASE "FLEXURAL"
            Arg2=Density*((32*L^2)/(Pi*D*Fmode^2))^2
5020
5030
            Eflex_max=Arg2*Actual_freq_max^2
            Power=LOG(Eflex max) DIV LOG(10)
5040
5050
            Scale factor=10^Power
            Scale eflex max=Eflex max/Scale factor
5060
            Scale_eflex_min=(Arg2*Actual_freq_min^2)/Scale_factor
5070
5080
            FOR I=0 TO 20*Arg1
5090
               Eflex(I)=(Arg2*Resfreq(I)^2)/Scale_factor
            NEXT I
5100
```

```
CASE "TORSIONAL"
5110
            Arg3=(Density*4*L^2)/(Tmode^2)
5120
            Gtor_max=Arg3*Actual_freq_max^2
5130
            Power=LOG(Gtor_max) DIV LOG(10)
5140
            Scale_factor=10^Power
5150
            Scale gtor max=Gtor_max/Scale_factor
5160
5170
            Scale gtor min=(Arg3*Actual_freq_min^2)/Scale_factor
            FOR J=0 TO 20*Arg1
5180
              Gtor(J)=(Arg3*Resfreq(J)^2)/Scale_factor
5190
5200
            NEXT J
5210
          CASE "LONGITUDINAL"
5220
            Arg4=(Density*4*L^2)/(Lmode^2)
            Elong_max=Arg4*Actual_freq_max^2
5230
5240
            Power=LOG(Elong max) DIV LOG(10)
5250
            Scale factor=10^Power
            Scale_elong_max=Elong_max/Scale_factor
5260
            Scale elong min=(Arg4*Actual freq_min^2)/Scale_factor
5270
5280
            FOR K=O TO 20*Arg1
5290
              Elong(K)=(Arg4*Resfreq(K)^2)/Scale_factor
            NEXT K
5300
5310
         END SELECT
         DISP
5320
5330
         RETURN
5340!******
5350 Percent moduli: ! Determines the percent change in modulus per degree C
5360!*
5370
         Delta temp=Actual_temp_max-Actual_temp_min
5380
         Fsum2pt=Actual freq max+Actual freq min
5390
         Fdiff2pt=Actual freq max-Actual_freq min
5400
         Fminls=Actual_temp_max*Slope+Intercept
5410
         Fmaxls=Actual_temp_min*Slope+Intercept
5420
         Fsumls=Fmaxls+Fminls
5430
         Fdiffls=Fmaxls-Fminls
         Prcnt_per_c_2pt=100*4*(Fdiff2pt/Fsum2pt)/Delta temp
5440
         Prcnt_per_c_ls=100*4*(Fdiffls/Fsumls)/Delta_temp ! least squares
5450
5460
         RETURN
5470!**
5480 Mag_temp: ! Produces In phase mag vs Temperature graph w/ curve
5490!****
         Main_title$=Label$(15)
5500
5510
         Sub title$=Label$(2)
5520
         X_axis_name$=Label$(5)
         Y axis name$=Label$(13)
5530
5540
         Xmin=Actual_temp_min
         Xmax=Actual_temp_max
5550
         Ymin=Actual_mag_min
5560
5570
         Ymax=Actual_mag_max
5580
         GOSUB Generic_plot
         CALL Generic_curve(Pen3,Thermistor(*),Inphmag(*),20*Arg1)
5590
5600
         RETURN
```

```
5610!**
5620 Mag_freq: !Produces In phase mag vs Resonant frequencies
5630!*
5640
         Main title$=Label$(16)
         Sub_title$=" "
5650
5660
         X_axis_name=Label$(4)
         Y_axis_name$=Label$(13)
5670
5680
         Xmin=Actual freq min
5690
         Xmax=Actual freq max
5700
         Ymin=Actual mag min
5710
         Ymax=Actual mag_max
5720
         GOSUB Generic_plot
5730
         CALL Generic curve(Pen3, Resfreq(*), Inphmag(*), 20*Arg1)
         RETURN
5740
5750!***
5760 Shear temp: ! Produces Shear modulus vs Temperature graph w/ curve
5770!*
5780
         Main_title$=Label$(10)
         Sub_title$=" "
5790
5800
         X axis name$=Label$(5)
5810
         Y axis name$=Label$(11)&VAL$(Power)
                                        ! Actual minimum temperature
5820
         Xmin=Actual temp_min
5830
         Xmax=Actual_temp_max
                                         ! Actual maximum temperature
5840
         Ymin=Scale_gtor_min
                                      ! Scaled minimum shear modulus
5850
         Ymax=Scale_gtor_max
                                      ! Scaled maximum shear modulus
5860
         GOSUB Generic_plot
5870
         CALL Generic curve(Pen3.Thermistor(*),Gtor(*),20*Arg1)
5880
         RETURN
5890!********
5900 Young_temp: ! Produces Young's modulus vs Temperature graph w/ curve
5910!*
5920
         Main_title$=Label$(9)
         Sub title$=""
5930
         X axis_name$=Label$(5)
5940
5950
         Y_axis_name$=Label$(12)&VAL$(Power)
         Xmin=Actual_temp_min
                                        ! Actual minimum temperature
5960
5970
         Xmax=Actual_temp_max
                                         ! Actual maximum temperature
5980
         SELECT UPC$(Block3$)
5990
          CASE "FLEXURAL"
            Ymin=Scale_eflex_min
                                      ! Scaled minimum Y (flexural)
6000
                                       ! Scaled maximum Y (flexural)
            Ymax=Scale_eflex_max
6010
6020
            GOSUB Generic_plot
6030
            CALL Generic_curve(Pen3,Thermistor(*),Eflex(*),20*Arg1)
          CASE "LONGITUDINAL"
6040
6050
            Ymin=Scale elong min
                                     ! Scaled minimum Y (longitudinal)
                                      ! Scaled maximum Y (longitudinal)
6060
            Ymax=Scale elong max
6070
            GOSUB Generic_plot
            CALL Generic_curve(Pen3,Thermistor(*),Elong(*),20*Arg1)
6080
         END SELECT
6090
         RETURN
6100
```

```
6110!*************************
6120 Generic plot: ! Produces design and layout of line graph
6130!**
6140
         GINIT
                          ! Initialize various graphics parameters
         GCLEAR
6150
                                  ! Clear the graphics display
         GRAPHICS ON
                                     ! Turn the graphics display on
6160
                                               ! Clear the CRT
6170
         OUTPUT KBD:Clear$:
6180!
6190
         IF Plot device$="Plotter" THEN ! Route output to HP7475A plotter
6200
           GRAPHICS OFF
6210
           BEEP 1000..1
          DISP "Press CONTINUE when the plotter is ready"
6220
6230
          PAUSE
6240
           OUTPUT 705;"IP 1300,1000,9000,6750;"
                                                   ! Sets scaling points
6250
           PLOTTER IS 705,"HPGL"
6260
         END IF
6270!
6280
         Xgdumax=100*MAX(1,RATIO)
                                            ! How many gdu's wide screen is
6290
                                            ! How many gdu's high screen is
         Ygdumax=100*MAX(1.1/RATIO)
6300
          CALL Scale(.02,.98,.10,.98,Top,Left,Xcntr,Ycntr,Xgdumax,Ygdumax)
6310
         PEN Pen2
         FRAME
6320
6330!
6340
         IF LEN(Main title$)>30 THEN
                                                ! Size main title
6350
           CALL Label(4,.6,0,6,Pen2,Xcntr,Top-2,Main title$)
6360
6370
           CALL Label(6,.6,0,6,Pen2,Xcntr,Top-2,Main title$)
6380
         END IF
6390!
6400
         CALL Label(4,.6,0,6,Pen2,Xcntr,.9*Top,Sub_title$)
         CALL Block info(Block1$Block2$Block3$Block4$XgdumaxPen5Pen2)
6410
6420
         CALL Scale(.15,.90,.25,.8,Top,Left,Xcntr,Ycntr,Xgdumax,Ygdumax)
6430
         CLIP OFF
         CALL Label(4,.6,0,4,Pen5,Xcntr,-18,X_axis_name$)
6440
6450
         CALL Label(4,.6,90,4,Pen5,-12,Ycntr,Y_axis_name$)
6460
         CLIP ON
6470!
         SELECT Xscale$
6480
          CASE "Auto scale X"
                                           ! Auto scale X axis
6490
6500
            CALL Xscale(Xmin, Xmax, Xminor, Xmajor)
          CASE "User scale X"
                                           ! User scale X axis
6510
            SELECT Pass$
6520
              CASE "Initial"
6530
                                          ! Initial pass
                                    ! Minimum time, hours
6540
               Xmin=0
               Xmax=20
                                     ! Maximum time, hours
6550
6560
               Xmajor=1
                Xminor=.5
6570
              CASE "Follow on"
                                      ! Use user modified values
6580
6590
               Xmin=Xmin manual
               Xmax=Xmax_manual
6600
               Xmajor=Xmajor_manual
6610
```

```
6620
               Xminor=Xminor manual
6630
            END SELECT
         END SELECT
6640
6650!
         SELECT Yscale$
6660
6670
          CASE "Auto scale Y"
                                         ! Auto scale Y axis
            CALL Yscale(Ymin, Ymax, Yminor, Ymajor)
6680
6690
          CASE "User scale Y"
                                         ! User scale Y axis
6700
            SELECT Pass$
6710
             CASE "Initial"
                                         ! Initial pass
6720!
               Ymin=User freq min
                                      ! Use user entered min freq
6730!
               Ymax=User_freq_max
                                    ! Use user entered maximum freq
6740
               Ymin=User mag min
                                     ! Use user entered min mag
6750
               Ymax=User mag max
                                     ! Use user entered max mag
6760
               Ymajor=(Ymax-Ymin)/5
               Yminor=Ymajor/5
6770
               Pass$="Follow on"
6780
               Xscale$="Auto scale X"
6790
6800
               Yscale$="Auto scale Y"
              CASE "Follow on"
                                      ! Use user modified values
6810
6820
               Ymin=Ymin manual
6830
               Ymax=Ymax_manual
6840
               Ymajor=Ymajor_manual
6850
               Yminor=Yminor manual
6860
            END SELECT
6870
         END SELECT
         WINDOW Xmin, Xmax, Ymin, Ymax
6880
6890!
6900
         CALL Lbl_axes(2,.6,Pen4,Xmin,Xmax,Xmajor,Ymin,Ymax,Ymajor)! Axes
6910
         PEN Pen2
6920
         AXES Xminor, Yminor, Xmin, Ymin, Xmajor/Xminor, Ymajor/Yminor, 3
6930
         AXES Xminor, Yminor, Xmax, Ymax, Xmajor/Xminor, Ymajor/Yminor, 3
6940!
6950
         SELECT Grid_type$
                                                ! Grid
6960
          CASE "Partial"
6970
            GRID Xmajor, Ymajor, Xmin, Ymin
6980
          CASE "Full"
6990
            GRID Xminor, Yminor, Xmin, Ymin, Xmajor/Xminor, Ymajor/Yminor, 1
         END SELECT
7000
7010!
7020
         PENUP
7030
         GRAPHICS ON
7040
         RETURN
7050!******************
7060 Take plot data: ! Collects frequency vs temperature data during the run
7070!***
7080
        ON KEY 0 LABEL "Take Data" GOTO Take
         FOR Keynumber=1 TO 9
7090
7100
           ON KEY Keynumber LABEL "" GOSUB Comment1
7110
         NEXT Keynumber
7120 Wait: GOTO Wait
```

```
7130 Take: ON KEY 0 LABEL "" GOSUB Comment1
7140
         PEN Pen3
         OUTPUT KBD; "Taking data .....";
7150
        T0=TIMEDATE
7160
         SELECT UPC$(Block3$)
7170
7180
           CASE "FLEXURAL"
            FOR I=0 TO 20*Arg1
7190
7200
              ENTER 720; Resfreq(I)
              ENTER 722:Thermistor(I)
7210
              ENTER 724;Inphmag(I)
7220
              Time(I)=I/Arg1
7230
              PLOT Time(I), Inphmag(I)
7240
7250
               GOSUB Compute redfreq
7260
               GOSUB Young_mod
               OUTPUT @Path 1:Eflex(I), Thermistor(I), Resfreq(I), Inphmag
7270
(I).Redfreq(I)
               DISP I
7280
               WAIT 295.787 !Adjustment for 1 sample every 5 minutes
7290
7300
             NEXT I
          CASE "TORSIONAL"
7310
7320
            FOR J=0 TO 20*Arg1
              ENTER 720; Resfreq(J)
7330
7340
              ENTER 722:Thermistor(J)
              ENTER 724:Inphmag(J)
7350
              Time(J)=J/Arg \hat{I}
7360
7370
              PLOT Time(J), Inphmag(J)
              GOSUB Compute_redfreq
7380
              GOSUB Shear mod
7390
7400
              OUTPUT @Path_1;Gtor(J),Thermistor(J),Resfreq(J),Inphmag(J
),Redfreq(J)
              DISP J
7410
              WAIT 295.787
7420
7430
            NEXT J
7440
          CASE "LONGITUDINAL"
7450
            FOR K=0 TO 20*Argi
              ENTER 720; Resfreq(K)
7460
              ENTER 722:Thermistor(K)
7470
              ENTER 724:Inphmag(K)
7480
              Time(K)=K/Arg1
7490
              PLOT Time(K), Inphmag(K)
7500
              GOSUB Compute_redfreq
7510
              GOSUB Lyoung mod
7520
              OUTPUT @Path 1; Elong(K), Thermistor(K), Resfreq(K), Inphmag(
7530
K), Redfreq(K)
7540
              DISP K
               WAIT 295.787
7550
7560
             NEXT K
7570
         END SELECT
         T1=TIMEDATE
7580
         DISP "IT TOOK ";DROUND(T1-T0,4);"SECONDS"
7590
7600
         WAIT 10
```

```
! Clears the CRT
7610
         OUTPUT KBD; Clear$;
7620
         BEEP
         ON KEY 0 LABEL "Post Process" GOTO 7650
7630
7640 Wait1: GOTO Wait1
         RETURN
7650
7660!********
7670 Post process: ! Permits user to extract plots, tables, and other info
7680!**
7690
         GCLEAR
7700
          CALL Least squares(20*Arg1, Thermistor(*), Resfreq(*), A,B,C,D,E,F,G)
7710
                       ! Keeps call to Least squares to one program line
7720
         Intercept=B
7730
         Correlation=C
7740
         Slope error=D
7750
         Intropterr=E
         Tmean=F
7760
7770
         Fmean=G
7780!
7790
         Actual temp min=MIN(Thermistor(*)) ! Find maximum and minimum
7800
         Actual temp_max=MAX(Thermistor(*)) ! temperature and frequency
7810
         Actual_freq_min=MIN(Resfreq(*))
7820
         Actual freq max=MAX(Resfreq(*))
7830
         Actual mag min=MIN(Inphmag(*))
7840
         Actual mag max=MAX(Inphmag(*))
7850!
7860
         Volume=.25*(Length/100)*Pi*(Diameter/100)^2
7870
         GOSUB Percent moduli
7880
         GOSUB Compute_modulus
7890!
7900
                                                  ! Clear the CRT
         OUTPUT KBD:Clear$:
7910
         OUTPUT KBD:Home$:
                                                    ! Home display
7920
         GCLEAR
7930
         PRINT TABXY(1,1)
                                        ! Start at top with bleank line
7940
         Center=(Screen-42)/2
                                       ! Leading spaces for centering
7950
         PRINT TAB(Center); "Key
                                          Purpose"
7960
         PRINT TAB(Center);"---
         PRINT TAB(Center); "0 Plot Frequency vs Time"
7970
         PRINT TAB(Center);" 1 Plot Temperature vs Time"
PRINT TAB(Center);" 2 Plot Frequency vs Temperature"
7980
7990
8000
         SELECT UPC$(Block3$)
8010
           CASE ="TORSIONAL"
             PRINT TAB(Center);" 3 Plot Shear modulus vs Temperature"
8020
           CASE ="FLEXURAL"
8030
             PRINT TAB(Center): 3 Plot Young's modulus vs Temperature"
8040
           CASE ="LONGITUDINAL"
8050
8060
             PRINT TAB(Center); 3 Plot Young's modulus vs Temperature
8070
         END SELECT
         PRINT TAB(Center);" 4 Send Information to the Printer"
8080
         PRINT TAB(Center);" 5 Select the graph output device"
PRINT TAB(Center);" 6 Plot In phase mag vs Temperature"
8090
8100
         PRINT TAB(Center);" 7 Plot In phase mag vs Temperature"
8110
```

```
PRINT TAB(Center);" 7 Select the type of X axis scaling"
8120
        PRINT TAB(Center);" 8 Select the type of Y axis scaling'
PRINT TAB(Center);" 9 Exit this program"
8130
8140
8150!
         ON KEY 0 LABEL "Freq vs Time" GOSUB Freq_time
8160
        ON KEY 1 LABEL "Temp vs Time" GOSUB Temp_time
8170
         ON KEY 2 LABEL "Freq vs Temp" GOSUB Freq_temp
8180
8190
         SELECT UPC$(Block3$)
          CASE ="TORSIONAL"
8200
            ON KEY 3 LABEL "G vs Temp" GOSUB Shear_temp
8210
8220
          CASE ="FLEXURAL"
8230
            ON KEY 3 LABEL "E vs Temp" GOSUB Young_temp
8240
          CASE ="LONGITUDINAL"
8250
            ON KEY 3 LABEL "E vs Temp" GOSUB Young_temp
8260
          CASE ELSE
            ON KEY 3 LABEL "" GOSUB Comment1
8270
8280
         END SELECT
8290
         ON KEY 4 LABEL "Print Info" GOSUB Dump_info
8300
         ON KEY 5 LABEL "Output Device" GOSUB Output device
         ON KEY 6 LABEL "Grid Option" GOSUB Grid_option
8310!
         ON KEY 6 LABEL "Imag vs Temp" GOSUB Mag_temp
8320
         ON KEY 7 LABEL "X scale option" GOSUB Xscale_option
8330!
8340
         ON KEY 7 LABEL "Imag vs Freq" GOSUB Mag_freq
8350
         ON KEY 8 LABEL "Y scale option" GOSUB Yscale_option
8360
         ON KEY 9 LABEL "Exit Program" GOSUB Program_end
8370!
8380 Blink3: WAIT 1
         DISP "Make a DECISION"
8390
8400
         WAIT 1
8410
         DISP
8420
         GOTO Blink3
8430
         RETURN
8450 Grid option: ! Accepts the user's choice for the plot grid
8460!***************
8470
         GRAPHICS OFF
                                      ! Turns off graphics display
8480
         OUTPUT KBD; Clear$;
                                              ! Clears the CRT
         DISP Grid_type$;" grid is currently selected"
8490
8500
         INPUT "Enter F - full; P - partial; N - No grid?", Response$
8510
         SELECT Response$
          CASE "F"
8520
8530
            Grid_type$="Full"
          CASE "P"
8540
            Grid_type$="Partial"
8550
          CASE "N"
8560
8570
            Grid type$="No"
          CASE ELSE
8580
8590
            DISP "No change"
            WAIT 1
8600
            DISP
8610
            WAIT 1
8620
```

```
8630
        END SELECT
        DISP Grid_type$;" grid is selected"
8640
8650
         WAIT 1
         DISP
8660
8670
        RETURN
8680!****
8690 Dump info: ! Sends selected data and table information to the printer
8700!**************
8710
         PRINTER IS 701
8720
         Perfskip$=CHR$(27)&CHR$(38)&CHR$(108)&CHR$(49)&CHR$(76)
8730
         Formfeed$=CHR$(12)
8740
        PRINT Perfskip$
                                      ! Skip on Perforation
        PRINT Formfeed$
8750
        PRINT USING "3/,#"
8760
                                          ! Three line feeds
        PRINT "Rod: "&Block1$;TAB(70);"Page 1 of 2"
8770
                      "&Block2$
8780
        PRINT "Run:
        PRINT "Mode: "&Block3$
8790
        PRINT "Date: "&Block4$
8800
8810
        PRINT USING "3/,#"
                                       ! Three more line feeds
8820!
8830
        C1$="Time"
8840
        C2$="Temperature"
         C3$="Frequency"
8850
         C4a$="Shear modulus"
8860
8870
         C4b$="Young's modulus"
8880
         C5$="In Phase Component"
         C6$="hours"
8890
8900
         C7$="deg C"
8910
         C8\$="Hz"
8920
         C9$="Pa*10^"
        C10$="DCV"
8930
8940!
8950
        SELECT UPC$(Block3$)
          CASE "TORSIONAL"
8960
8970
            PRINT USING 8980;C1$,C2$,C3$,C4a$,C5$
8980
            IMAGE 4A,6X,11A,5X,9A,5X,13A,5X,18A
8990
            PRINT
            PRINT USING 9010;C6$,C7$,C8$,C9$,Power,C10$
9000
9010
            IMAGE 5A,8X,5A,11X,2A,12X,6A,ZZ,14X,3A,12X
9020
            PRINT
9030
           FOR I=0 TO 20*Arg1 STEP Arg1
9040
            PRINT USING 9050; Time(I), Thermistor(I), Resfreq(I), Gtor(I), In
phmag(I)
9050
                                        IMAGE
                                                 X,3D,8X,SDD.DDD,4X,
DDDD.DDDE,9X,D.DDD,13X,SDD.DDDDDE
9060
            NEXT I
9070
          CASE "FLEXURAL"
9080
            PRINT USING 9140;C1$,C2$,C3$,C4b$,C5$
9090
            PRINT
            PRINT USING 9010;C6$,C7$,C8$,C9$,Power,C10$
9100
9110
           PRINT
```

```
FOP J=0 TO 20*Arg1 STEP Arg1
9120
9130
              P: NT USING 9050:Time(J), Thermistor(J), Resfreq(J), Eflex(J)
,Inphmag(I)
               IMAGE 4A.6X,11A,5X,9A,5X,15A,3X,18A
9140
            NEXT J
9150
           CASE "LONGITUDINAL"
9160
9170
             PRINT USING 9140;C1$,C2$,C3$,C4b$,C5$
9180
            PRINT
             PRINT USING 9010;C6$,C7$,C8$,C9$,Power,C10$
9190
9200
            PRINT
9210
            FOR K=0 TO 20*Arg1 STEP Arg1
9220
              PRINT USING 9050; Time(K), Thermistor(K), Resfreq(K), Elong(K)
,Inphmag(I)
9230
            NEXT K
         END SELECT
9240
9250!
9260
         PRINT Formfeed$
                                      ! Advance to top of next page
         PRINT USING "3/.#"
9270
                                           ! Three more line feeds
         PRINT "Rod:
                       "&Block1$:TAB(70);"Page 2 of 2"
9280
                        "&Block2$
9290
         PRINT "Run:
         PRINT "Mode: "&Block3$
9300
9310
         PRINT "Date: "&Block4$
9320!
         PRINT USING "3/,#"
                                           ! Three more line feeds
9330
9340
         PRINT "Physical properties:"
9350
         PRINT
9360
         PRINT USING "3X,12A,14X,DDD.DDD"; "Mass, grams: ",Mass
         PRINT USING "3X,20A,06X,DDD,DDD"; "Length, centimeters:",Length
9370
         PRINT USING "3X.22A.04X.DDD.DDD": "Diameter, centimeters: ", Diameter
9380
         PRINT USING "3X,21A,07X,D.DDDE"; "Volume, cubic meters:", Volume
9390
         PRINT USING "3X,16A,09X,DDDD.D"; "Density, kg/m^3:", Density
9400
9410!
9420
         PRINT USING "3/.#"
                                           ! Three more line feeds
9430
         PRINT "Least-squares fit results [frequency versus temperature]:"
9440
         PRINT
         PRINT USING "3X.12A.13X.DDDD.DDD": "Slope, Hz/C:", Slope
9450
         PRINT USING "3X,18A,07X,DDDD.DDD"; "Slope error, Hz/C:", Slope_error
9460
         PRINT USING "3X,14A,11X,DDDD.DDD"; "Intercept, Hz: ",Intercept
9470
         PRINT USING "3X,20A,05X,DDDD.DDD"; "Intercept error, Hz:",Intrepterr
9480
         PRINT USING "3X,12A,13X,DDDD.DDDDD"; "Correlation: ",Correlation
9490
         PRINT USING "3X,20A,05X,DDDD.DDD"; "Mean temperature, C:",Tmean PRINT USING "3X,19A,06X,DDDD.DDD"; "Mean frequency, Hz:",Fmean
9500
9510
         PRINT
9520
         PRINT
9530
         PRINT "Other statistics:"
9540
9550
         PRINT
9560
         Tmin=Actual temp min
9570
         Tmax=Actual temp max
9580
         Tave=(Tmax+Tmin)/2
         Fmin=Actual_freq_min
9590
9600
         Fmax=Actual_freq_max
```

```
9610
         Fave=(Fmax+Fmin)/2
9620
         PRINT USING "3X,23A,02X,DDDD.DDD";"Minimum temperature, C:",Tmin
         PRINT USING "3X,23A,02X,DDDD.DDD";"Average temperature, C:",Tave
9630
             PRINT USING "3X,23A,02X,DDDD.DDD"; "Maximum temperature,
9640
C:",Tmax
9650
         PRINT
         PRINT USING "3X,22A,03X,DDDD.DDD"; "Minimum frequency, Hz:",Fmin PRINT USING "3X,22A,03X,DDDD.DDD"; "Average frequency, Hz:",Fave
9660
9670
9680
              PRINT USING "3X,22A,03X,DDDD.DDD"; "Maximum frequency,
Hz:",Fmax
9690
         PRINT
9700
         L1$="Percent change in shear modulus per degree C: "
9710
         L2$="Percent change in Young's modulus per degree C:"
9720
         L3$="Two point max-min approach:"
9730
        LA$="Multi-point least-squares approach:"
9740
         SELECT UPC$(Block3$)
9750
          CASE "TORSIONAL"
9760
            Gmin=Scale_gtor_min
9770
            Gmax=Scale_gtor_max
9780
                         PRINT USING "3X,30A,ZZ,5X,D.DDD"; "Minimum
"&C4a$,Power,Gmin
9790
                         PRINT USING "3X,30A,ZZ,5X,D.DDD";"Maximum
"&C4a$.Power,Gmax
9800
            PRINT USING "3/.#"
                                        ! Three more line feeds
9810
            PRINT L1$
9820
            PRINT
9830
            PRINT USING "3X,27A,8X,DDD.DDD";L3$,Prcnt per c 2pt
            PRINT USING "3X,35A,DDD.DDD";L4$,Prcnt_per_c_ls
9840
9850
          CASE "FLEXURAL"
9860
           Emin=Scale_eflex_min
9870
           Emax=Scale_eflex_max
9880
                         PRINT USING "3X,30A,ZZ,5X,D.DDD"; "Minimum
"&C4b$,Power,Emin
9890
                         PRINT USING "3X,30A,ZZ,5X,D.DDD":"Maximum
"&C4b$.Power.Emax
9900
            PRINT USING "3/,#"
                                        ! Three more line feeds
9910
            PRINT L2$
9920
            PRINT
9930
            PRINT USING "3X,27A,8X,DDD.DDD";L3$,Prcnt per c 2pt
9940
            PRINT USING "3X,35A,DDD.DDD";L4$,Prent per c ls
          CASE "LONGITUDINAL"
9950
9960
           Emin=Scale elong min
9970
           Emax=Scale_elong_max
9980
                         PRINT USING "3X,32A,ZZ,5X,D.DDD"; "Minimum
"&C4b$,Power,Emin
9990
                         PRINT USING "3X,32A,ZZ,5X,D.DDD"; "Maximum
"&C4b$,Power,Emax
                                        ! Three more line feeds
10000
            PRINT USING "3/,#"
            PRINT L2$
10010
10020
            PRINT
10030
            PRINT USING "3X,27A,8X,DDD.DDD";L3$,Prcnt_per_c_2pt
```

```
10040
            PRINT USING "3X,35A,DDD.DDD"; L4$, Prent_per_c_ls
10050
         END SELECT
         PRINT Formfeed$
10060
                                   ! Advance to top of next page
10070
         PRINTER IS CRT
10080
         RETURN
10100 Freq_time:! Produces frequency vs time graph w/curve
10120
         GOSUB Draw_freq_time
10130
         CALL Generic_curve(Pen3,Time(*),Resfreq(*),20*Arg1)
10140
         RETURN
10150!***
10160 Output device: ! Permits user to route graphs to the screen or plotter
10170!******************
10180
         OUTPUT KBD:Clear$;
                                            ! Clear the CRT
10190
         OUTPUT KBD; Home$;
                                              ! Home display
10200
         GRAPHICS OFF
                                  ! Turn off the graphics display
10210
         SELECT Plot device$
10220
          CASE <> "Plotter"
10230
            INPUT "Graphs appear on the screen, OK? (Y/N) ",Response$
            IF UPC$(Response$)<>"Y" THEN
10240
             Plot_device$="Plotter"
10250
10260
             DISP "Graphs will be sent to the Plotter"
10270
            ELSE
10280
             DISP "Graphs will remain on the screen"
10290
             WAIT 1
             DISP
10300
10310
             GRAPHICS ON
10320
            END IF
10330
          CASE "Plotter"
10340
            INPUT "Graphs are sent to the plotter, OK? (Y/N) ", Response$
            IF UPC$(Response$) > "Y" THEN
10350
             Plot_device$="Screen"
10360
10370
             DISP "Plots will be sent to the Screen"
10380
10390
             DISP "Plots will stay routed to the plotter"
10400
            END IF
10410
         END SELECT
10420
         WAIT 1
10430
         DISP
         RETURN
10440
10450!**
10460 Xs.:ale_option: ! Permits user to auto scale or manual scale the X axis
! Clear the CRT
10480
         OUTPUT KBD:Clear$:
         OUTPUT KBD; Home$;
                                              ! Home display
10490
         GRAPHICS OFF
                                  ! Turn off the graphics display
10500
10510
        SELECT Xscale$
          CASE "Auto scale X"
10520
           INPUT "X axis is automatically scaled, OK? (Y/N) ", Response$
10530
            IF Response$<>"Y" THEN
10540
```

```
10550
               Xscale$="User scale X"
               INPUT "Minimum X axis value?", Xmin_manual
10560
10570
               INPUT "Maximum X axis value?",Xmax_manual
               INPUT "Major X axis increment?", Xmajor_manual
10580
               INPUT "Minor X axis increment?", Xminor_manual
10590
10600
               DISP "The X axis will be scaled manually"
10610
             ELSE
               DISP "The X axis will remain auto scaled"
10620
10630
               WAIT 1
               DISP
10640
10650
               GRAPHICS ON
10660
             END IF
10670
           CASE "User scale X"
             INPUT "X axis is manually scaled, OK? (Y/N) "Response$
10680
             IF Response$<\rightarrow\"Y" THEN
10690
               Xscale$="Auto scale X"
10700
               DISP "The X axis will be scaled automatically"
10710
10720
             ELSE
               INPUT "Change manual limits? (Y/N) ",Response$
10730
               IF Response$="Y" THEN
10740
                INPUT "Minimum X axis value?",Xmin_manual
10750
                INPUT "Maximum X axis value?", Xmax_manual
10760
10770
                INPUT "Major X axis increment?", Xmajor_manual
10780
                INPUT "Minor X axis increment?".Xminor manual
10790
                DISP "The X axis will be scaled with new values"
10800
               ELSE
10810
                DISP "The X axis will remain manually scaled"
10820
                WAIT 1
10830
                DISP
                GRAPHICS ON
10840
10850
               END IF
            END IF
10860
          END SELECT
10870
          WAIT 1
10880
10890
          DISP
          RETURN
10900
10910!***
10920 Yscale option: ! Permits user to auto scale or manual scale the Y axis
10930!**
10940
          OUTPUT KBD; Clear$;
                                                 ! Clear the CRT
                                                   ! Home display
10950
          OUTPUT KBD:Home$:
10960
                                      ! Turn off the graphics display
          GRAPHICS OFF
10970
         SELECT Yscale$
10980
           CASE "Auto scale Y"
             INPUT "Y axis is automatically scaled, OK? (Y/N) ", Response$
10990
             IF Response$<>"Y" THEN
11000
               Yscale$="User scale Y"
11010
              INPUT "Minimum Y axis value?", Ymin_manual
11020
              INPUT "Maximum Y axis value?", Ymax_manual
11030
              INPUT "Major Y axis increment?", Ymajor_manual
11040
              INPUT "Minor Y axis increment?", Yminor manual
11050
```

```
11060
               DISP "The Y axis will be scaled manually"
11070
             ELSE
               DISP "The Y axis will remain auto scaled"
11080
11090
               WAIT 1
               DISP
11100
11110
               GRAPHICS ON
11120
             END IF
11130
            CASE "User scale Y"
             INPUT "Y axis is manually scaled, OK? (Y/N) ", Response$
11140
             IF Response$<>"Y" THEN
11150
               Yscale$="Auto scale Y"
11160
               DISP "The Y axis will be scaled automatically"
11170
11180
             ELSE
11190
               INPUT "Change manual limits? (Y/N) ",Response$
11200
               IF Response$="Y" THEN
11210
                 INPUT "Minimum Y axis value?", Ymin_manual
                 INPUT "Maximum Y axis value ?", Ymax_manual INPUT "Major Y axis increment ?", Ymajor_manual
11220
11230
                 INPUT "Minor Y axis increment?", Yminor_manual
11240
11250
                 DISP "The Y axis will be scaled with new values"
11260
               ELSE
11270
                 DISP "The Y axis will remain manually scaled"
                 WAIT 1
11280
11290
                 DISP
11300
                 GRAPHICS ON
11310
               END IF
11320
            END IF
          END SELECT
11330
          WAIT 1
11340
11350
          DISP
          RETURN
11360
11370!
11380 Temp_time: ! Produces Temperature vs Time graph w/curve
11390!*
11400
          Main_title$=Label$(7)
11410
          Sub title$=Label$(8)
11420
          X_axis_name=Label$(3)
11430
          Y axis name$=Label$(5)
11440
          Xmin=0
                                    ! Minimum time is 0 hours
11450
          Xmax=20
                                     Maximum time is 20 hours
11460
                                           ! Actual minimum temperature
          Ymin=Actual_temp_min
11470
          Ymax=Actual_temp_max
                                           ! Actual maximum temperature
11480
          GOSUB Generic_plot
11490
          CALL Generic_curve(Pen3,Time(*),Thermistor(*),20*Arg1)
11500
          RETURN
11510!*
11520 Freq_temp: ! Produces Frequency versus temperature graph w/curve
11530!*
11540
          Main_title$=Label$(6)
11550
          Sub_title$=""
          X_axis_name$=Label$(5)
11560
```

```
11570
         Y axis name$=Label$(4)
         Xmin=Actual temp min
                                         ! Actual minimum temperature
11580
         Xmax=Actual_temp_max
                                         ! Actual maximum temperature
11590
          Ymin=Actual_freq_min
                                         ! Actual minimum frequency
11600
         Ymax=Actual_freq_max
                                         ! Actual maximum frequency
11610
11620
          GOSUB Generic_plot
11630
          CALL Generic curve(Pen3, Thermistor(*), Resfreq(*), 20*Arg1)
          PEN Pen4
11640!
         MOVE Actual_temp_min,Actual_temp_min*Slope+Intercept
11650!
11660!
          DRAW Actual temp max.Actual temp max*Slope+Intercept
11670!
          PEN 0
          RETURN
11680
11690!****
11700 Create new file: ! Creates a file for a new data run
11710!***
          Pass$="Initial"
11720
11730
          Grid_type$=Default_grid$
11740
          Xscale$="User scale X"
          Yscale$="User scale Y"
11750
          Plot device$="Screen"
11760
11770
          BEEP 1000,.1
          ON ERROR GOTO Fix2
11780
11790
           INPUT "Filename to store the data?", Filename$
           CREATE BDAT Filename$.50
11800
           ASSIGN @Path_1 TO Filename$
11810
11820
          OFF ERROR
          OUTPUT @Path_1;Block1$,Block2$,Block3$,Block4$
11830
          OUTPUT @Path 1:Mass,Length,Diameter,Density
11840
11850
          BEEP 1000,.1
          DISP "Output will be stored under Filename: ";Filename$
11860
11870
          WAIT 1
          DISP
11880
11890
          IF Flag=1 THEN
11900
           FOR I=0 TO 20*Arg1
11910
               OUTPUT @Path 1:Mod(I), Thermistor(I), Resfreq(I), Inphmag(I),
Redfreq(I)
           NEXT I
11920
11930
          END IF
11940
          RETURN
11950!*
11960 Open_old_file: ! Opens and retrieves data from an existing file
11970!****
11980
          Pass$="Follow on"
          Grid type$=Default_grid$
11990
          Xscale$="Auto scale X'
12000
          Yscale$="Auto scale Y"
12010
          Plot device$="Screen"
12020
          BEEP 1000..1
12030
12040
          ON ERROR GOTO Fix 1
12050
           INPUT "Filename to retrieve the data?", Filename$
           ASSIGN @Path_1 TO Filename$
12060
```

```
12070
          ENTER @Path 1;Block1$,Block2$,Block3$,Block4$
12080
          ENTER @Path_1; Mass, Length, Diameter, Density
          BEEP 1000..1
12090
12100
          DISP "Retrieving data stored under Filename: ":Filename$
12110
          FOR I=0 TO 20*Arg1
12120
            ENTER @Path_1; Mod(I), Thermistor(I), Resfreq(I), Inphmag(I), Red
freq(I)
12130
            Time(I)=I/Arg1
12140
          NEXT I
12150
         OFF ERROR
12160
         ASSIGN @Path 1 TO *
12170
         RETURN
12180!****
12190 Fix1: !
12200!**********************
12210
         SELECT ERRN
12220
         CASE 53
          DISP "Limit file names to 10 characters. No punctuation."
12230
12240
         CASE 56
12250
          DISP "This file doesn't exist on the data disk"
12260
         CASE 58
12270
          DISP "This file is not a BDAT file"
12280
         CASE ELSE
12290
          DISP "This file can not be processed by RT20B"
12300
         END SELECT
12310
         PRINTER IS CRT
12320
         BEEP 300..1
12330
        WAIT 1
12340
         DISP
12350
         WAIT 1
        GOTO Open_old_file
12360
12370!************************
12380 Fix2: !
12400
        SELECT ERRN
12410
        CASE 53
12420
          DISP "Limit file names to 10 characters. No punctuation."
12430
        CASE 54
12440
          DISP "Duplicate filename! Try another name."
12450
        END SELECT
         BEEP 300..1
12460
12470
        WAIT 1
12480
        DISP
12490
        WAIT 1
        GOTO Create_new_file
12500
12510!*****
12520 Close_file: ! Closes new data file after data collection is completed
12530!**
        GCLEAR
12540
        ASSIGN @Path 1 TO *
12550
12560
        BEEP 1000..1
```

```
DISP "Data is stored under Filename: ":Filename$
12570
12580
         WAIT 1
12590
         DISP
12600
         RETURN
12610!******
12620 Program end: ! Shuts down shop, plays a little melody
12630!**********
12640
         OUTPUT KBD; Clear$;
12650
         GRAPHICS OFF
12660
         CONTROL 1,12:0
12670
         BEEP 157..1
         BEEP 201,.1
12680
12690
         BEEP 178..1
         BEEP 272..1
12700
12710
         WAIT .5
         BEEP 272,.1
12720
12730
         BEEP 178..1
         BEEP 157..1
12740
         BEEP 201,.1
12750
12760
         DISP
12770
         DISP "Press RUN when you are ready for another try ...."
12780
12790!*******
12800 SUB Label(Csize, Asp. ratio, Ldir, Lorg, Pen, Xpos, Ypos, Text$)
12810!******
12820!
       This subroutine defines several systems variables (Csize, LDIR, etc.),
12830!
       and labels the text (if any) accordingly.
12840
       DEG
12850
       CSIZE Csize, Asp_ratio
12860
      LDIR Ldir
12870
      LORG Lorg
12880
       PEN Pen
12890
       MOVE Xpos, Ypos
       IF Text$$\hfinship\" THEN LABEL USING "#,K";Text$
12900
12910
       PENUP
12920
       SUBEND
12940 SUB Lbl axes(Csize, Asp ratio, Pen, Xmin, Xmax, Xstep, Ymin, Ymax, Ystep)
12960
12970
       CSIZE Csize, Asp_ratio
12980
       PEN Pen
12990
       CLIP OFF
13000
      LDTR 0
13010
      LORG 6
13020
       Yrange=Ymax-Ymin
13030
       Yoffset=.02*Yrange
13040
       FOR L=Xmin TO Xmax STEP Xstep
13050
         MOVE L, Ymin-Yoffset
13060
         IF ABS(L) < .001 THEN L=0
         LABEL USING "#.K":L
13070
```

```
13080
      NEXT L
13090
      LORG 8
      Xoffset=.02*(Xmax-Xmin)
13100
13110
       IF Yrange<=1 THEN
13120
        Mmax=DROUND(Yrange/Ystep,1)
13130
        Yval=Ymin
13140
        FOR M=0 TO Mmax
13150
          IF ABS(Yval)<=.001 THEN Yval=0
          MOVE Xmin-Xoffset, Yval
13160
          LABEL USING "#,SD.DD";Yval
13170
          Yval=Yval+Ystep
13180
13190
        NEXT M
13200
       ELSE
        FOR M=Ymin TO Ymax STEP Ystep
13210
          IF ABS(M) \le .001 THEN M=0
13220
          MOVE Xmin-Xoffset.M
13230
          LABEL USING "#,K":M
13240
13250
        NEXT M
13260
       END IF
13270
       CLIP ON
13280
       PENUP
13290
       SUBEND
13300!********************************
13310 SUB Block_info(Block1$,Block2$,Block3$,Block4$,Xgdumax,Pen,Pen2)
13320!***********************
13330
       CALL Label(3,.6,0,2,Pen,2,2,"Rod: "&Block1$)
       CALL Label(3,.6,0,5,Pen,Xgdumax/3,2,"Run: "&Block2$)
13340
13350
       CALL Label(3,.6,0,5,Pen,Xgdumax*2/3,2,"Mode: "&Block3$)
       CALL Label(3,.6,0,8,Pen,.97*Xgdumax,2,Block4$)
13360
13370
      MOVE 0.4
      PEN Pen2
13380
13390
      DRAW 133.4
13400
       PENUP
13410
       SUBEND
13420!*******
13430 SUB Least_squares(Imax,X(*),Y(*),Slp,Int,Cor,Slp_er,Int_er,Xmean,Ymean)
13440!*****************
       DISP "Computing least-squares fit ......"
13450
13460
       Sumx=0
13470
       Sumy=0
       Sumxx=0
13480
13490
       Sumxy=0
       FOR I=0 TO Imax
13500
         Sumx=Sumx+X(I)
13510
13520
         Sumxx=Sumxx+X(I)^2
13530
         Sumy=Sumy+Y(I)
         Sumxy=Sumxy+X(I)*Y(I)
13540
13550
       NEXT I
       Delta=(Imax+1)*Sumxx-Sumx^2
13560
       Int=(Sumxx*Sumy-Sumx*Sumxy)/Delta
13570
13580
       Slp=((Imax+1)*Sumxy-Sumx*Sumy)/Delta
```

```
13590
       Sumerrerr=0
13600
       FOR J=0 TO Imax
13610
           Sumerrerr=Sumerrerr+(Y(J)-Int-Slp*X(J))^2
13620
       NEXT J
13630
       Sigmayy=Sumerrerr/(Imax+1-2)
       Sigmay=SOR(Sigmayy)
13640
       Int_er=Sigmay*SQR(Sumxx/Delta)
13650
       Sly er=Sigmay*SQR((lmax+1)/Delta)
13660
       Xbarsum=0
13670
13680
       Ybarsum=0
13690
       FOR K=0 TO Imax
13700
          Xbarsum=Xbarsum+X(K)
         Ybarsum=Ybarsum+Y(K)
13710
13720
       NEXT K
13730
       Xmean=Xbarsum/(Imax+1)
13740
       Ymean=Ybarsum/(Imax+1)
       Sigmaxxsum=0
13750
       Sigmavvsum=0
13760
       Sigmaxysum=0
13770
       FOR L=O TO Imax
13780
13790
          Sigmaxxsum=Sigmaxxsum+(X(L)-Xmean)^2
13800
         Sigmayysum=Sigmayysum+(Y(L)-Ymean)^2
         Sigmaxysum=Sigmaxysum+(X(L)-Xmean)*(Y(L)-Ymean)
13810
13820
       NEXT L
13830
       Sigmax=SQR(Sigmaxxsum/(Imax+1))
13840
       Sigmav1=SOR(Sigmavvsum/(Imax+1))
13850
       Sigmaxy=Sigmaxysum/(Imax+1)
13860
       Cor=Sigmaxy/(Sigmax*Sigmay1)
13870
       DISP
13880
       SUBEND
13890!******
13900 SUB Scale(L,R,B,T,Top,Left,Xcenter,Ycenter,Xgdumax,Ygdumax)
13910!*
13920
       Top=T*Ygdumax
       Bottom=B*Ygdumax
13930
       Left=L*Xgdumax
13940
13950
       Right=R*Xgdumax
13960
       Xcenter=(Right+Left)/2
13970
       Ycenter=(Top+Bottom)/2
13980
        VIEWPORT Left Right Bottom, Top
13990
       SUBEND
14000!*******
14010 SUB Yscale(Ymin, Ymax, Yminor, Ymajor)
14020!***********
14030
       DIM Diff(36), Minor(36)
         DATA .1,.005,.2,.01,.25,.01,.3,.02,.4,.02,.5,.02,.75,.05,1,.05
14040
         DATA 5..2,10..5,15,1,20,1,25,1,30,2,40,2,50,2,75,5,100,5,125,5
14050
        DATA 150,10,200,10,250,10,300,20,400,20,500,20,750,50,1000,50
14060
        DATA 1250.50.1500.100.2000.100.2500.100.3000.200.4000.200.5000
14070
14080
        DATA 200,7500,500,10000,500
       FOR I=1 TO 36
14090
```

```
14100
         READ Diff(I),Minor(I)
14110
       NEXT I
14120
       Yrange=Ymax-Ymin
14130
       Index=1
       WHILE Yrange>Diff(Index)
14140
         Index=Index+1
14150
       END WHILE
14160
       Yminor=Minor(Index)
14170
       Ymajor=Diff(Index)/5
14180
14190
       IF Ymin<0 THEN
14200
         Newmin=Ymin-Ymajor+ABS(Ymin MOD Ymajor)
14210
       ELSE
14220
         Newmin=Ymin-(Ymin MOD Ymajor)
14230
       END IF
14240
       Newmax=Newmin+Diff(Index)
14250
       WHILE Ymax>Newmax
         Index=Index+1
14260
14270
         Yminor=Minor(Index)
         Ymajor=Diff(Index)/5
14280
14290
         IF Ymin<0 THEN
14300
           Newmin=Ymin-Ymajor+ABS(Ymin MOD Ymajor)
14310
14320
           Newmin=Ymin-(Ymin MOD Ymajor)
14330
          END IF
14340
         Newmax=Newmin+Diff(Index)
       END WHILE
14350
14360
       Ymax=Newmax
       Ymin=Newmin
14370
14380
       SUBEND
14390!***********************
14400 SUB Xscale(Xmin, Xmax, Xminor, Xmajor)
14420
       DIM Diffx(40), Minorx(40), Majorx(40)
          DATA 5.,0.2,1.0,6.,.2,1.,7.0,0.2,1.0,8.0,0.2,1.0,10.0,0.5,2.0,12.0,0.5
14430
         DATA 2.0,14.0,0.5,2.0,16.0,0.5,2.0,20.0,1.0,4.0,25.0,1.0,5.0,30.0,1.0
14440
14450
         DATA 5.0,35.0,1.0,5.0,40.0,1.0,5.0,50.0,2.0,10.0,60.,2.0,10.0,70.0,2.0
         DATA 10.0,80.0,2.0,10.0,100.0,5.0,20.0,120.0,5.0,20.0,140.0,5.0,20.0
14460
14470
         DATA 200.0,10.0,20.0,400.0,10.0,50.0,600.0,20.0,100.0,800.0,50.0,100.0
         DATA 1000.0,50.0,100.0,1200.0,50.0,200.0,1400.0,50.0,200.0,1600.0
14480
         DATA 50.0.200.0.1800.0.100.0.300.0.2000.0.100.0.500.0.2500..100..500.0
14490
         DATA 3000.,100.,500.0,3500.,100.,500.0,4000.,200.,400.0
14500
14510
       FOR I=1 TO 34
14520
         READ Diffx(I), Minorx(I), Majorx(I)
14530
       NEXT I
14540
       Xrange=Xmax-Xmin
14550
       Index=1
14560
       WHILE Xrange>Diffx(Index)
14570
          Index=Index+1
       END WHILE
14580
14590
       Xminor=Minorx(Index)
       Xmajor=Majorx(Index)
14600
```

```
14610
      IF Xmin<0 THEN
        Newmin=Xmin-Xmajor+ABS(Xmin MOD Xmajor)
14620
14630
      ELSE
14640
        Newmin=Xmin-(Xmin MOD Xmajor)
      END IF
14650
14660
      Newmax=Newmin+Diffx(Index)
14670
       WHILE Xmax>Newmax
        Index=Index+1
14680
        Xminor=Minorx(Index)
14690
14700
        Xmajor=Majorx(Index)
        IF Xmin<0 THEN
14710
14720
          Newmin=Xmin-Xmajor+ABS(Xmin MOD Xmajor)
14730
14740
          Newmin=Xmin-(Xmin MOD Xmajor)
14750
        END IF
14760
        Newmax=Newmin+Diffx(Index)
14770
      END WHILE
       Xmax=Newmax
14780
14790
      Xmin=Newmin
      SUBEND
14800
14810!*****************************
14820 SUB Generic_curve(Pen,X(*),Y(*),Max_point)
14830!******************
14840
      PEN Pen
14850
      FOR Point=0 TO Max point
14860
        PLOT X(Point), Y(Point)
14870
      NEXT Point
14880
      PENUP
14890
      SUBEND
14900!******
14910! Nothing follows.
14920!***********
14930!**********
14940!********************
14950 SUB Calc_redfreq(Imax, Thermistor(*), Resfreq(*), Redfreq(*))
14960!*****************
14970
      FOR I=0 TO Imax
14980
        Temp(I)=Thermistor(I)+273.15
14990
         X(I)=-129*(Temp(I)-283.15)/(107+Temp(I)-283.15)
        Y(I)=X(I)*LOG(10)
15000
15010
        Alphat(I)=EXP(Y(I))
        Redfreq(I)=Resfreq(I)*Alphat(I)
15020
15030
       NEXT I
       SUBEND
15040
```

## APPENDIX E. LISTING OF HP BDAT FILE TO MACINTOSH TEXT FILE CONVERSION PROGRAM

```
10 PRINTER IS CRT:WIDTH 80
```

- 20 PRINT "\*\*\*\*\*
- 30 PRINT "\*PROGRAM HPTOMAC: Program to transfer BDAT files on the HP to"
- 40 PRINT "TEXT files readable by Cricket Graph on the Macintosh."
- 50 PRINT "Ref. pp. C-6 and C-17 of the Cricket Graph User's Manual."
- 60 PRINT "Author: Steve Baker Last revision date: 10 Aug 1989"
- 70 PRINT "\*HARDWARE REQUIRED: HP Series 200 with 98644A serial interface or"
- 80 PRINT "Series 300 with built-in interface, Macintosh with built-in serial"
- 90 PRINT "interface, Hayes modern cable for the Macintosh (DB-9 or Din-8 to"
- 100 PRINT "male DB-25 connectors. Ref. p.G-5 of the VersaTerm Pro User's"
- 110 PRINT "Manual), standard male-male RS-232 cable with at least pins 1-8"
- 120 PRINT "and 20 wired straight through for the HP. These cables can each"
- 130 PRINT "be hooked up directly to a modem, or they can be connected to each"
- 140 PRINT "other through a null modern with the following pins connected:"
- 150 PRINT "1to1, 2to3, 3to2, 4and5to8, 6to20, 7to7, 8to4and5, 20to6."
- 160 PRINT "\*SOFTWARE REQUIRED: HPTOMAC running on an HP Series 200/300 and a"
- 170 PRINT "communications program capable of faithfully capturing incoming"
- 180 PRINT "text (ASCII characters) to a TEXT-type file running on the Mac,
- 190 PRINT "such as MacTerm (desk accessory bundled with Borland SideKick) or"
- 200 PRINT "VersaTerm PRO. NOTE: text captured by Microsoft Works cannot be"
- 210 PRINT "read by Cricket Graph."
- 220 PRINT "\*INSTRUCTIONS FOR USE:"
- 230 PRINT "Both serial ports must be set to 2400 baud, 8 data bits, one stop"
- 240 PRINT "bit, no parity. The following will correctly set up both machines"
- 250 PRINT "following power-up."
- 260 PRINT "\*SETTING UP THE HP: HPTOMAC asks for the select code of the"
- 270 PRINT "serial port and sets the baud rate to 2400 baud. The other"
- 280 PRINT "settings are automatic at startup, so no additional user action is"
- 290 PRINT "required (Ref. p. 13-10 of Vol.2 of BASIC Interfacing Techniques)."
- 300 PRINT "\*SETTING UP MACTERM: launch the ""Configure MacTerm"" utility and"
- 310 PRINT "click on the appropriate buttons to set serial port parameters"
- 320 PRINT "(Ref. p. 107 of SideKick v2.0 User's Manual). Clicking on ""Save"
- 330 PRINT "Setup" saves these settings. The serial port parameters may also"
- 340 PRINT "be set in the ""MacTerm"" menu while running MacTerm (MacTerm is"
- 350 PRINT "launched from the desk accessory menu)."
- 360 PRINT "\*SETTING UP VERSATERM PRO: Launch VersaTerm PRO. Set the baud'
- 370 PRINT "rate to 2400 in the ""Baud"" menu. Enable Xon/Xoff, set Parity to"
- 380 PRINT "none, Char Size to 8 bits, and Stop Bits to 1.0 in the"
  390 PRINT """Settings"" menu. Other features may be enabled and disabled in"
- 400 PRINT "the ""Extras"" dialog box, selected from the ""Settings"" menu"
- 410 PRINT "(Ref. pp. F-15 to F-18 of the User's Manual). Be sure that ""Auto"
- 420 PRINT "Tek 4014 Entry"" is disabled."
- 430 PRINT "\*TRANSFERRING A BDAT FILE from the HP to the Mac is accomplished"
- 440 PRINT "in text recording mode under MacTerm (ref. p. 109 in User's"
- 450 PRINT "Manual) and in Save Stream mode under VersaTerm PRO (ref. pp."
- 460 PRINT "B-28, F-8, F-13, F-15 in the User's Manual). Refer to each User's

```
470 PRINT "Manual for details. HPTOMAC is self-prompting."
480 PRINT "*NOTE that PROG files may also be transferred over the serial port"
490 PRINT "connection simply by LOADing each PROG file into the HP's memory"
500 PRINT "and issuing a LIST #Sc command, where Sc is the select code of the"
510 PRINT "serial port. The setup and procedure for receiving a PROG file"
520 PRINT "under MacTerm or VersaTerm PRO is identical to that for receiving"
530 PRINT "a BDAT file."
550 !
560 !****PROGRAM BEGINS HERE**********************
570 !
580 DIM Ch$[1],Name$(100)[31]
581 DIM C1$[50],C2$[50],C3$[50],C4$[50]
590 INTEGER Outdev J.N
600 PRINT "PROGRAM HPTOMAC: Program to transfer BDAT files on the HP to
TEXT"
610 PRINT "files readable by Cricket Graph on the Macintosh. Detailed"
620 PRINT "instructions for using this program are in the comments above."
630 BEEP
640 PRINT
650 PRINT "**** MAKE SURE THE MAC SERIAL PORT IS SET TO 2400 BAUD,
8 DATA"
660 PRINT "BITS, 1 STOP BIT, NO PARITY *****"
670 PRINT
680 MASS STORAGE IS ":.4.0"
690 PRINT "Mass storage default has been set to: .4.0"
700 INPUT "Enter select code of output device (CRT=1, PRT=701, Serial Port=9 o
r 10):",Outdev
710 IF Outdev=9 OR Outdev=10 THEN CONTROL Outdev,3;2400
720 INPUT "Enter name of source data file:", Srcfile$
730 ASSIGN @Path1 TO Srcfile$
740 INPUT "Enter number of elements per record (1 to 100):",N
750 IF N<1 OR N>100 THEN GOTO 740
760 INPUT "Do you want to send element names? (Y or N, default is N)", Ch$
770 IF Ch$="Y" OR Ch$="y" THEN
    Ch$="Y"
780
790
    FOR I=1 TO N
800
      PRINT "Enter name of ":I;"th element:"
810
      LINPUT Name$(I)
820 NEXT I
830 END IF
840 INPUT "Hit CONTINUE to continue", Ch$
850 PRINT
860 PRINT "Sending output to device select code ";Outdev
870 PRINTER IS Outdev: WIDTH OFF
880 IF Ch$="Y" THEN
    PRINT "*"
890
900
    FOR I=1 TO N-1
910
     PRINT Name$(I);CHR$(9);
920
     NEXT I
930 PRINT Name$(N)
```

```
940 END IF
950 ON END @Path1 GOTO 1040
951 ENTER @Path1;C1$,C2$,C3$,C4$
952 ENTER @Path1; Mass, Length, Diameter, Density
960 REPEAT
970 FOR I=1 TO N-1
980
     ENTER @Path1;Data
990
     PRINT Data; CHR$(9);
1000 NEXT I
1010 ENTER @Path1; Data
1020 PRINT Data
1030 UNTIL False
1040 OFF END @Path1
1050 ASSIGN @Path1 TO *
1060 BEEP
1070 PRINTER IS CRT; WIDTH 80
1080 PRINT "Transfer complete. Close Mac file."
1090 PRINT "Open new Mac file and enter HP source file name to transfer"
1100 INPUT "another file with the same attributes or hit RUN to restart:", Srcfi
le$
1110 ASSIGN @Path1 TO Srcfile$
1120 GOTO 840
1130 END
```

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